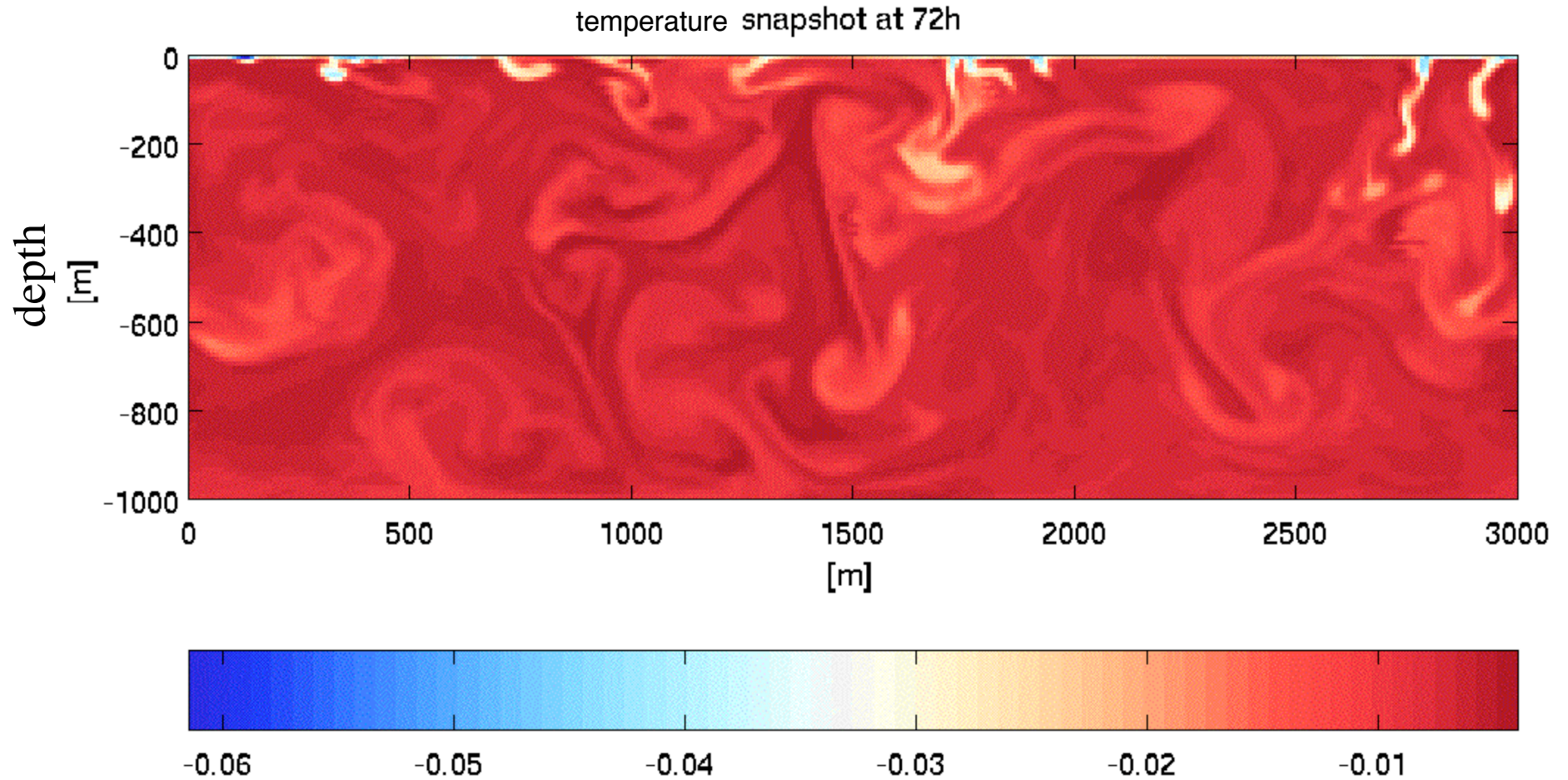




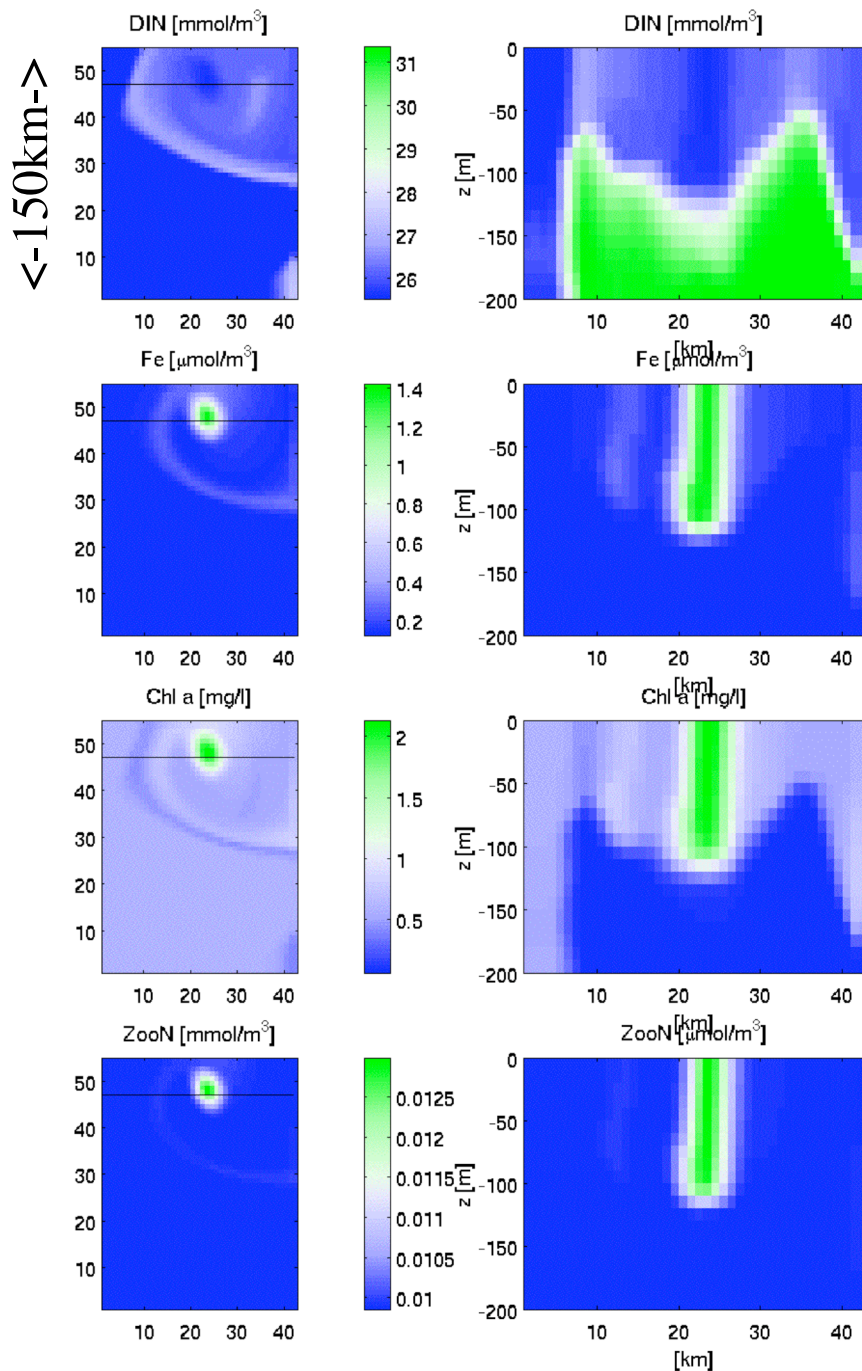
- Very accurately measures gravity, geoid, SSH
- serves as place holder for other high accuracy data
- Are ocean models up to this challenge?

