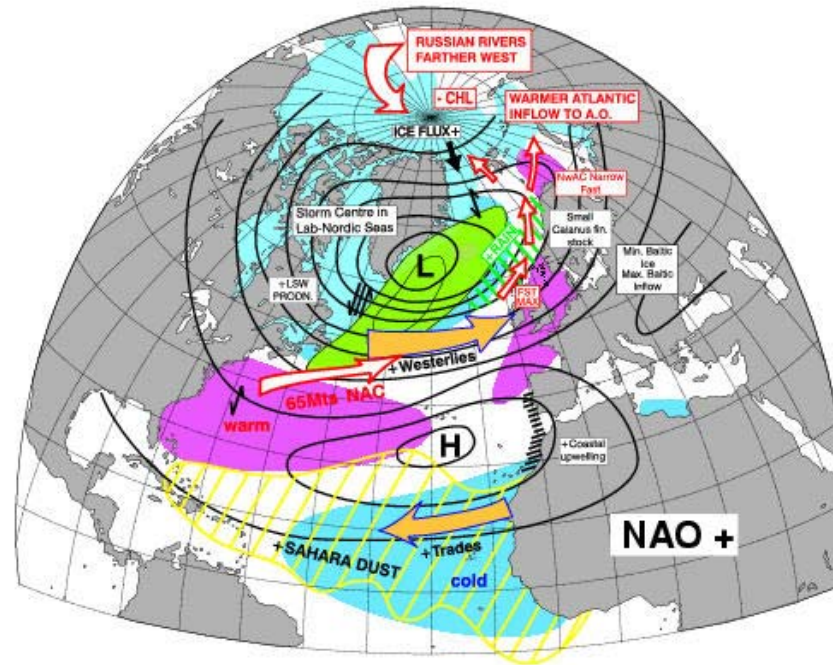


# Analysis of spatio-temporal pattern

## The Phases of the North Atlantic Oscillation



During the high phase of the NAO westerlies in the North Atlantic are enhanced, resulting in mild and wet winter conditions over Northern Europe. (Courtesy of CEFAS, UK)

# The North Atlantic oscillation (NAO)

is a climatic phenomenon in the North Atlantic Ocean of fluctuations in the difference of [sea-level pressure](#) between the [Icelandic Low](#) and the [Azores high](#).

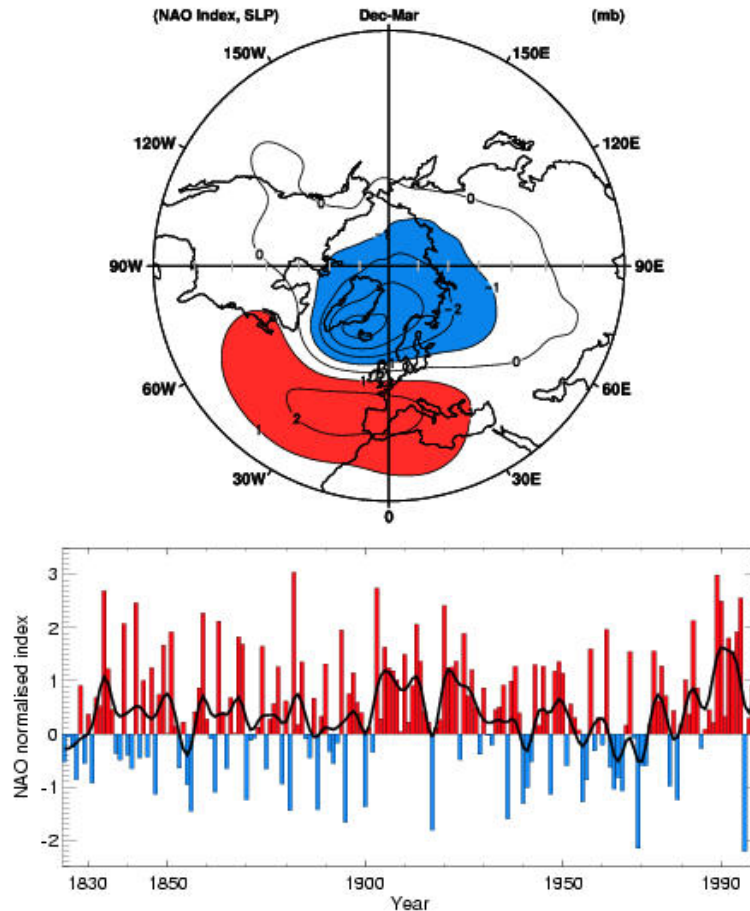
It controls the strength and direction of westerly [winds](#) across the North Atlantic

The NAO was discovered in the 1920s by Sir Gilbert Walker. The NAO is one of the most important drivers of climate fluctuations in the North Atlantic and surrounding continents.

# Analysis of spatio-temporal pattern

- NAO, ENSO
- Definitions
- Practical work

# The North Atlantic Oscillation



**Upper panel:** Observed Dec-March change in SLP associated with a 1 standard deviation change in the NAO index (after Hurrell, 1995, *Science*, 269, 676-679).

**Lower Panel:** Winter (December to March) index or the NAO based on the difference of normalized pressure between Lisbon, Portugal and Stykkisholmur, Iceland from 1864 to 1995. The SLP anomalies at each station were normalized by division of each seasonal pressure by the long-term mean (1864-1995) standard deviation. The heavy solid line represents the meridional pressure gradient smoothed with a low pass filter with seven weights (1,3,5,6,5,3, and 1) to remove fluctuations with periods less than 4 years (after Hurrell, 1995, *Science*, 269, 676-679, this version: courtesy of T. Osborn, CRU, UEA).

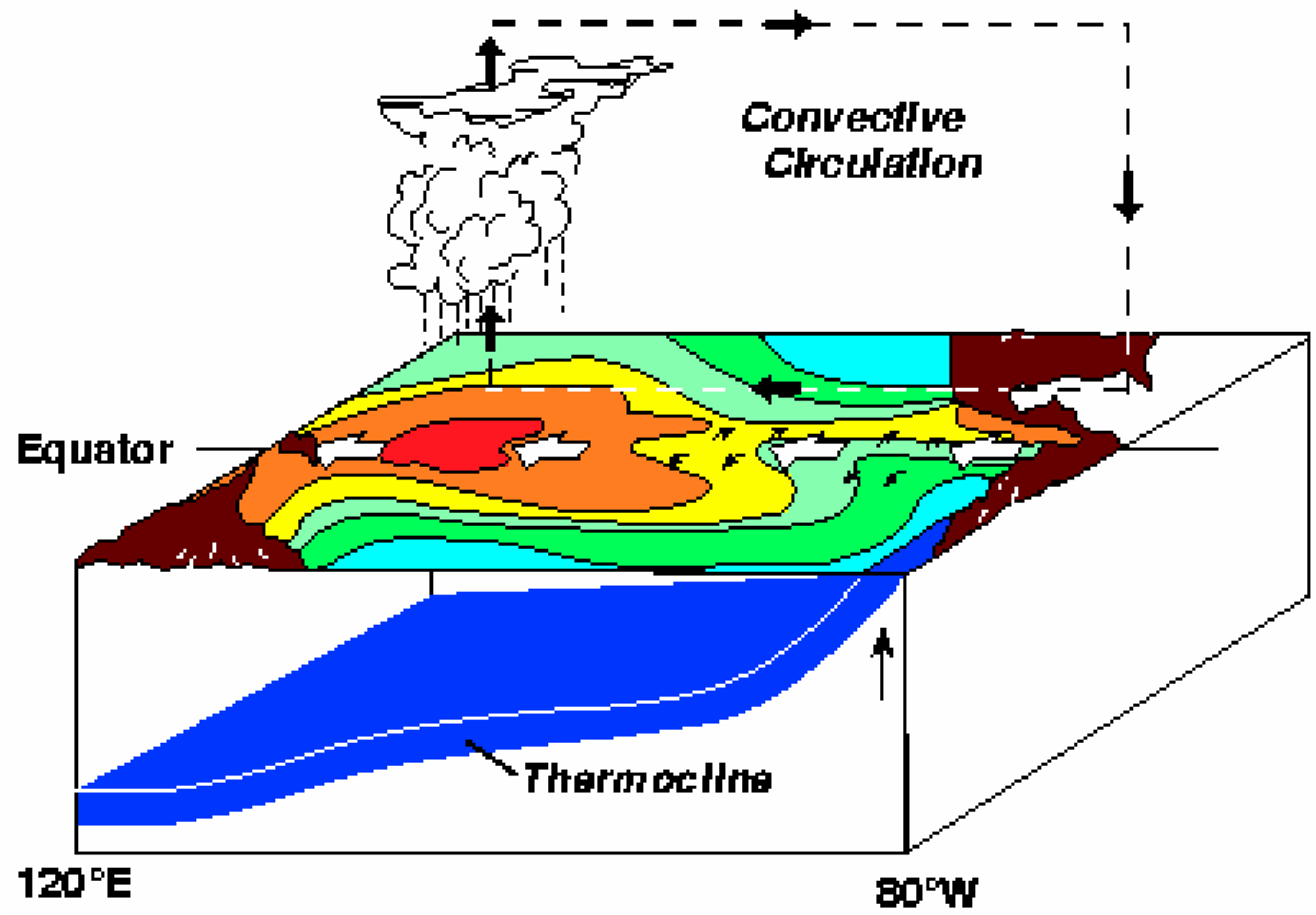
# El Niño-Southern Oscillation (ENSO)

**El Niño** and **La Niña** are important temperature fluctuations in surface waters of the tropical Eastern Pacific Ocean.

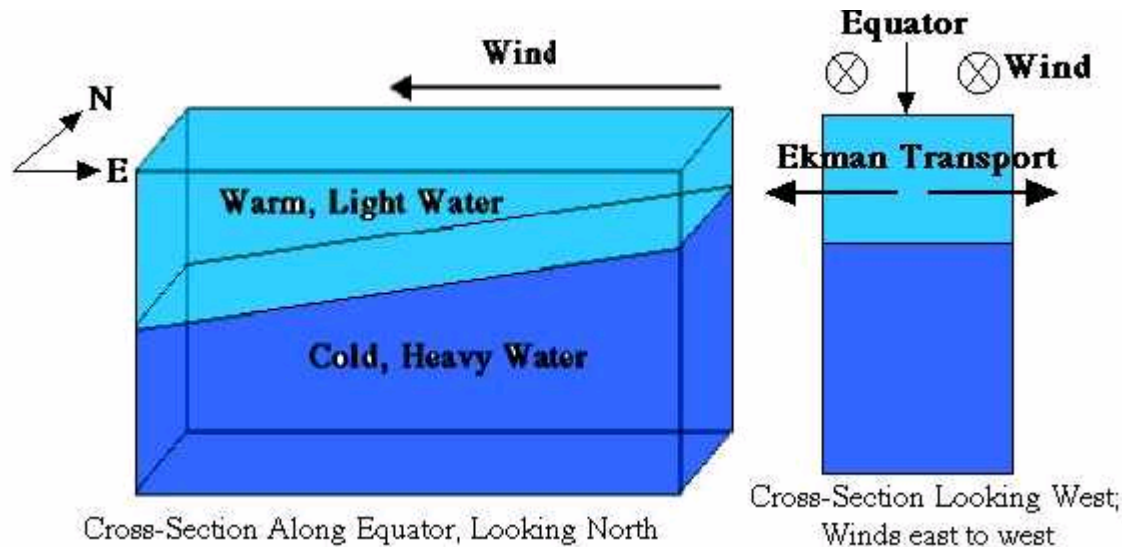
The name El Niño, from the [Spanish](#) for "the child", refers to the Christ child, because the phenomenon is usually noticed around Christmas time in the Pacific Ocean off the west coast of South America. La Niña means "the little girl".

These effects were first described in 1923 by [Sir Gilbert Thomas Walker](#) from whom the [Walker circulation](#), an important aspect of the Pacific ENSO phenomenon, takes its name. The atmospheric signature, the **Southern Oscillation (SO)** reflects the monthly or seasonal fluctuations in the air pressure difference between [Tahiti](#) and [Darwin](#).