LES, vertical mixing

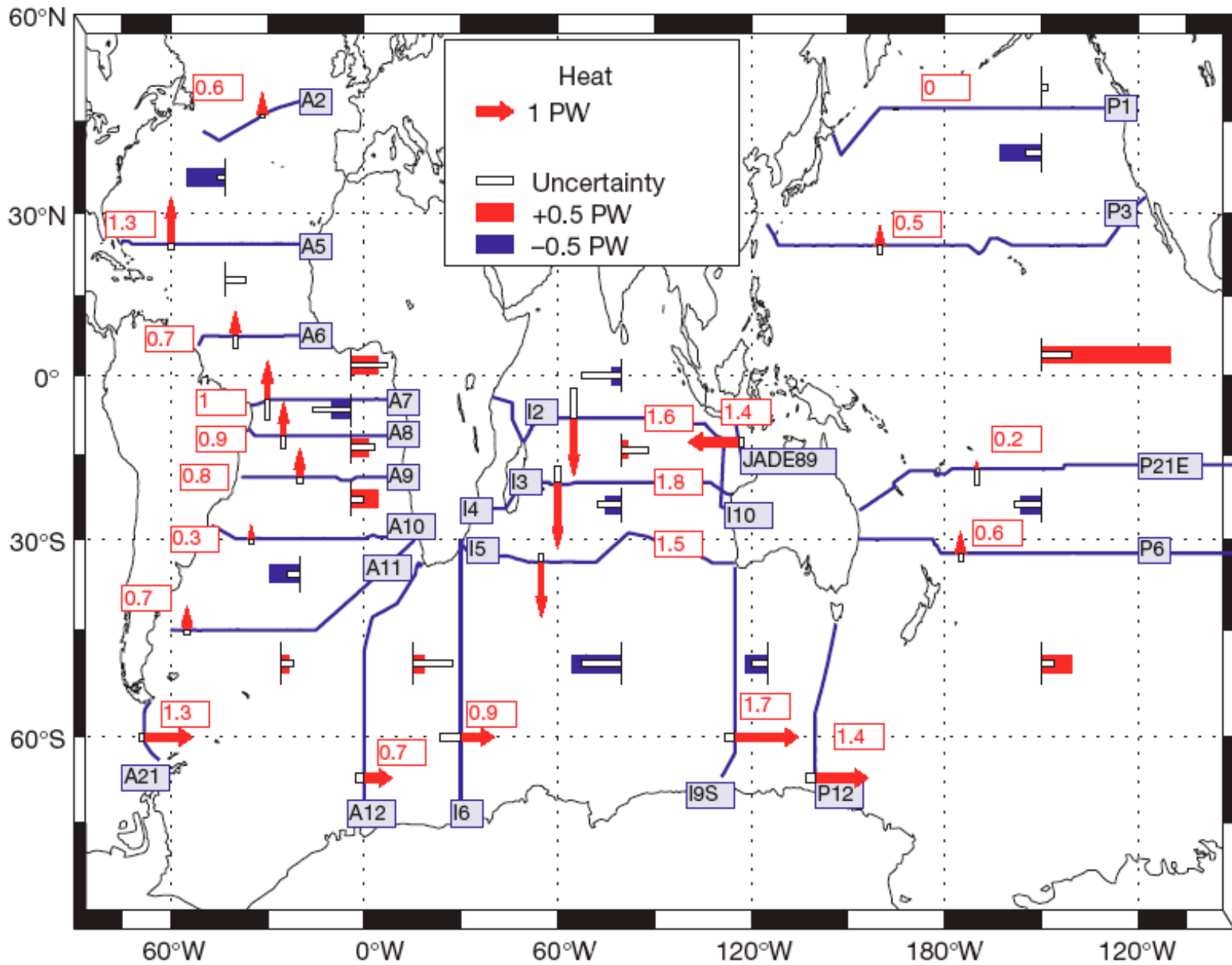


with V.Gryanik

day 30

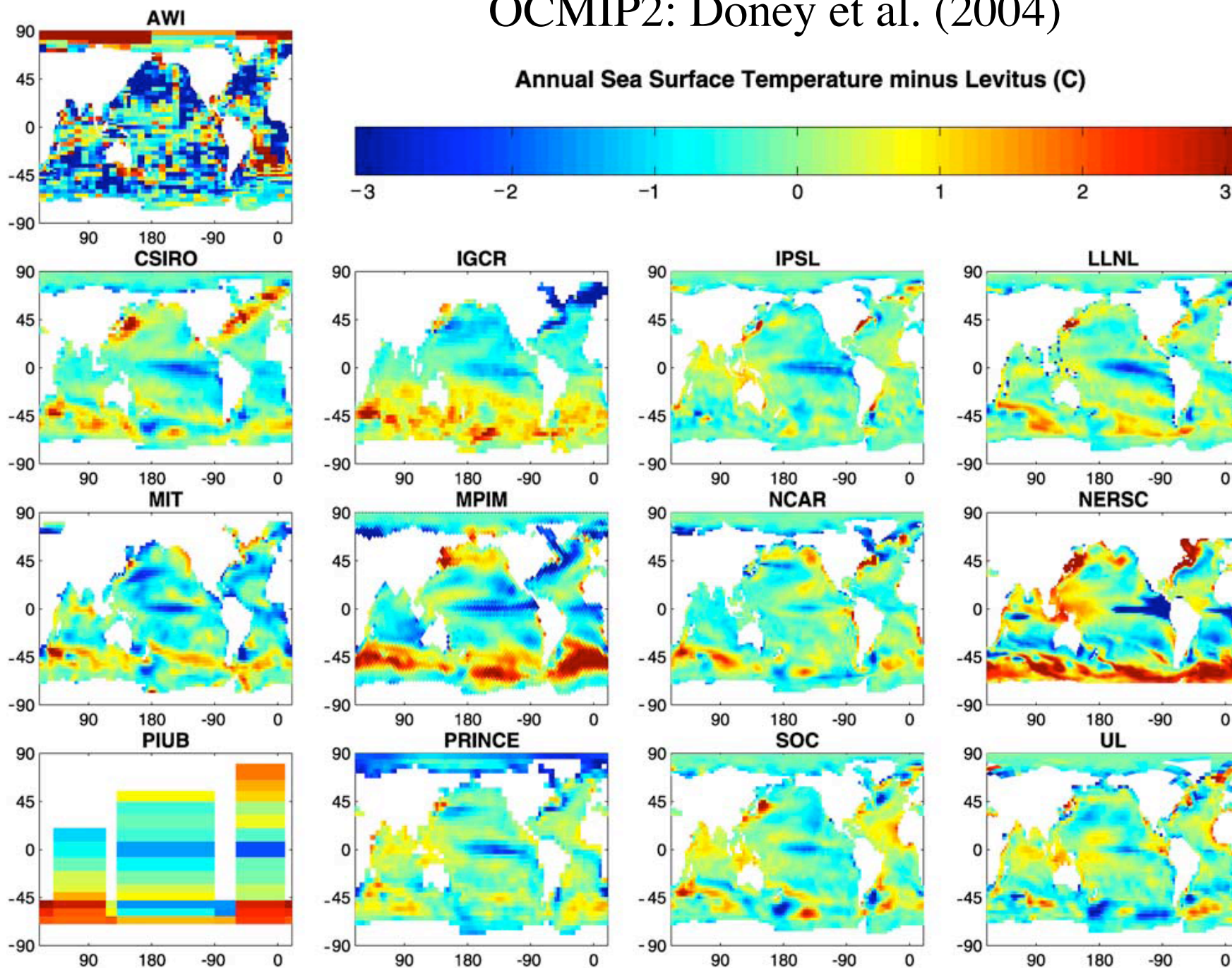


Regional model in
the Antarctic Polar
Frontal Zone:
EIFEX analysis with
MITgcm and
REcoM
(with M. Schartau,
V. Strass)



Ganachaud and Wunsch (2000)

OCMIP2: Doney et al. (2004)



Estimating the accuracy of ocean circulation models

Martin Losch

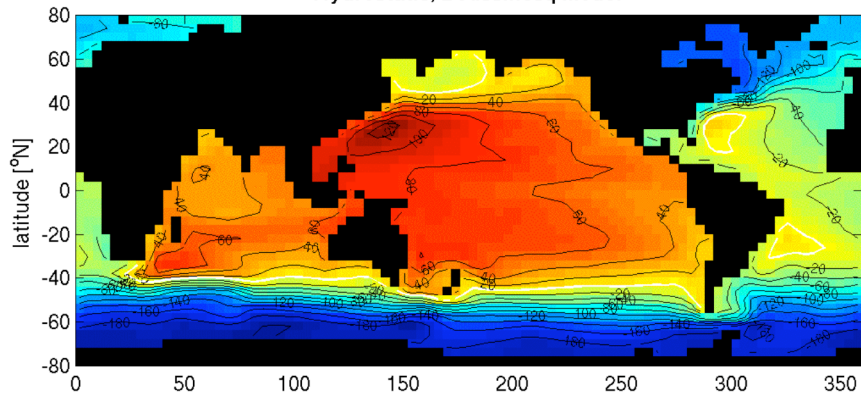
- To what extent can we trust ocean model-based estimates?
- random errors -> parameter perturbation, adjoint sensitivity
- systematic errors (very hard to assess) -> comparison to measurements; leads to state estimation with formal error estimates

A. perturbation experiments (“brute force”)

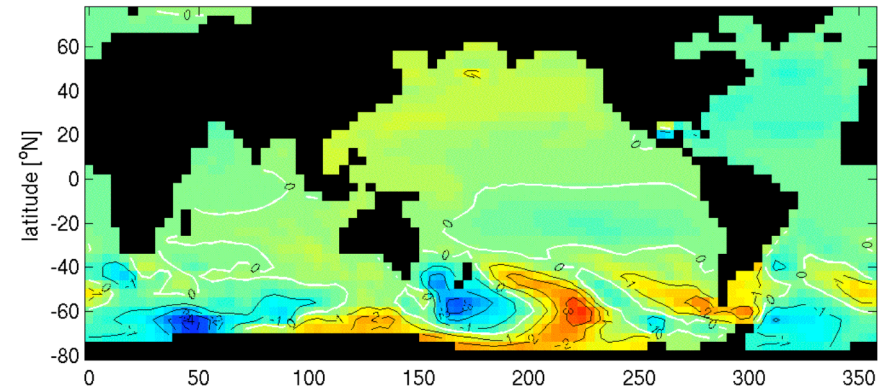
- perturb 1 parameter, observe effect
- perturb next parameter, etc.
 - Problem: very costly, if systematic
- ensemble methods, Monte Carlo methods
 - choose ensemble of experiments and compare ensemble members, determine spread of solutions
 - Problems: what is the optimal ensemble size, how do you choose the ensemble?
- Example: Losch, Adcroft, and Campin (2004)

Mean SSH and changes to mean SSH

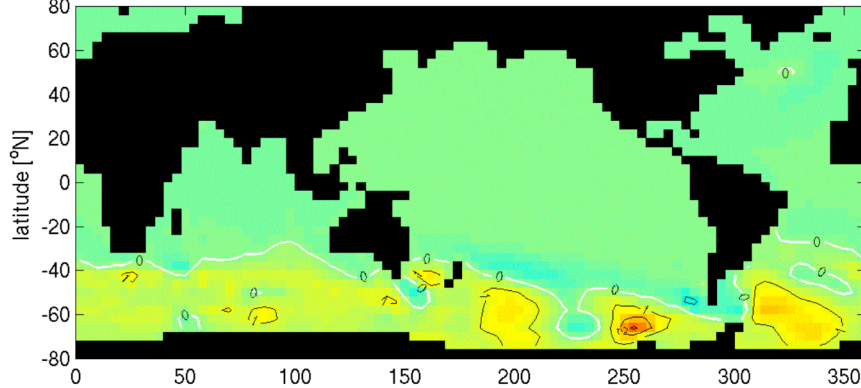
Hydrostatic, Boussinesq model



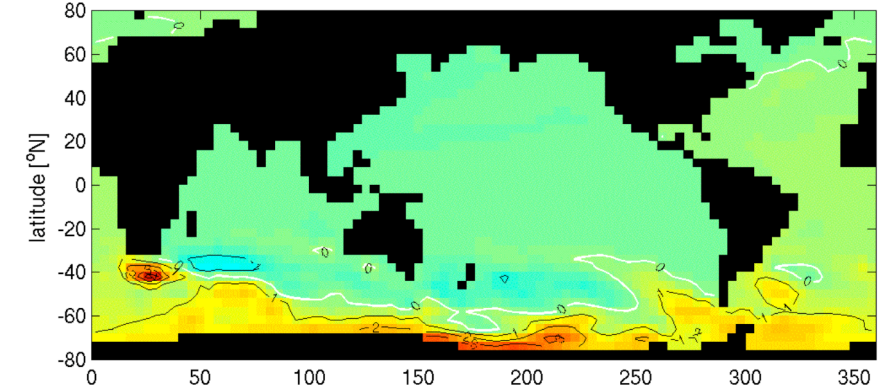
Boussinesq - non-Boussinesq



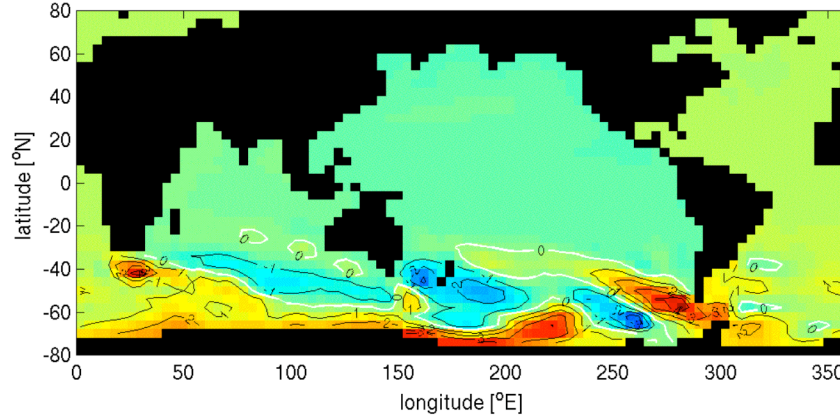
Boussinesq Hydrostatic - Boussinesq Quasi-Hydrostatic



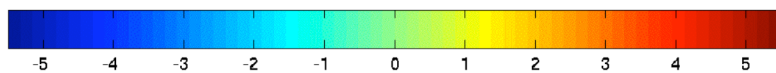
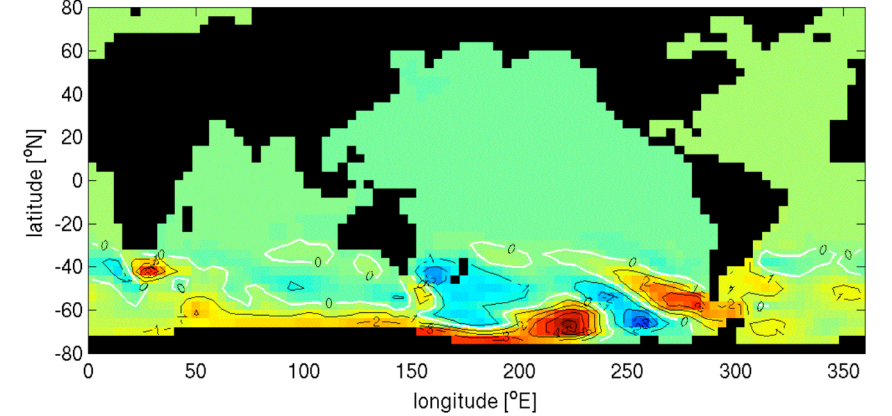
Difference due to changed EOS