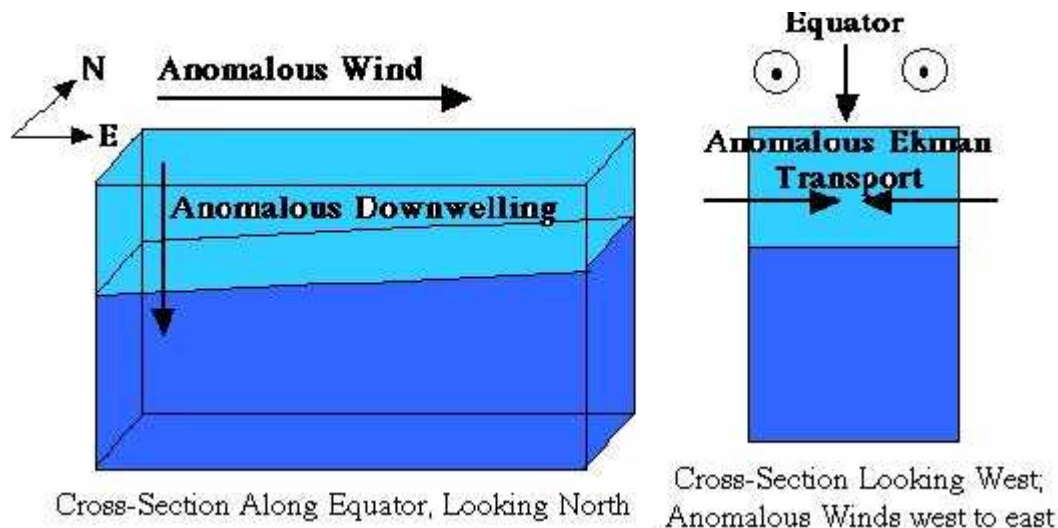
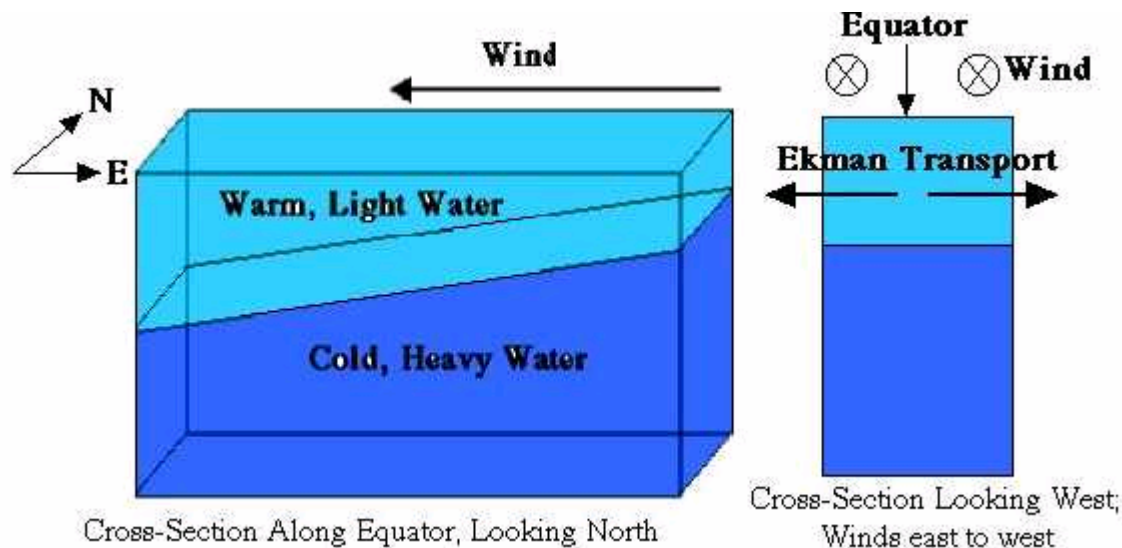
# Normal Conditions



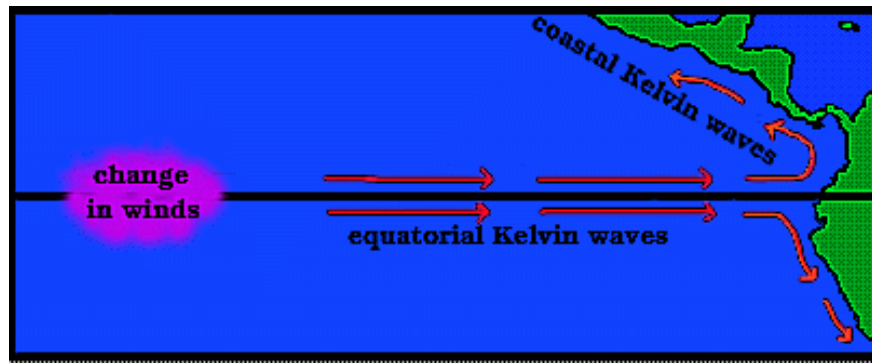
# Change in the Ekman transport



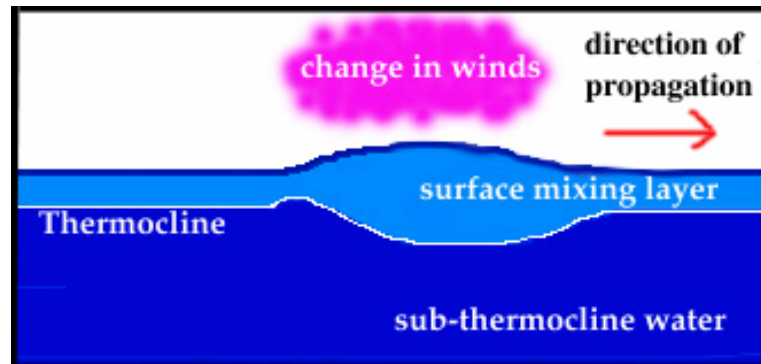
# Change in the Ekman transport







There are two types of Kelvin waves, coastal and equatorial, and they are both gravity driven and non-dispersive. They are often excited by an abrupt change in the overlying wind field, such as the shift in the trade winds at the start of El Niño.



The surface waves are very fast moving, typically with speeds of  $\sim 2.8$  m/s, or about 250 kilometers in a day. A Kelvin wave would take about 2 months to cross the Pacific from New Guinea to Peru.

# Kelvin wave

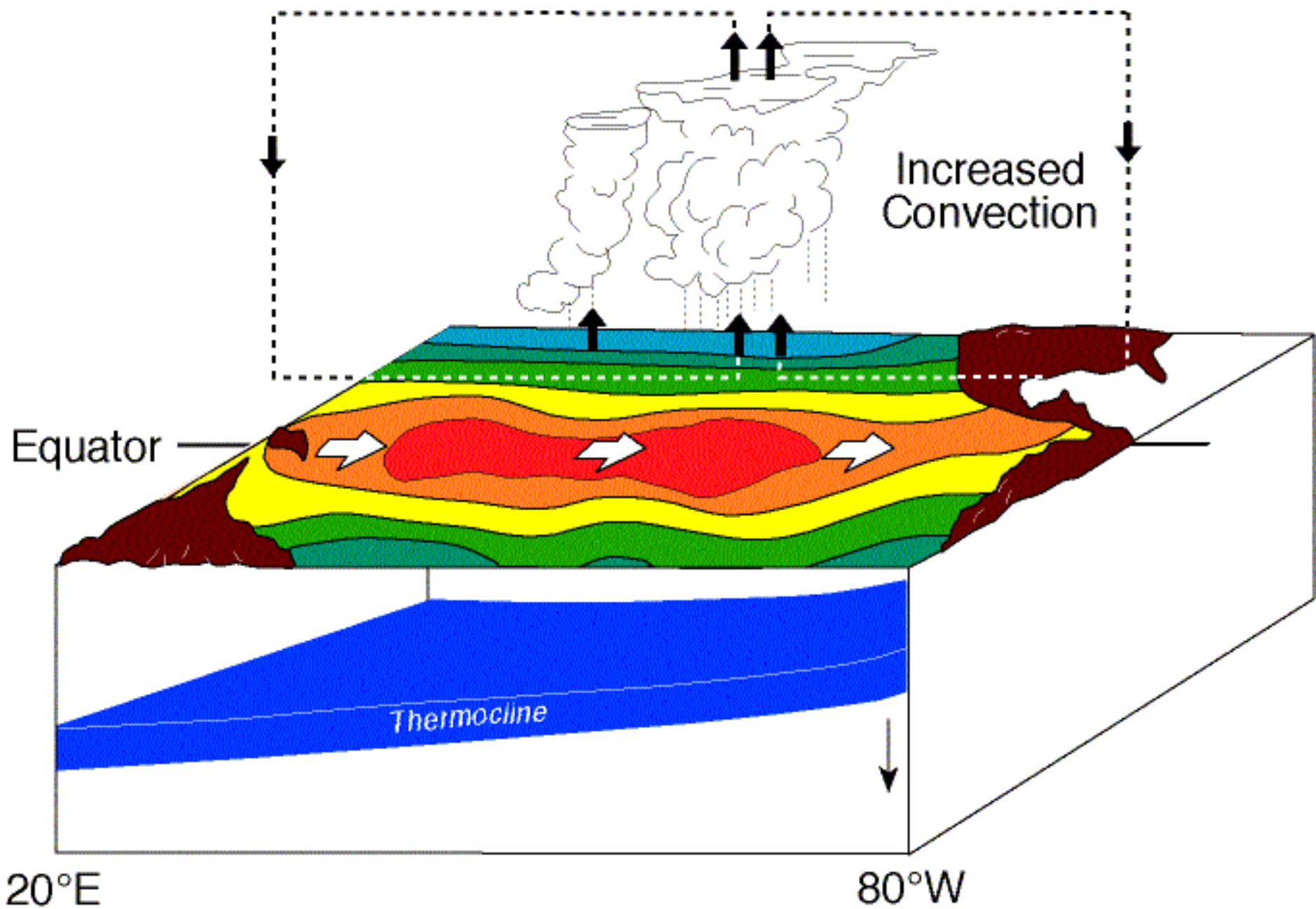
A type of low-frequency gravity wave trapped to a vertical boundary, or the equator, which propagates anticlockwise (in the Northern Hemisphere) around a basin. The flow is parallel to the boundary and in geostrophic balance with the pressure gradient perpendicular to the boundary.

The velocity normal to the boundary is identically zero.

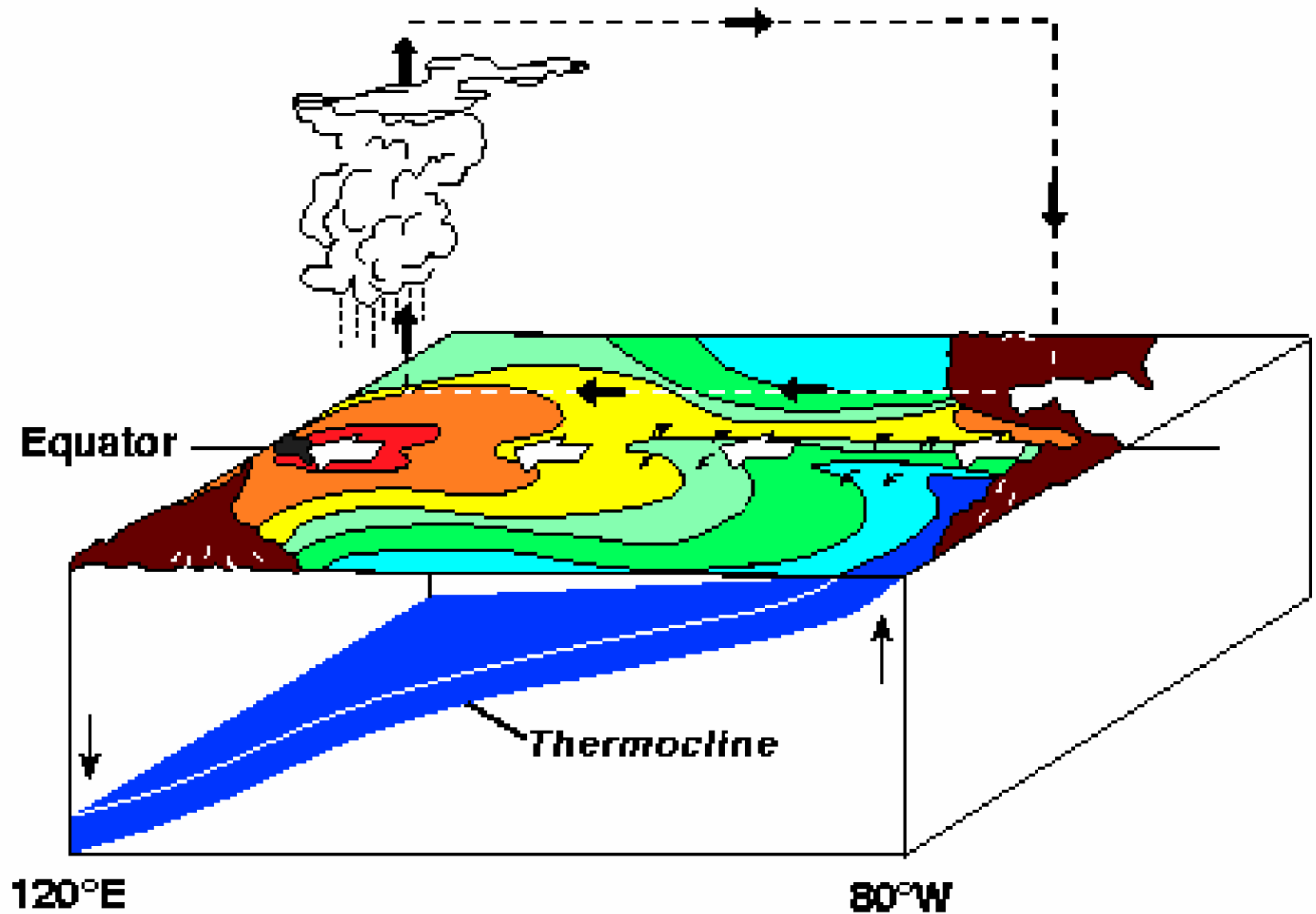
The wave height decreases exponentially from the side wall with an e-folding length scale equal to the Rossby radius of deformation

In the shallow water approximation the waves are nondispersive with frequency  $\omega = c k$ , in which  $k$  is the along-boundary wavenumber  $c = (gH)^{1/2}$ ,