Difference due to perturbed diffusivity



Difference due to perturbed forcing

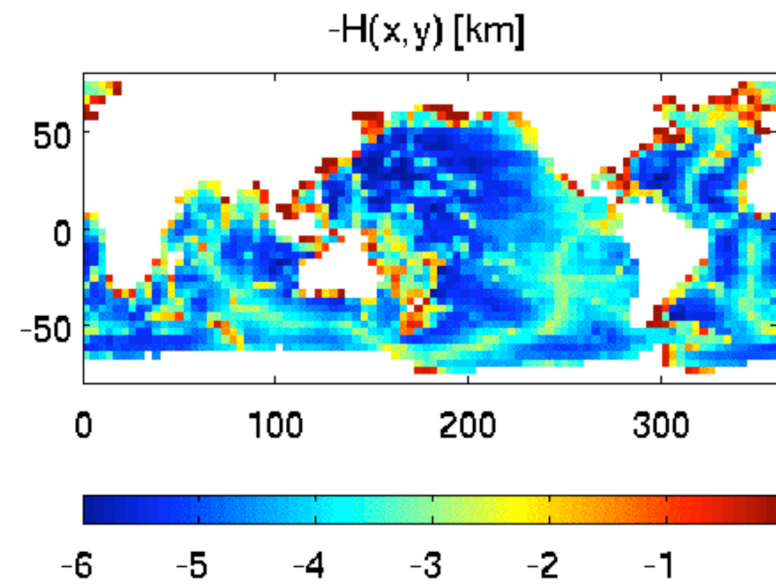
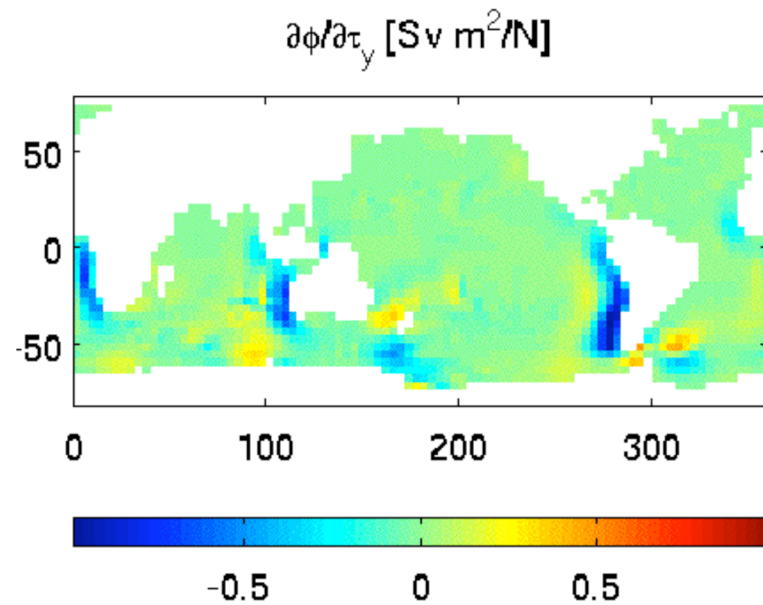
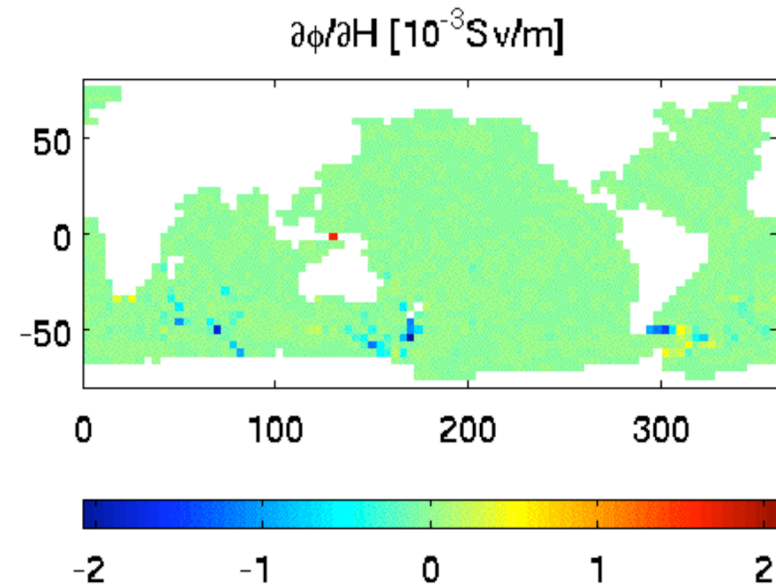
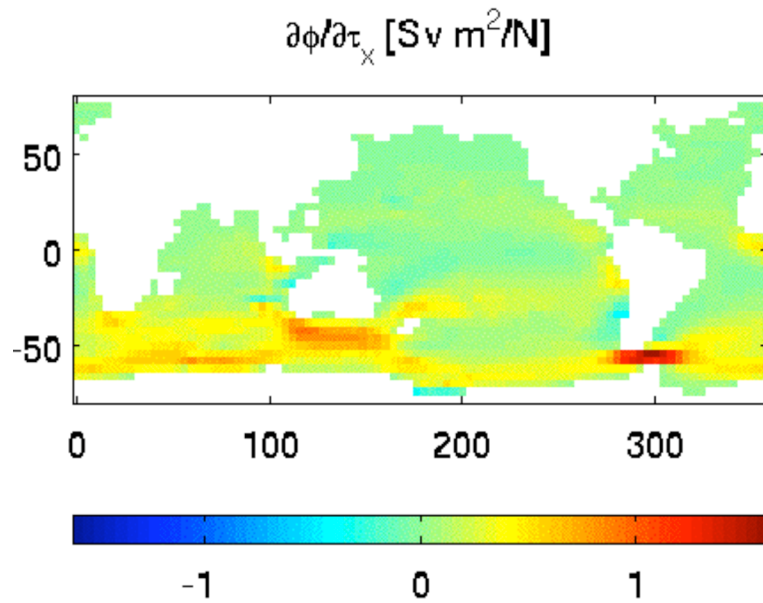


difference in SSH [cm]