# El Niño Conditions



# La Niña Conditions



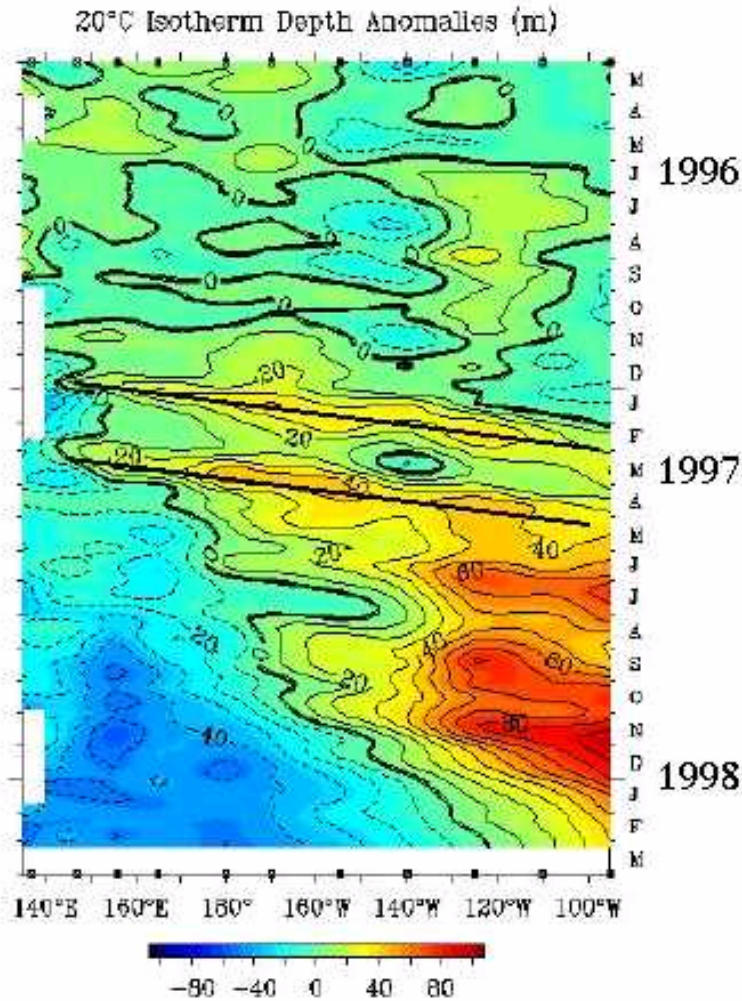
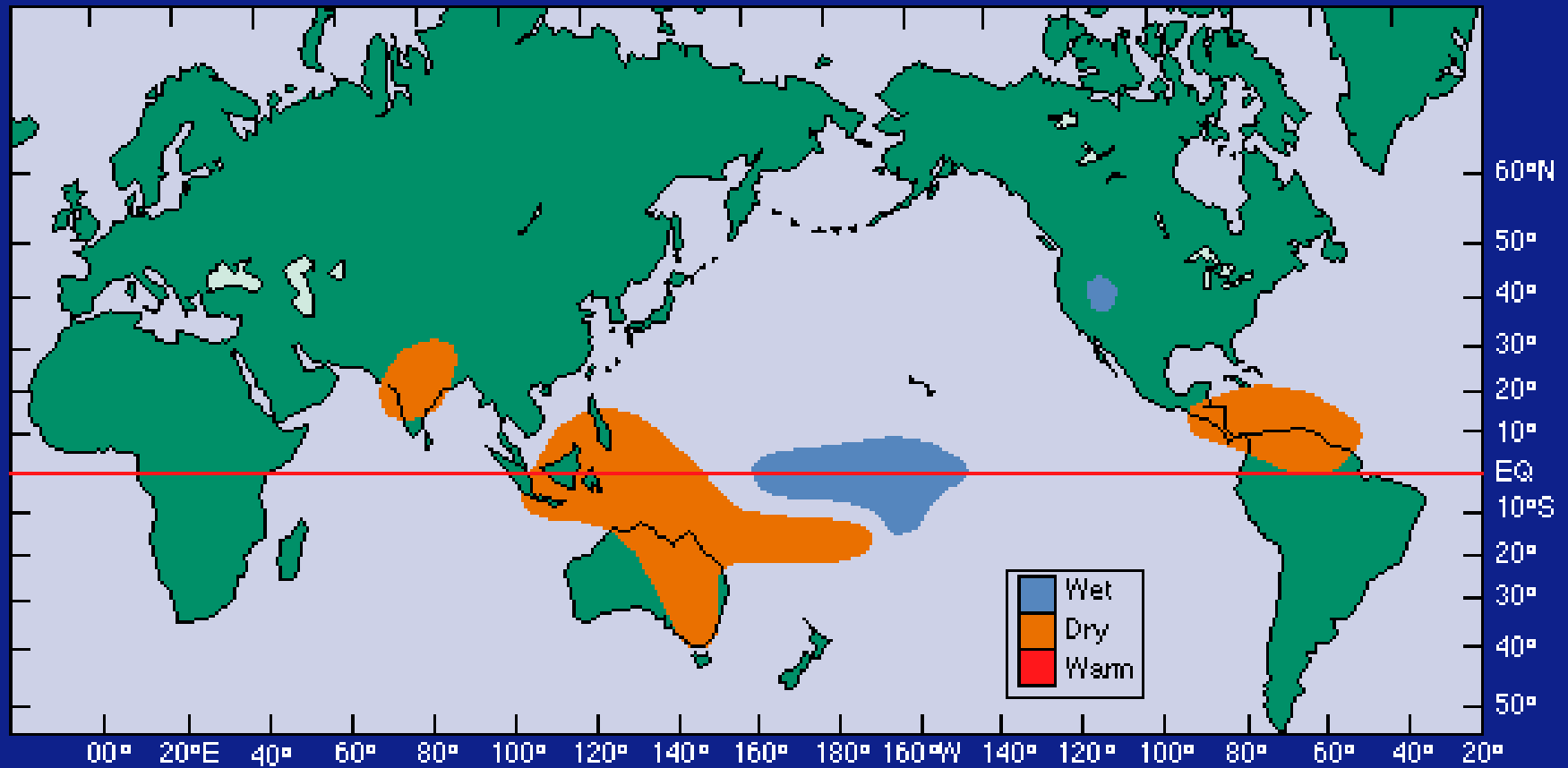


Figure courtesy of NOAA PMEL

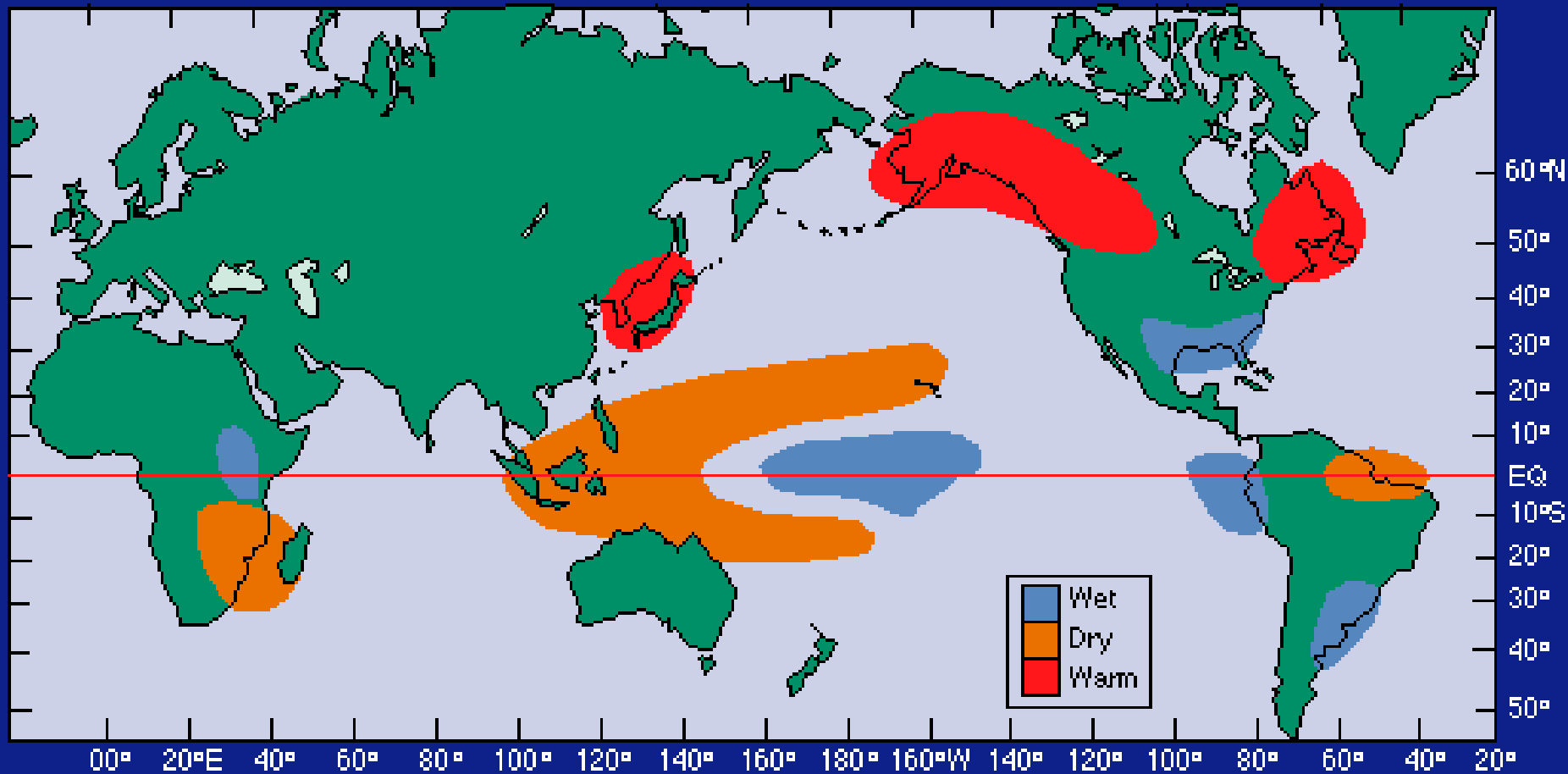
Kelvin waves can cross the Pacific in two months. The amplitude of the Kelvin wave is several tens of meters along the thermocline, and the length of the wave is thousands of kilometers (1 degree of longitude = 111 km)

Eastward movement is indicated by the slope in time from west to east. These waves set up a change in the warm water thickness of the Eastern Pacific beginning in March.

# Northern Hemisphere Summer



# Northern Hemisphere Winter



**Flooding**

Bolivia \$300,000,000  
Ecuador, Northern  
Peru \$650,000,000  
Cuba \$170,000,000  
U.S. Gulf  
States \$1,270,000,000

**Hurricanes**

Tahiti \$50,000,000  
Hawaii \$230,000,000

**Drought/Fires**

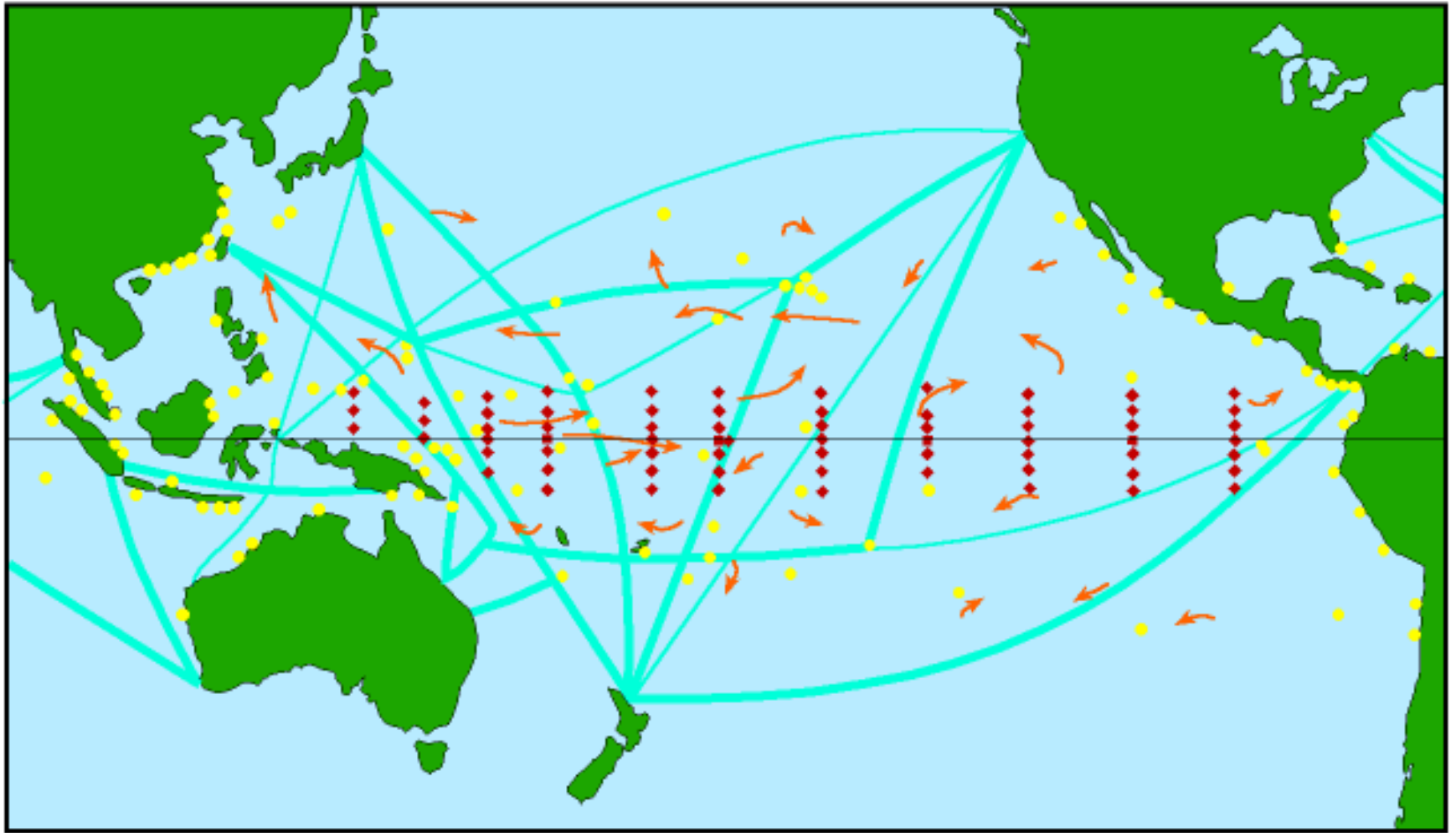
Southern  
Africa \$1,000,000,000  
Southern India,  
Sri Lanka \$160,000,000  
Philippines \$450,000,000  
Indonesia \$500,000,000  
Australia \$2,500,000,000  
Southern Peru, Western  
Bolivia \$240,000,000  
Mexico, Central  
America \$600,000,000

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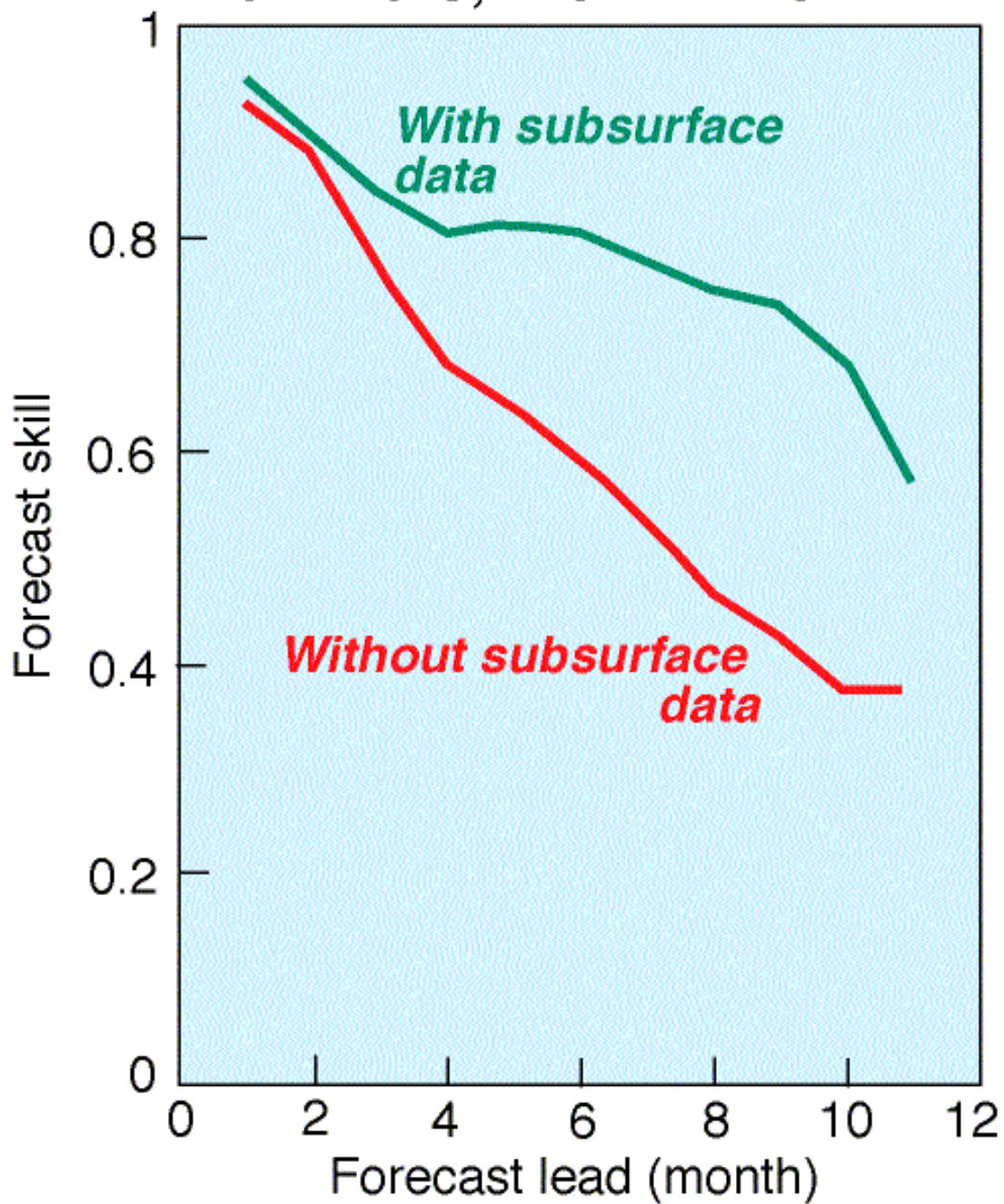
**Total \$8,110,000,000**