B. (linear) adjoint sensitivity

- choose observable, objective function (OF)
- compute exact derivative of OF with respect to “control variables”, $d(\text{OF})/dx$ by means of the adjoint model.
- very elegant, needs only 1 forward and 1 backward integration
- Problem: requires gradient code of ocean model, always involves linearization
- Example: OF = transport through Drake Passage, control variables: wind stress (conventional), bottom topography (unconventional), (with P. Heimbach, MIT)

adjoint sensitivities



with P. Heimbach, MIT

C. Systematic comparison to observations:

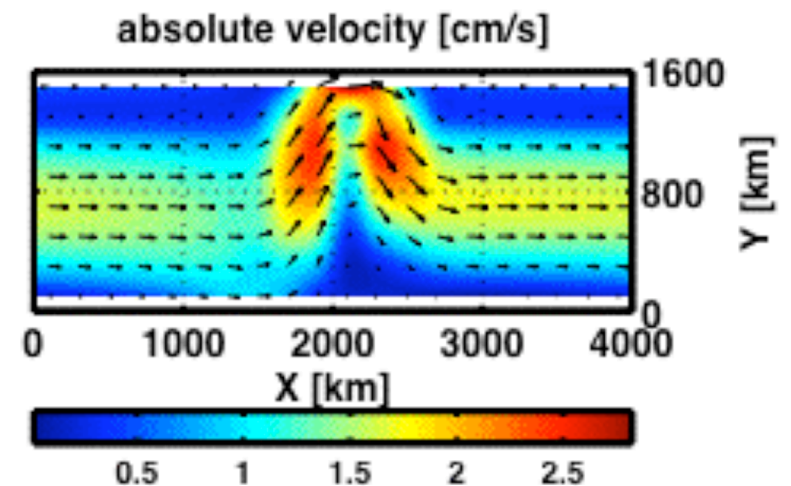
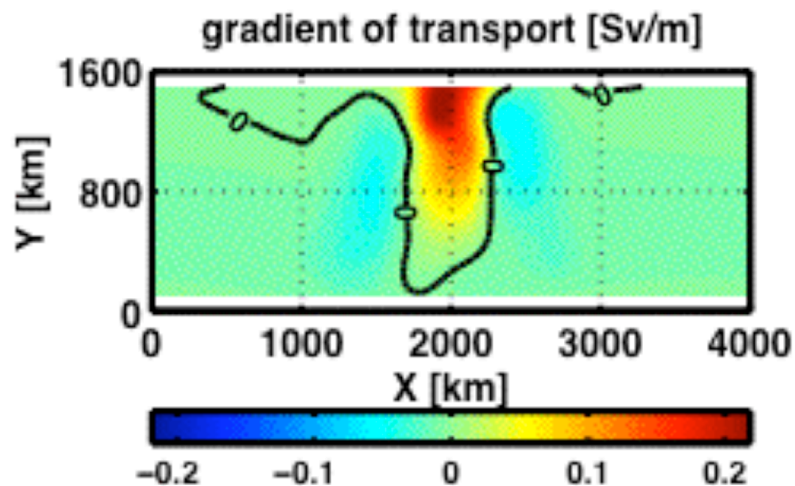
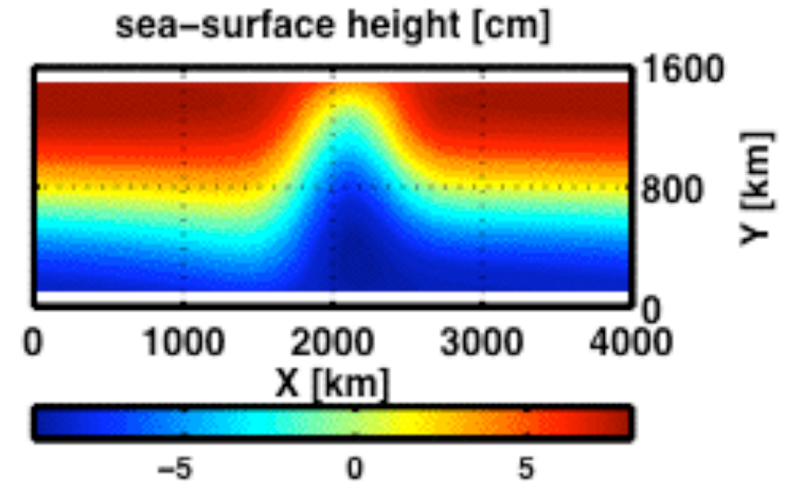
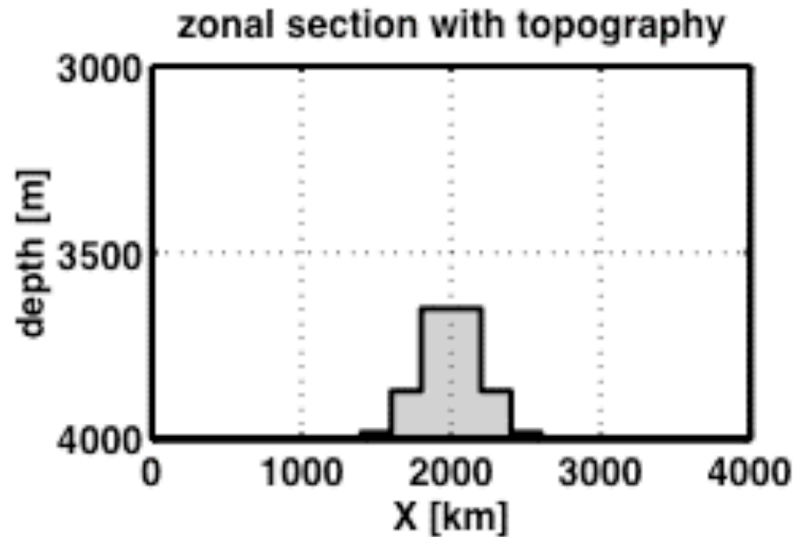
- Data assimilation, state estimation, with error analysis
- different techniques
- variational/adjoint methods use gradient information (previous slide)
- example: ECCO-consortium (Stammer, Fukumori, Wunsch, and many others)
- large computational effort

C. Systematic comparison to data: error analysis

- cost function $J = \frac{1}{2} (d - m(x))^T W (d - m(x))$
- error covariance $C_{xx} = H^{-1} = \left(\frac{\partial^2 J}{\partial x_i \partial x_j} \right)^{-1}$
- error analysis is almost always computationally prohibitive, but yields “best estimate” with error estimate
- example: Losch and Wunsch (2003) and FEMSECT

linear shallow water model

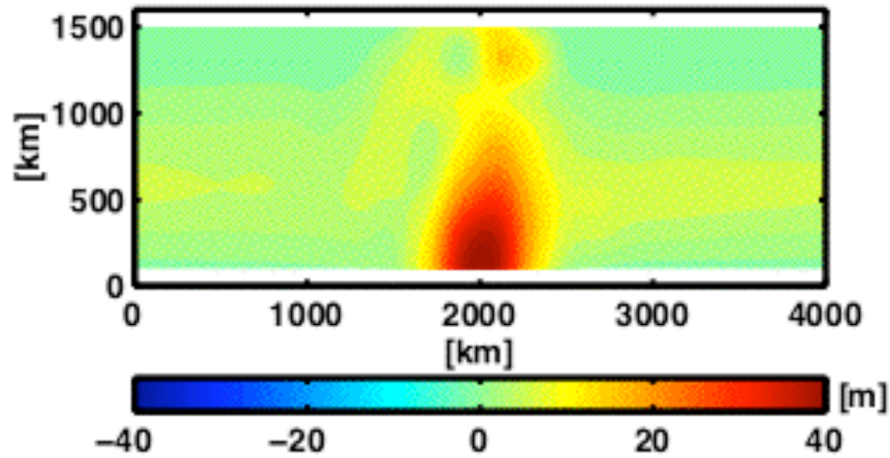
Losch and Wunsch (2003)