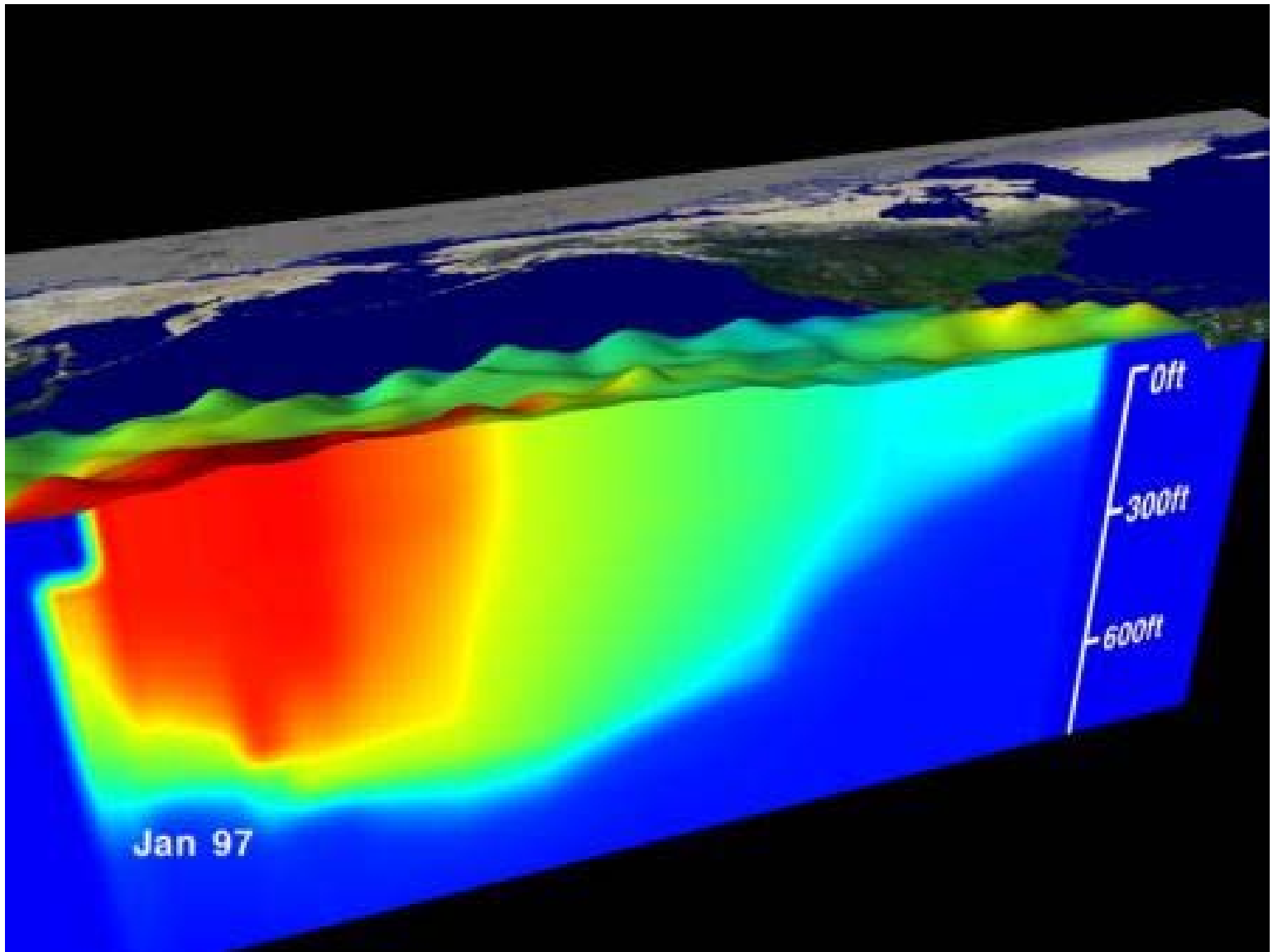


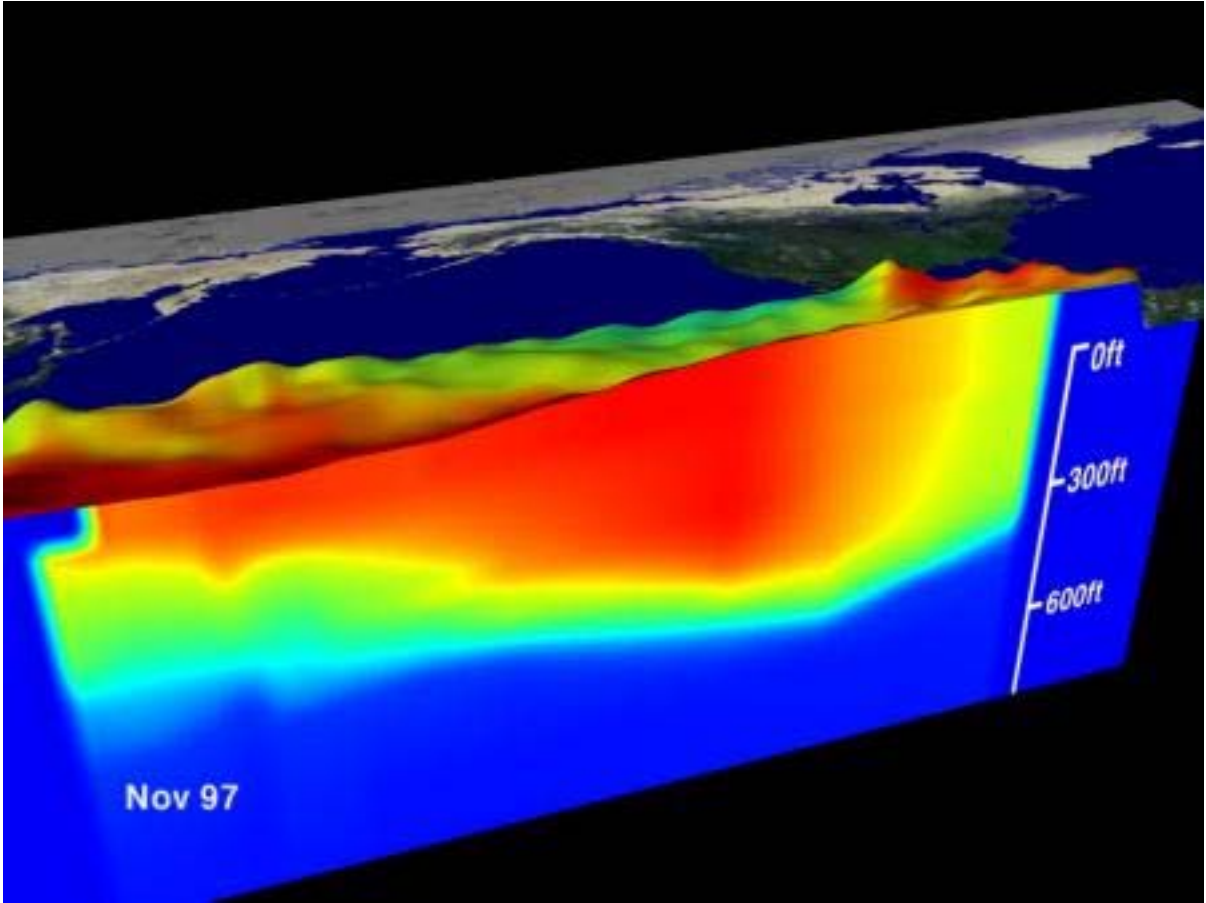
# ENSO Observing System

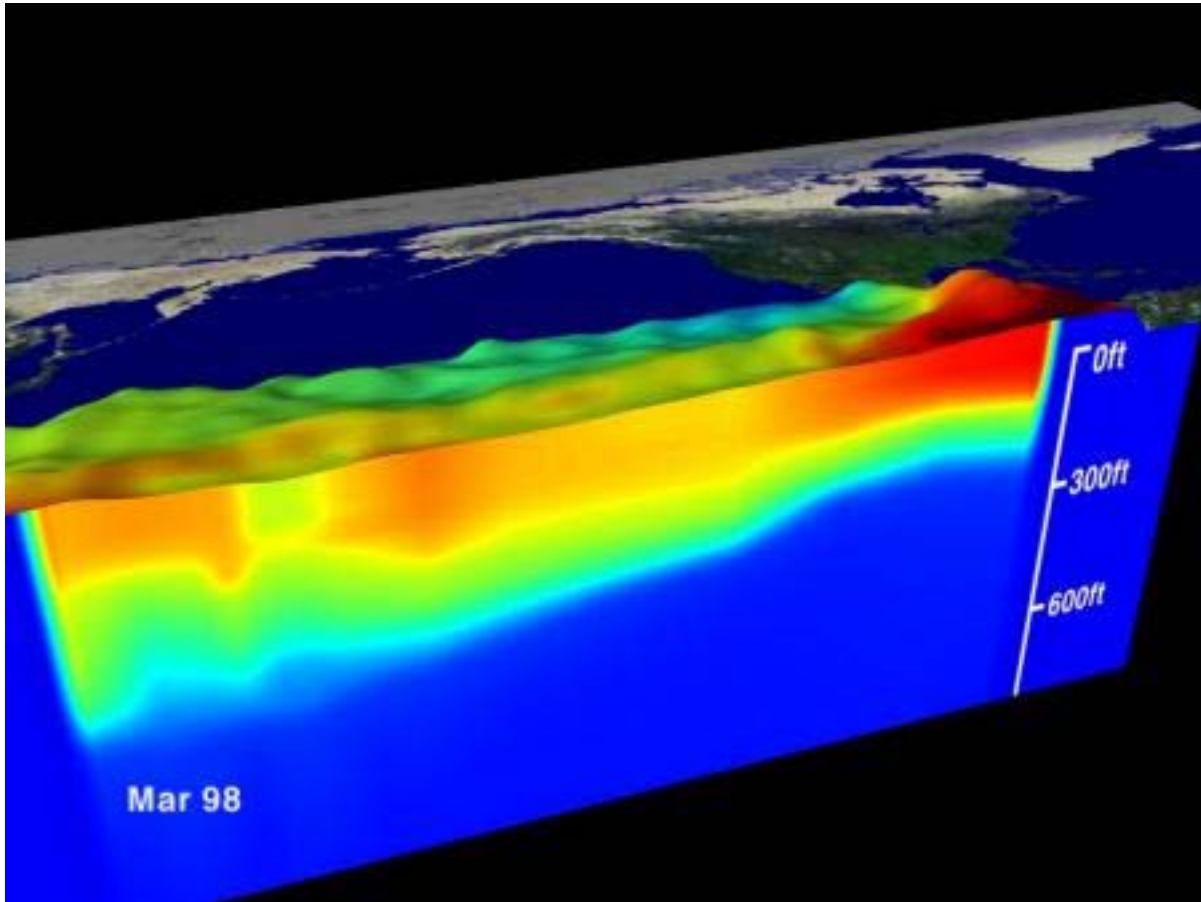


# Sea Surface Temperature 5°N - 5°S, 120°W - 170°W



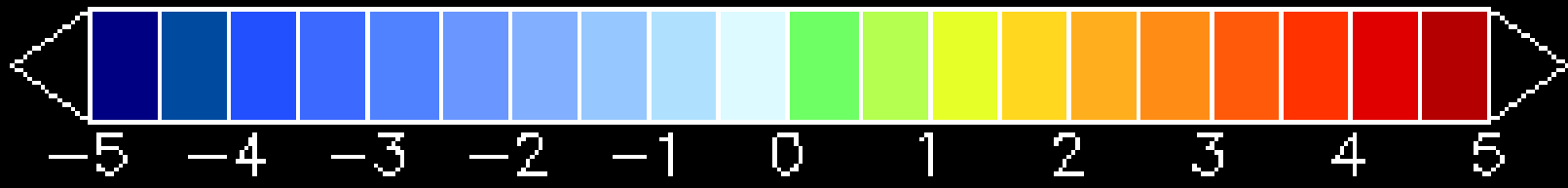
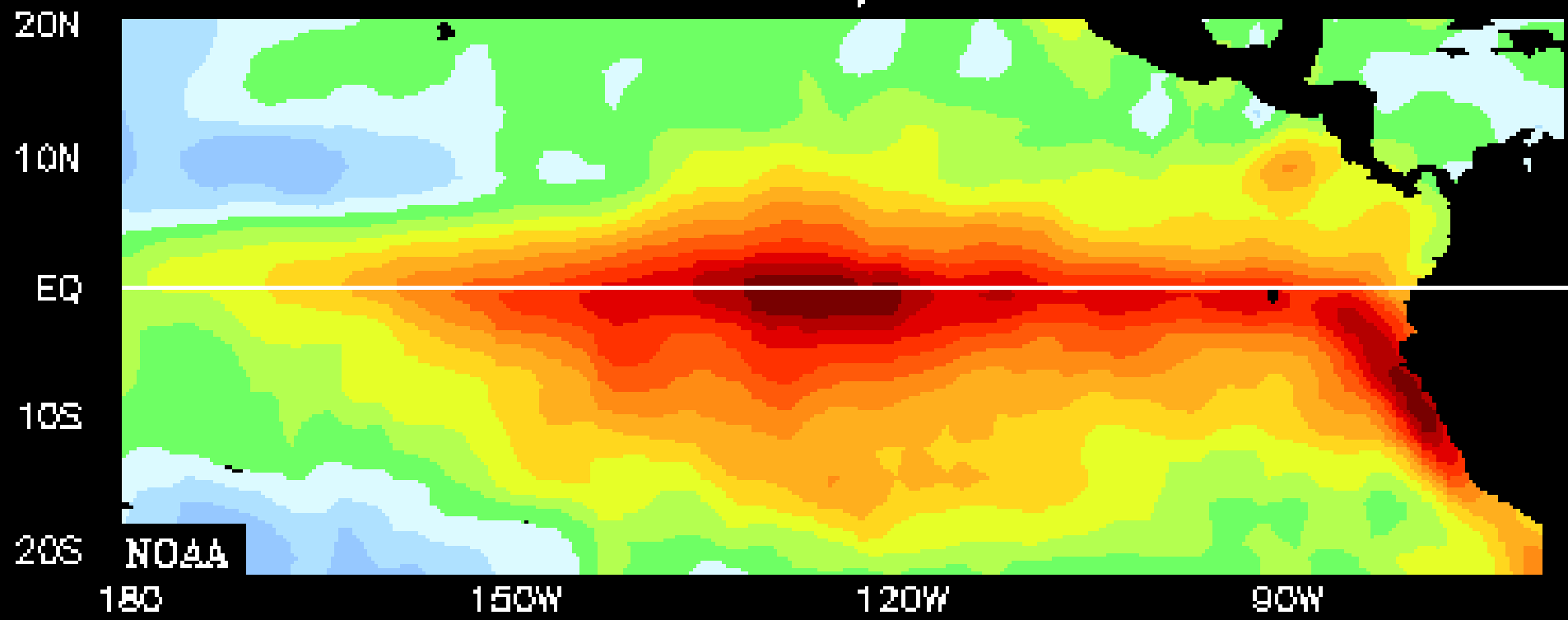






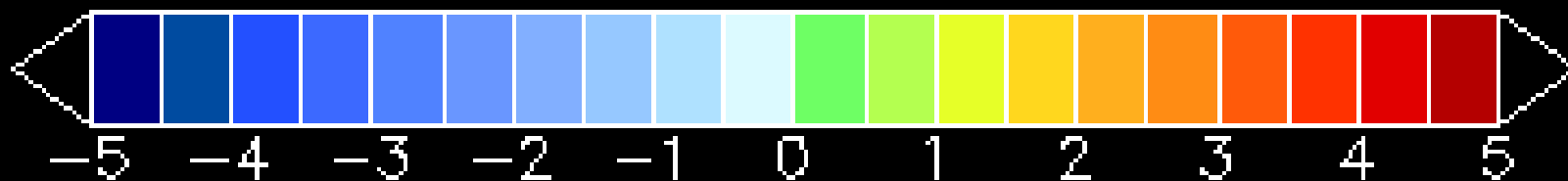
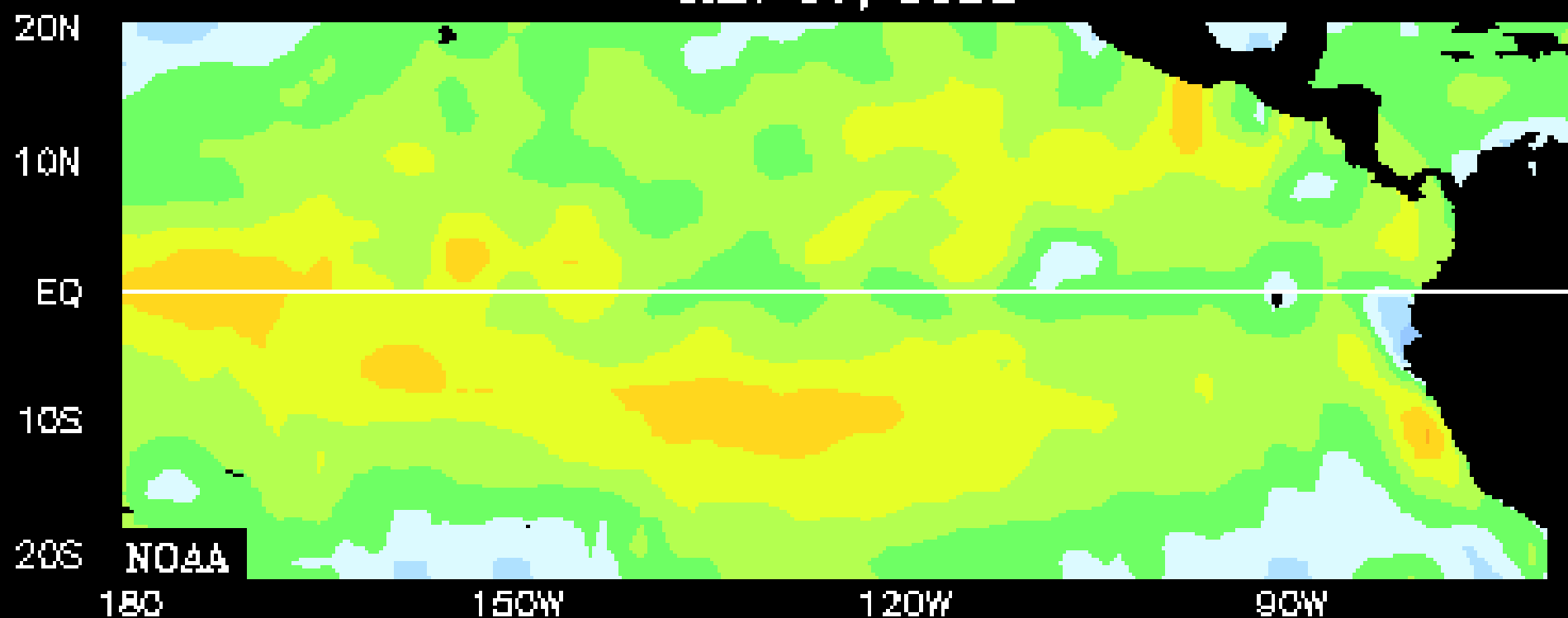
# SST ANOMALIES °C

JAN 08, 1983



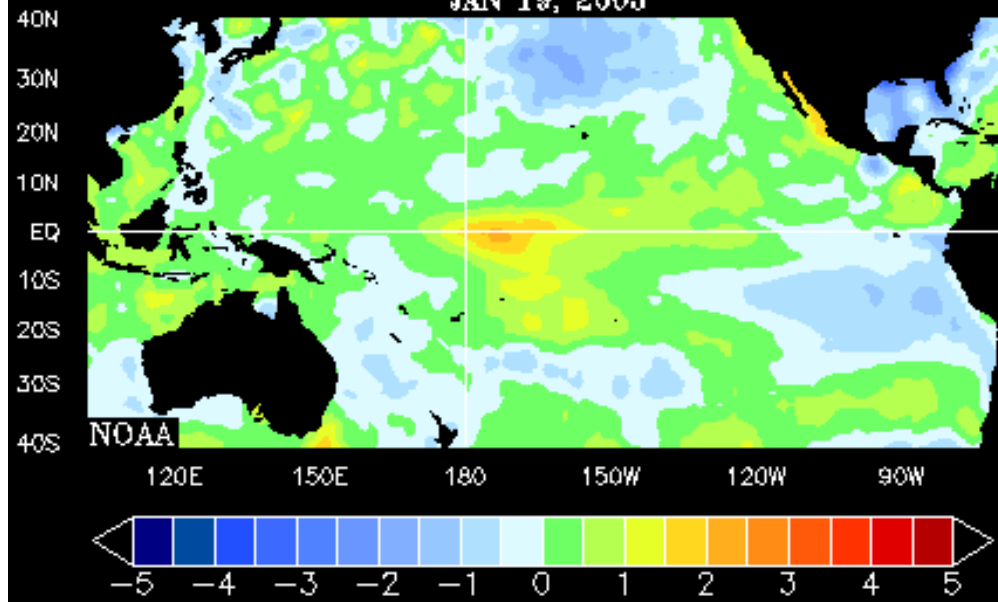
# SST ANOMALIES °C

JAN 07, 1988



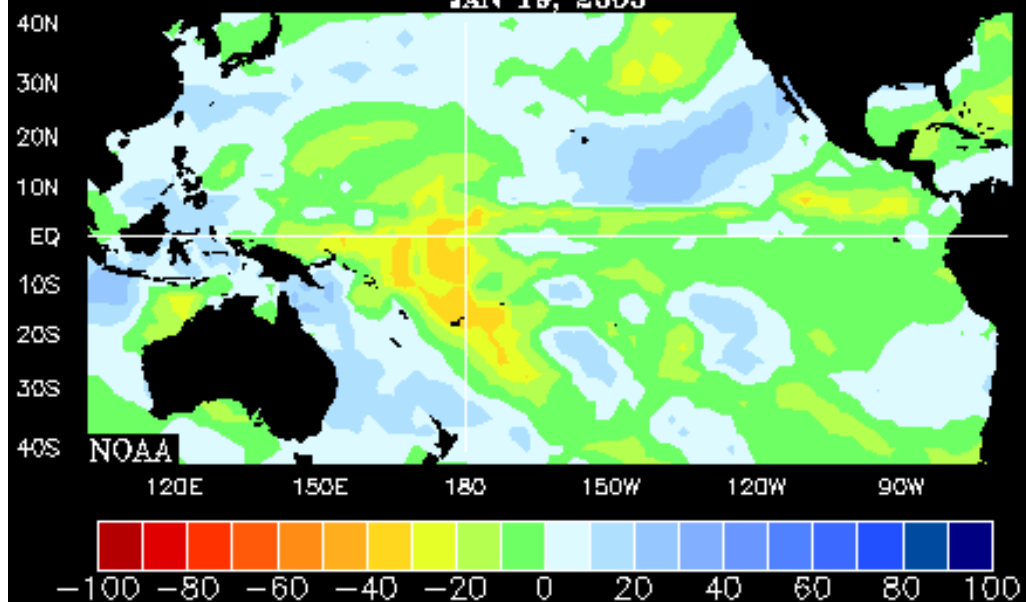
### SST ANOMALIES °C

JAN 19, 2003



### RAINFALL ANOMALIES (OLR $Wm^{-2}$ )

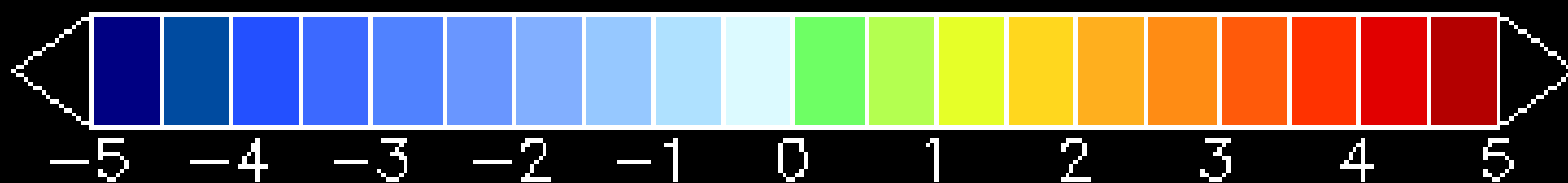
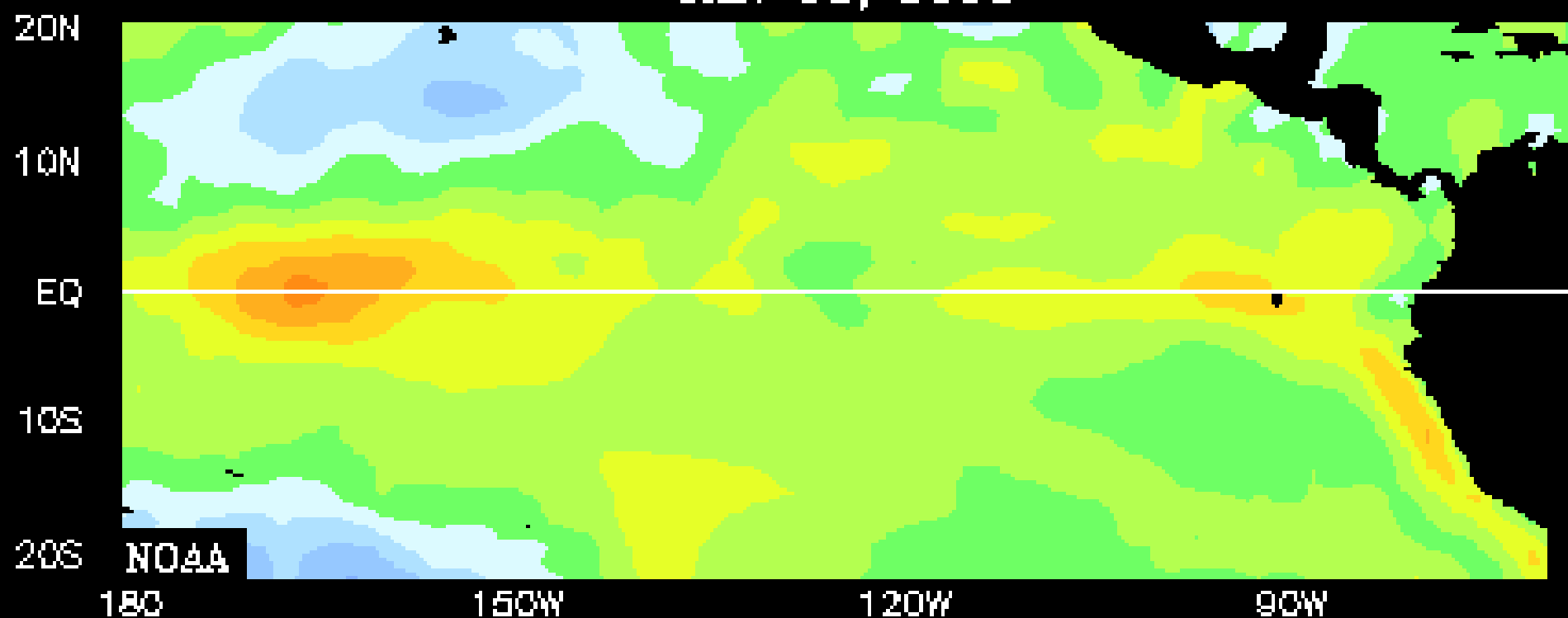
JAN 19, 2003





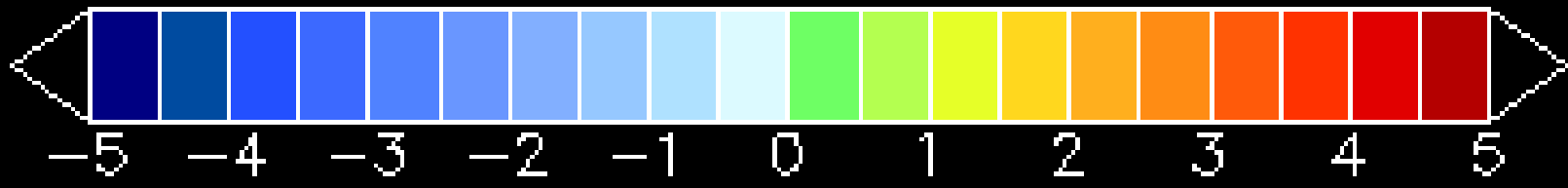
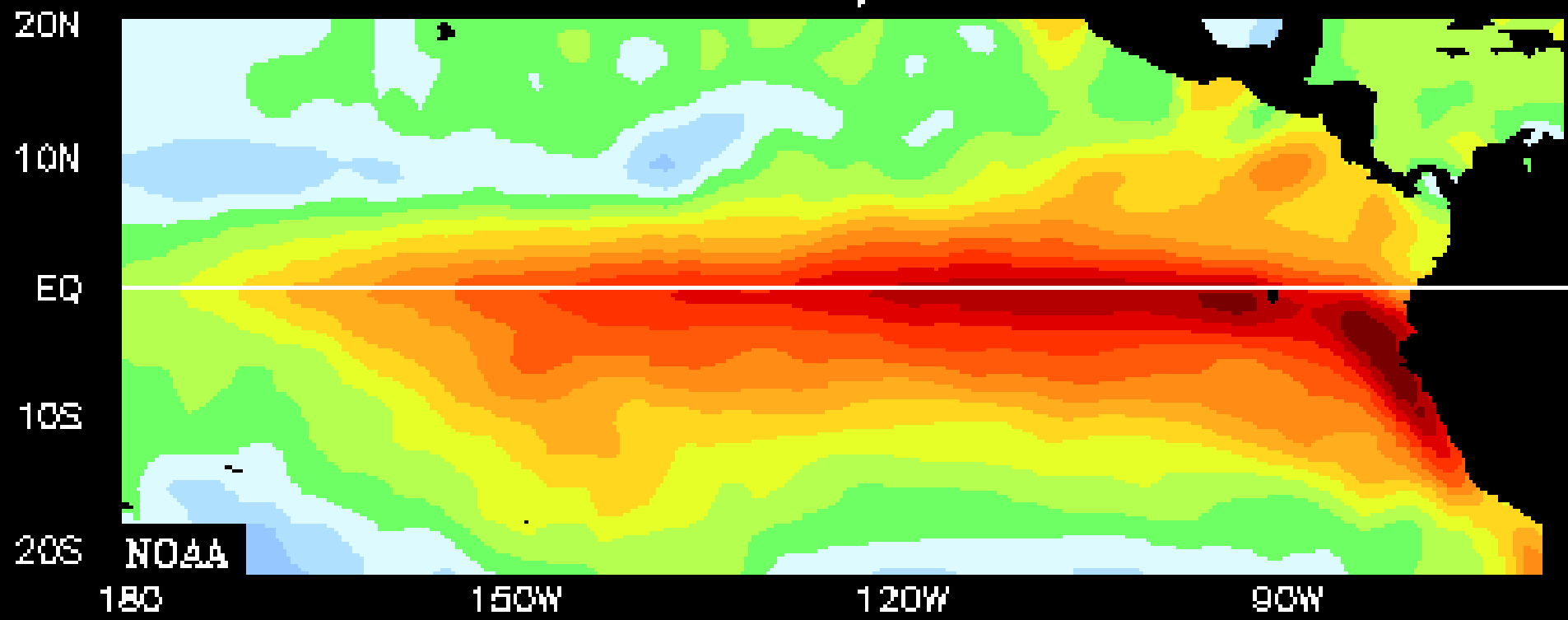
# SST ANOMALIES °C

JAN 01, 1995



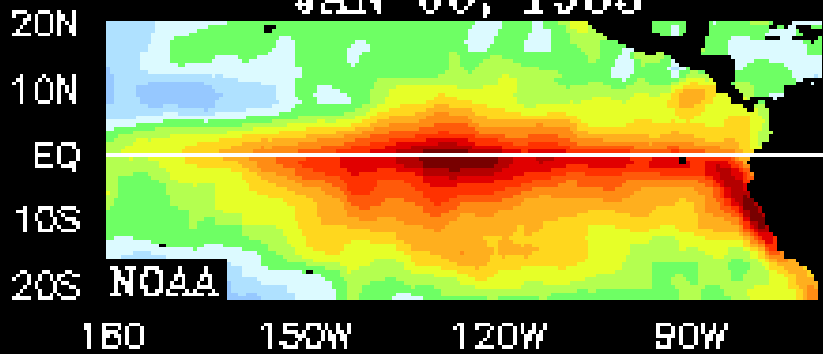
# SST ANOMALIES °C

JAN 04, 1998

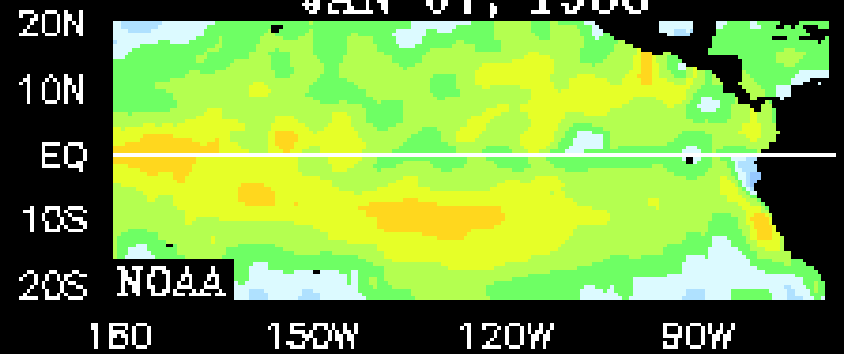


# SST ANOMALIES °C

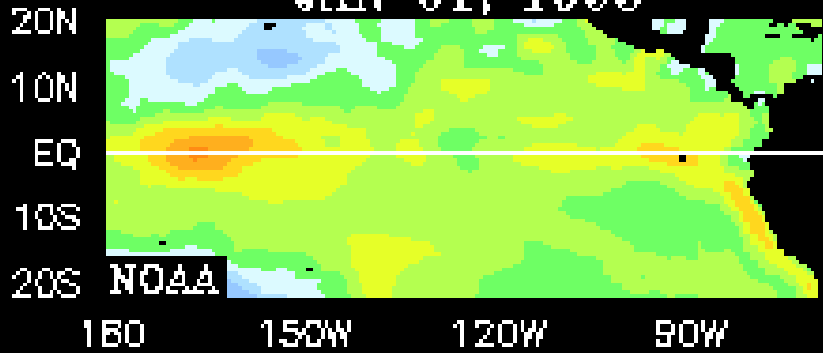
JAN 06, 1983



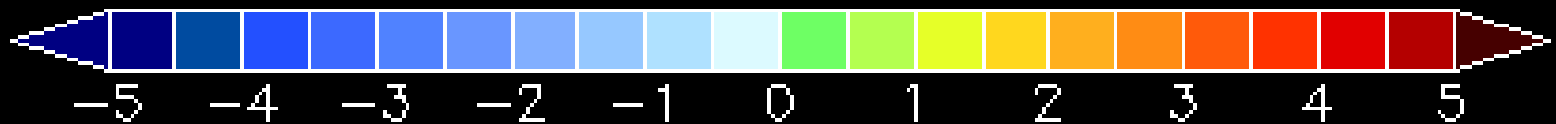
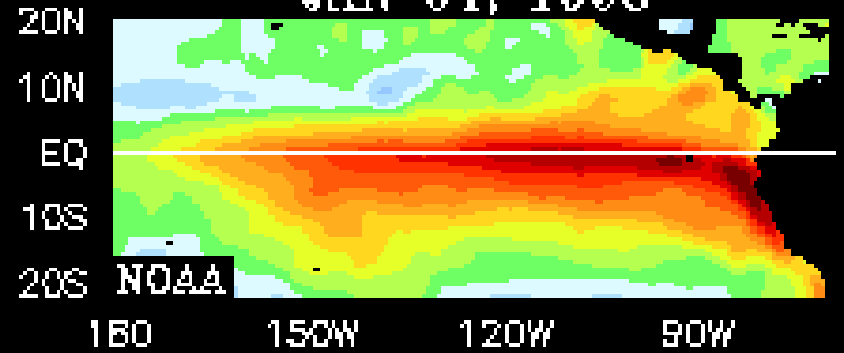
JAN 07, 1988