linear SWM: optimized solution

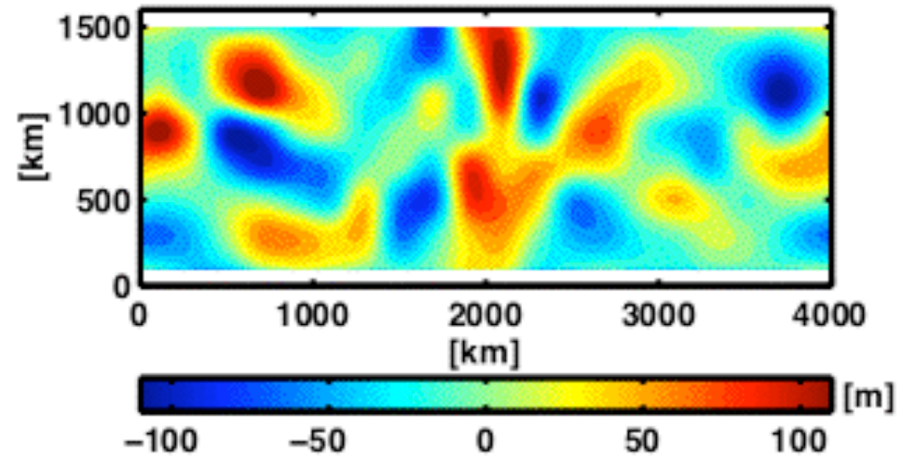
a) perfect sea-surface height data

residual = optimal - true depth

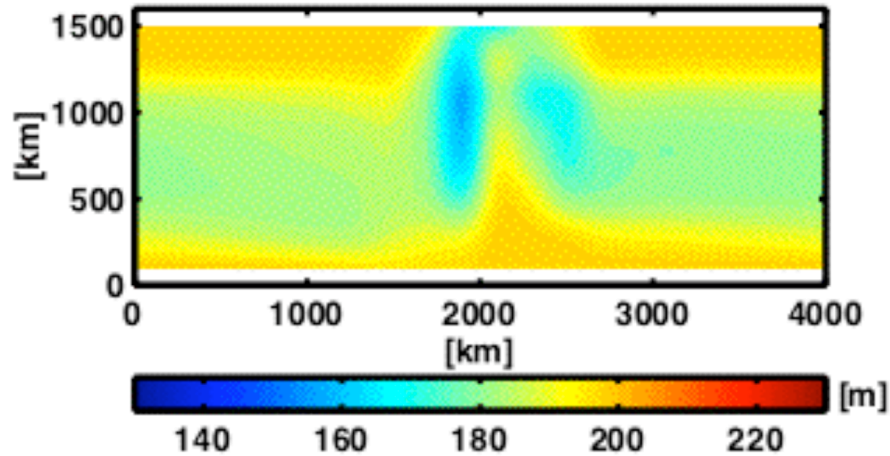


b) sea-surface height data with white noise

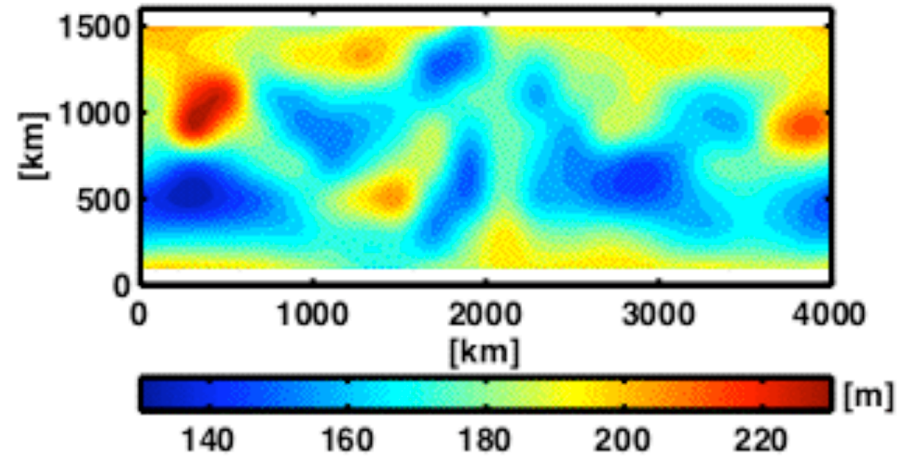
residual = optimal - true depth



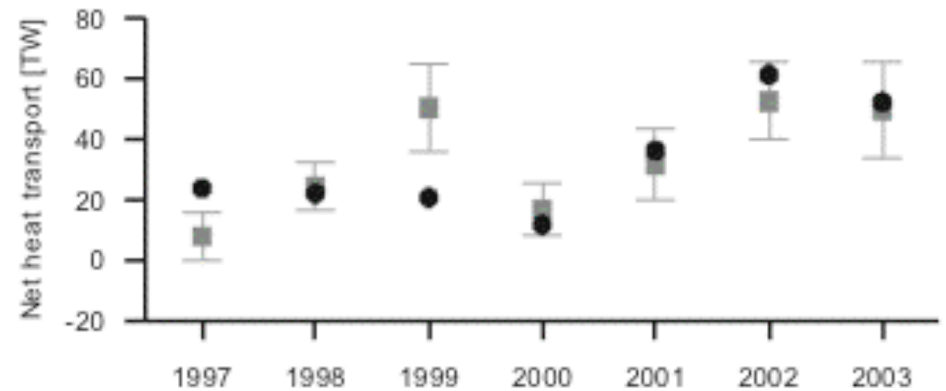
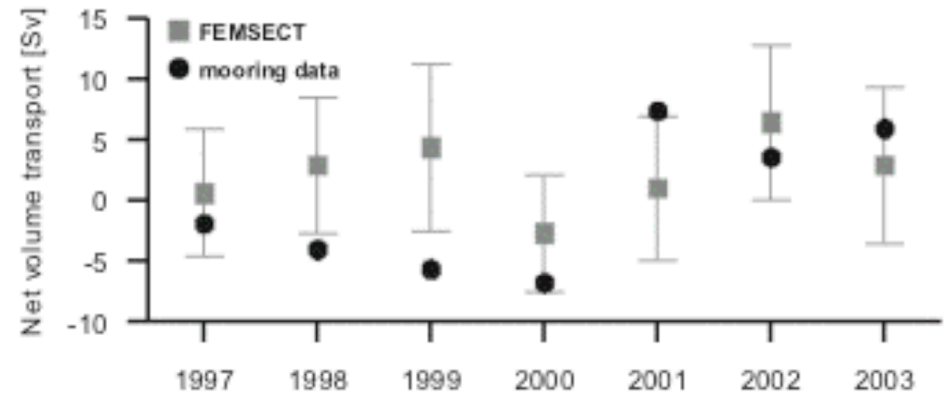
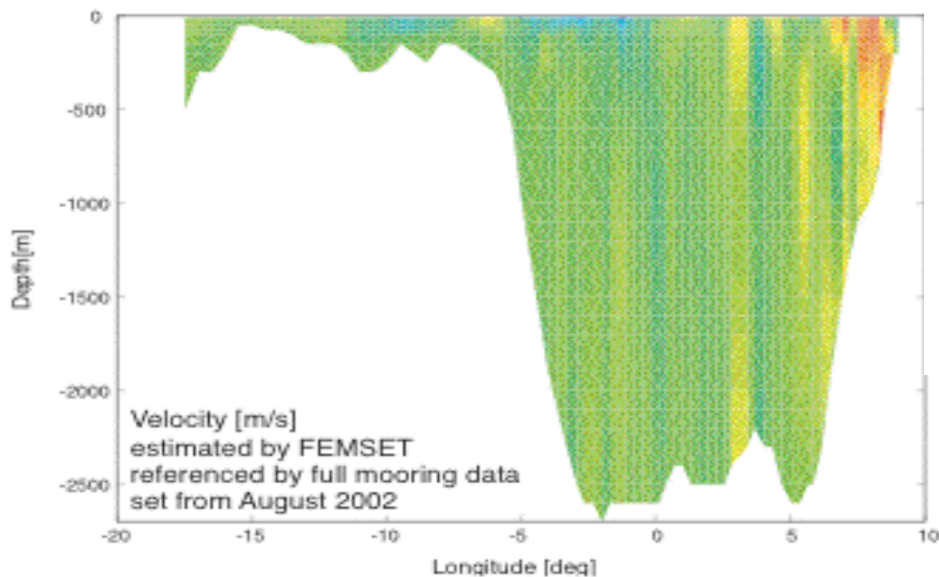
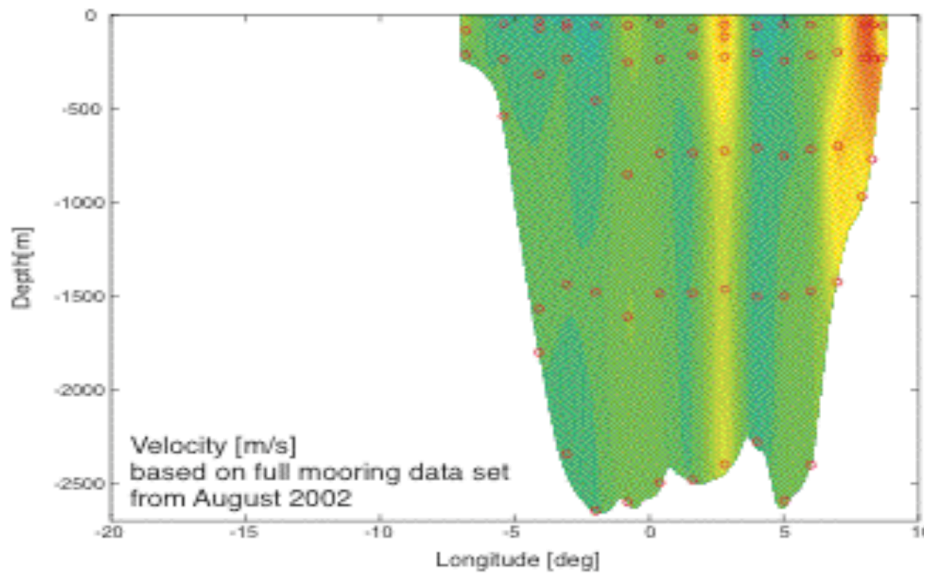
posterior error estimate



posterior error estimate



FEMSECT: finite element inverse section model. Application to Fram Strait



with D. Sidorenko, A. Beszczynska-Möller

Well, and how do you to estimate the accuracy of ocean circulation models?

a list with increasing complexity:

- “brute force” perturbation/ensemble methods, but very expensive
- adjoint sensitivity
- comparison to observations; data assimilation/state estimation with error estimates

to do

- explore unconventional control parameters in ocean models:
 - topography, diffusivity, lateral boundary conditions, ...
 - revise parameterization of the above
- state estimation with (coupled) ecosystem models (very nonlinear), to improve flux estimates of, e.g., CO₂