JAN 01, 1995

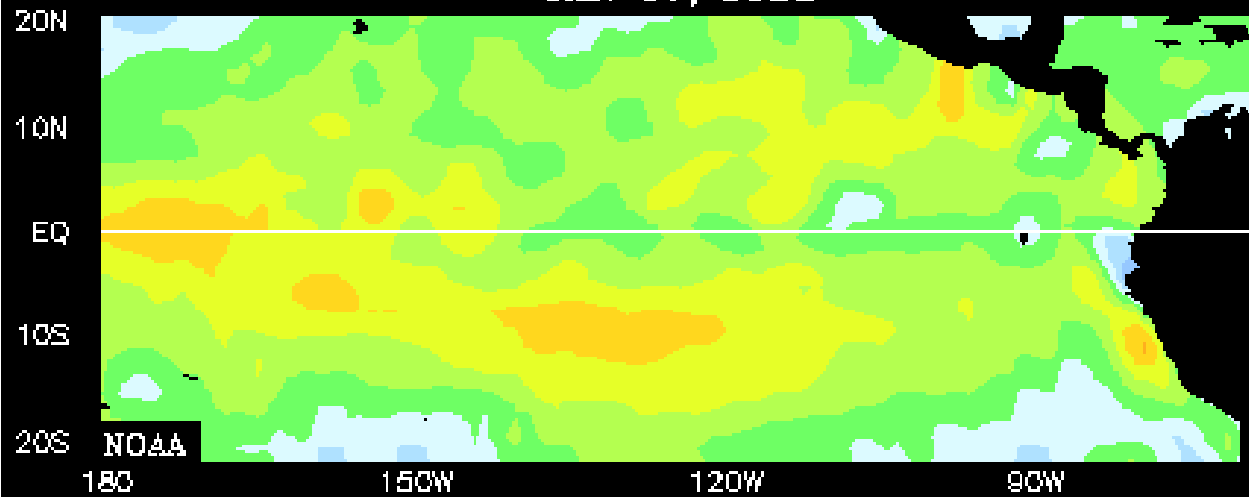


JAN 04, 1998

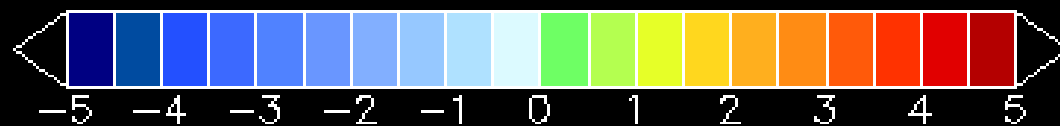
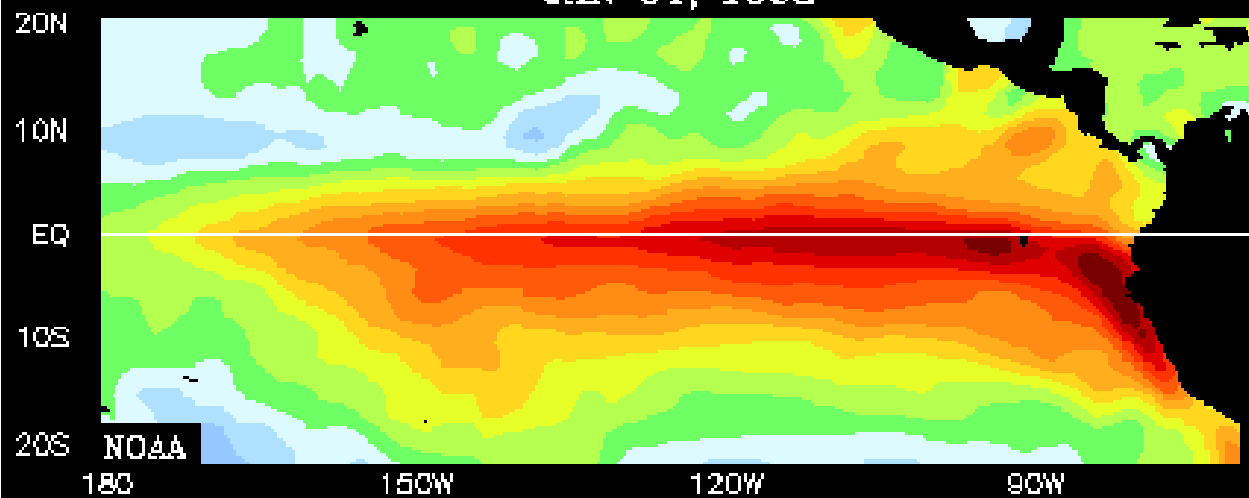


# SST ANOMALIES °C

JAN 07, 1998

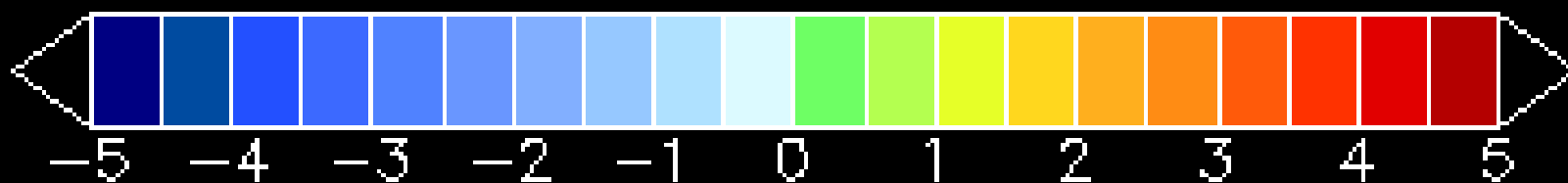
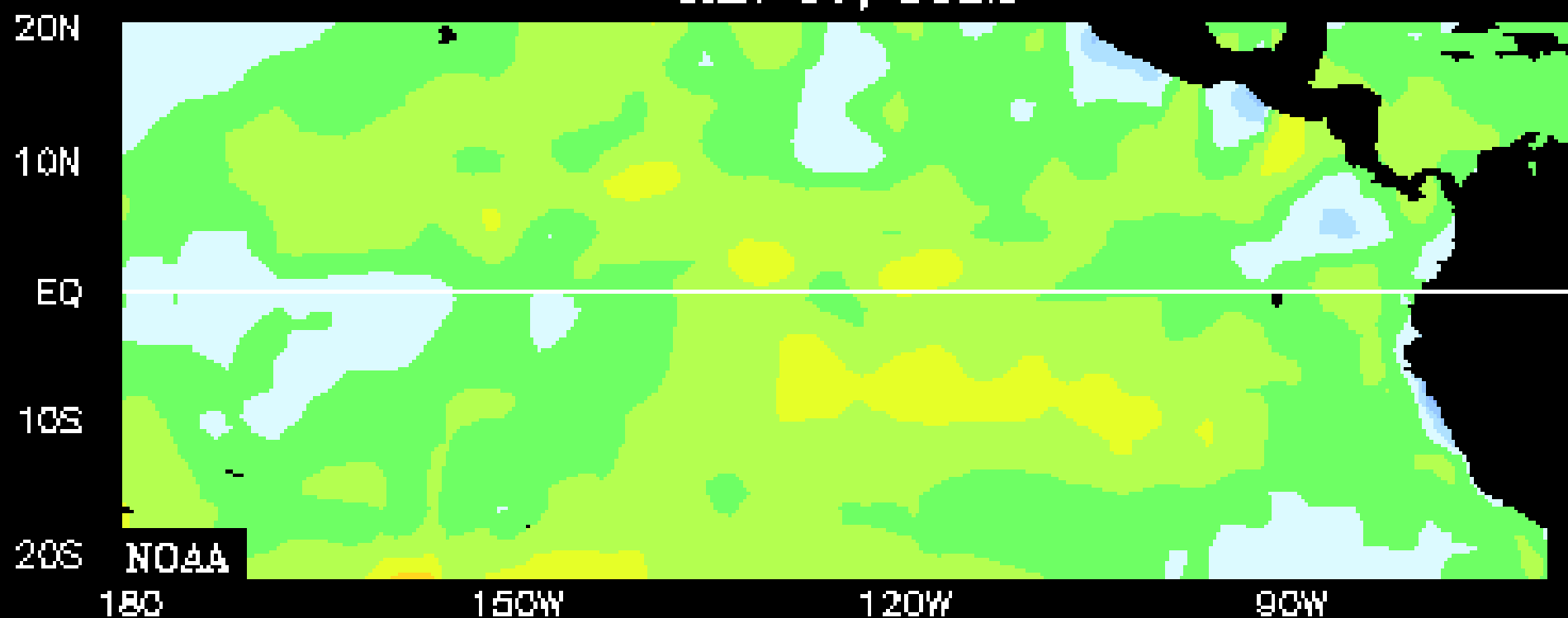


JAN 04, 1998



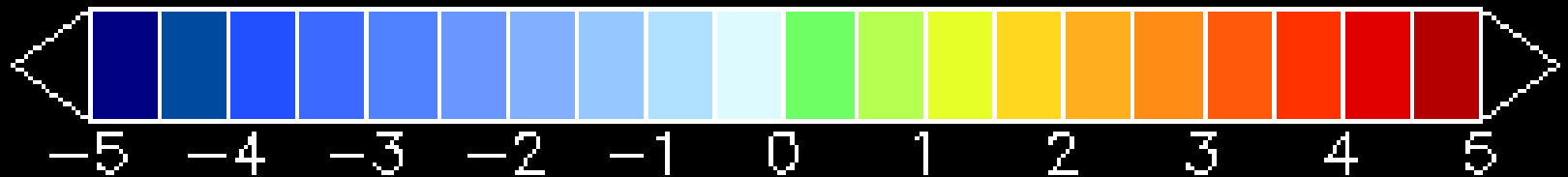
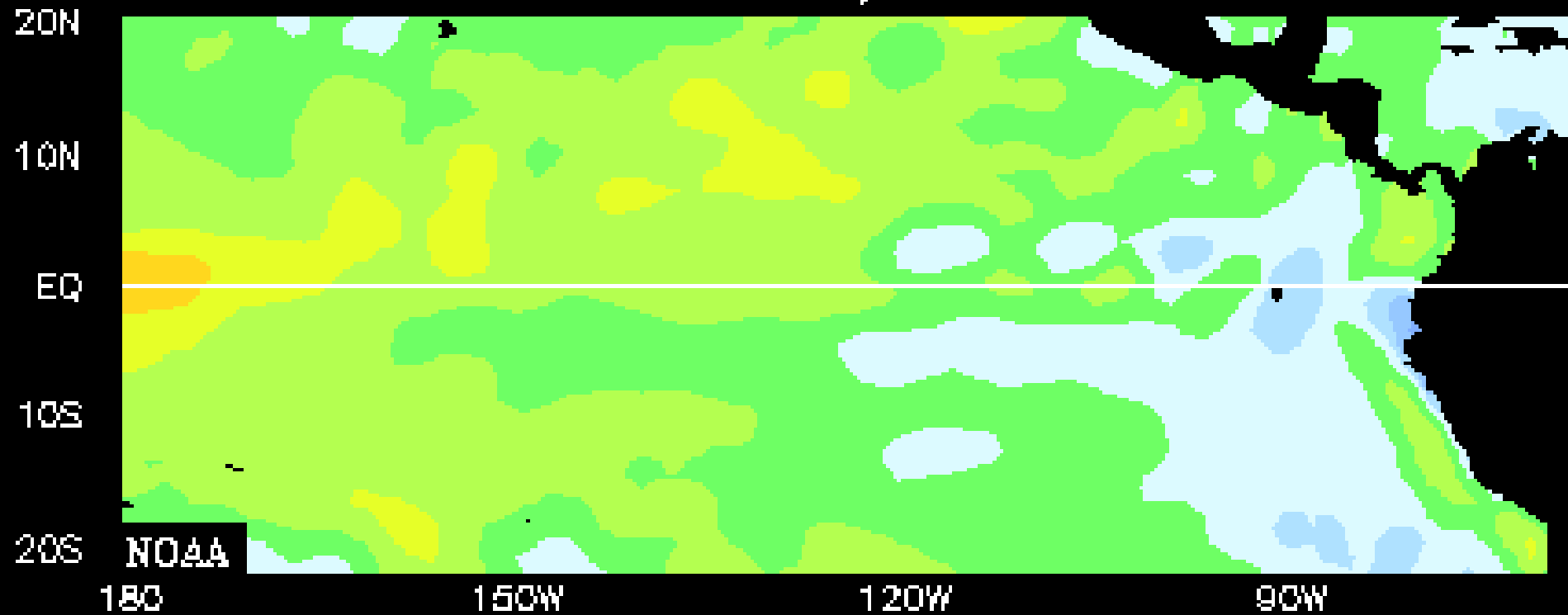
# SST ANOMALIES °C

JAN 07, 1982



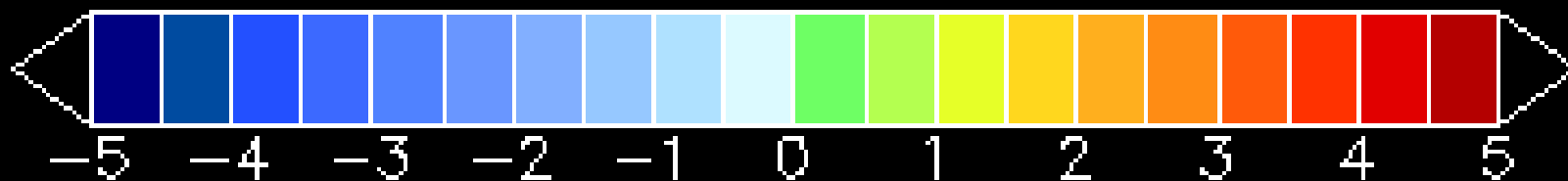
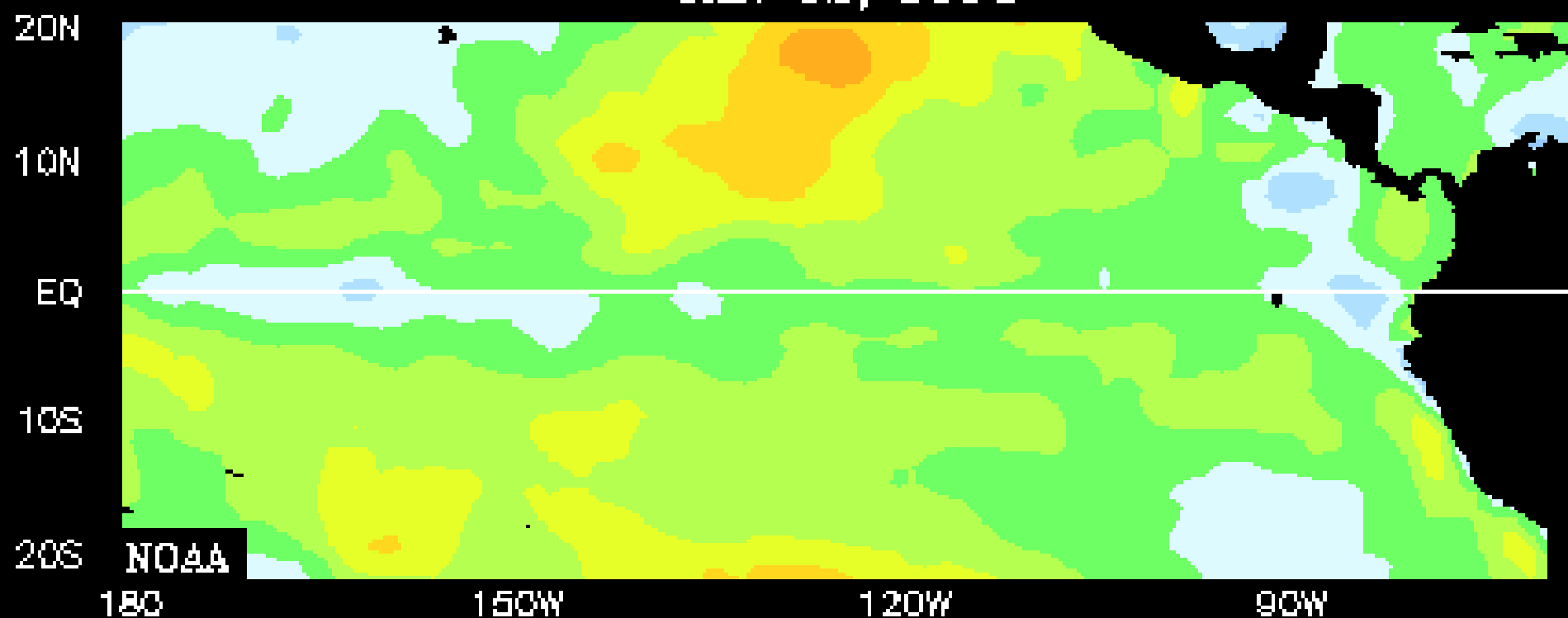
# SST ANOMALIES °C

JAN 08, 1991



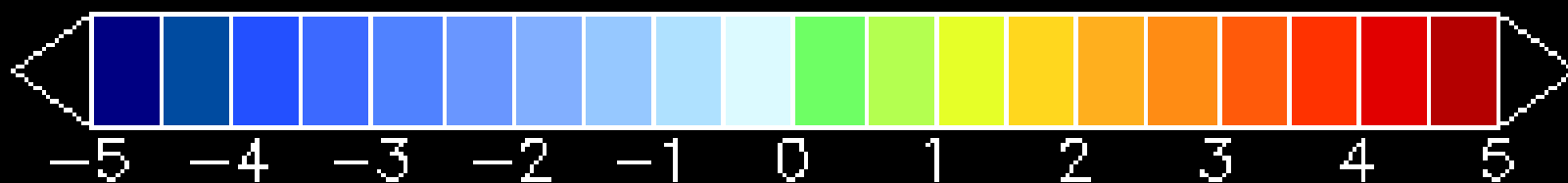
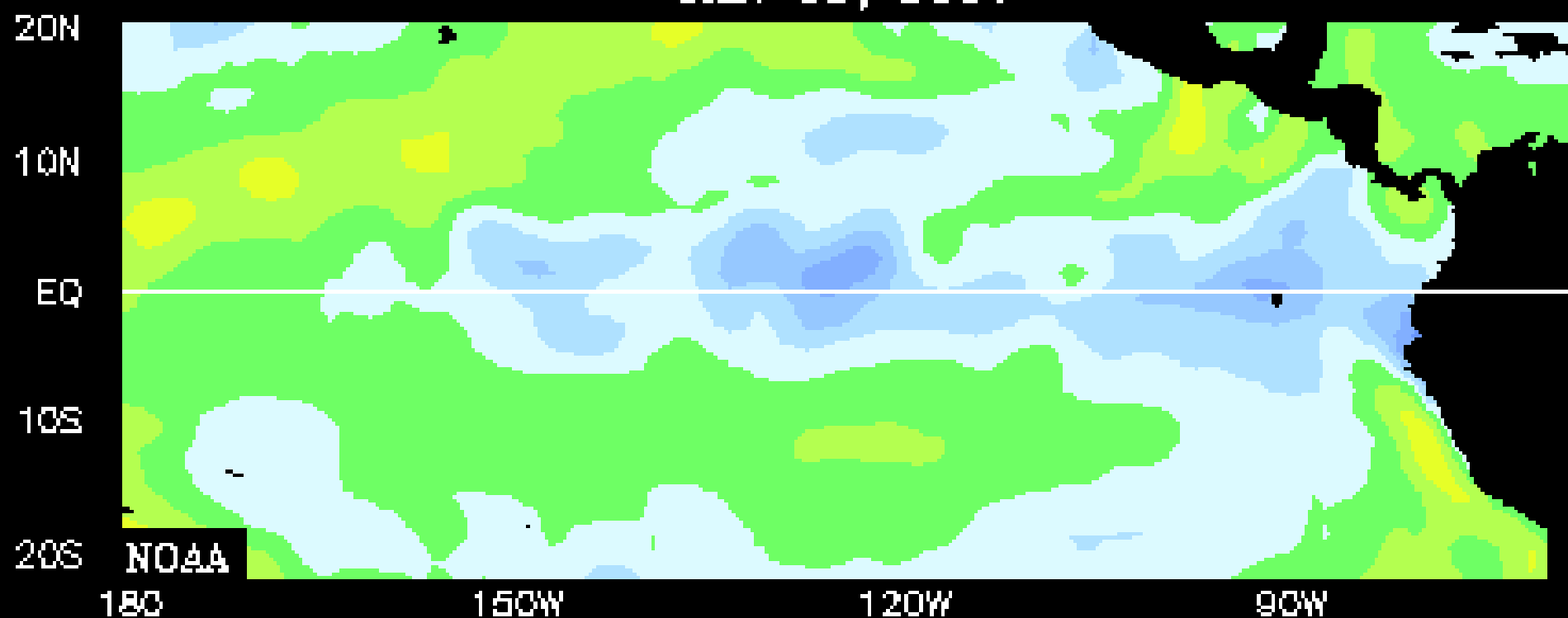
# SST ANOMALIES °C

JAN 02, 1994



# SST ANOMALIES °C

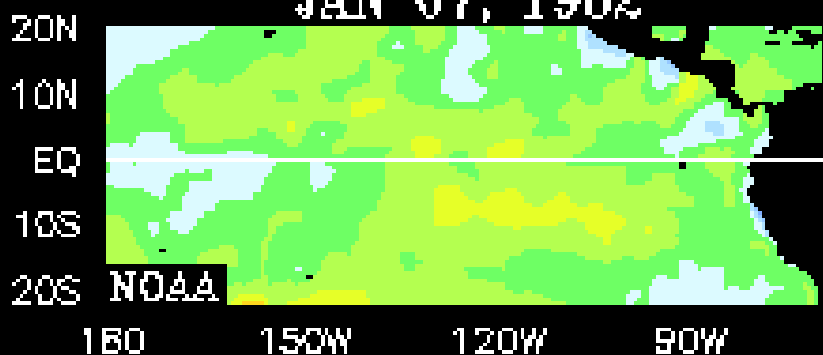
JAN 05, 1997



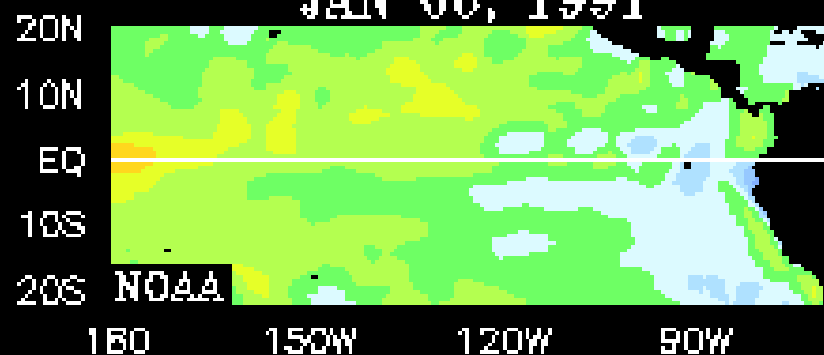


# SST ANOMALIES °C

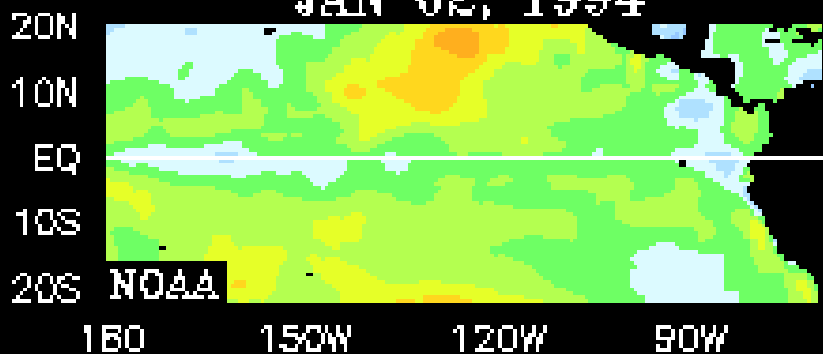
JAN 07, 1982



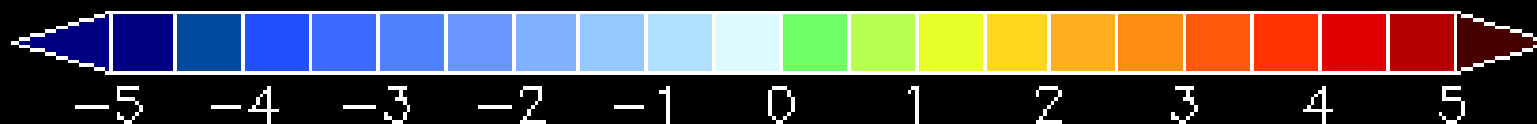
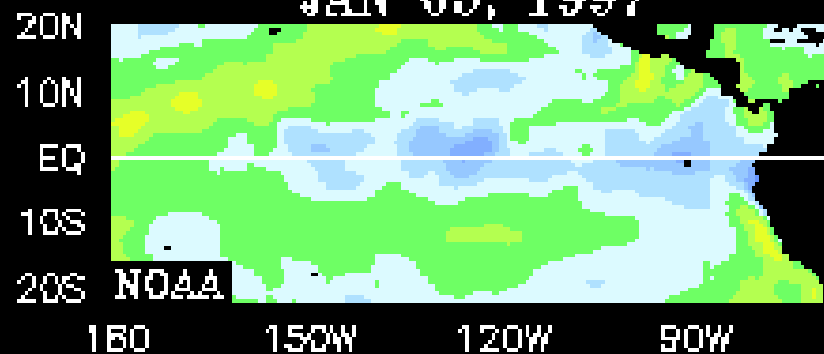
JAN 06, 1991



JAN 02, 1994

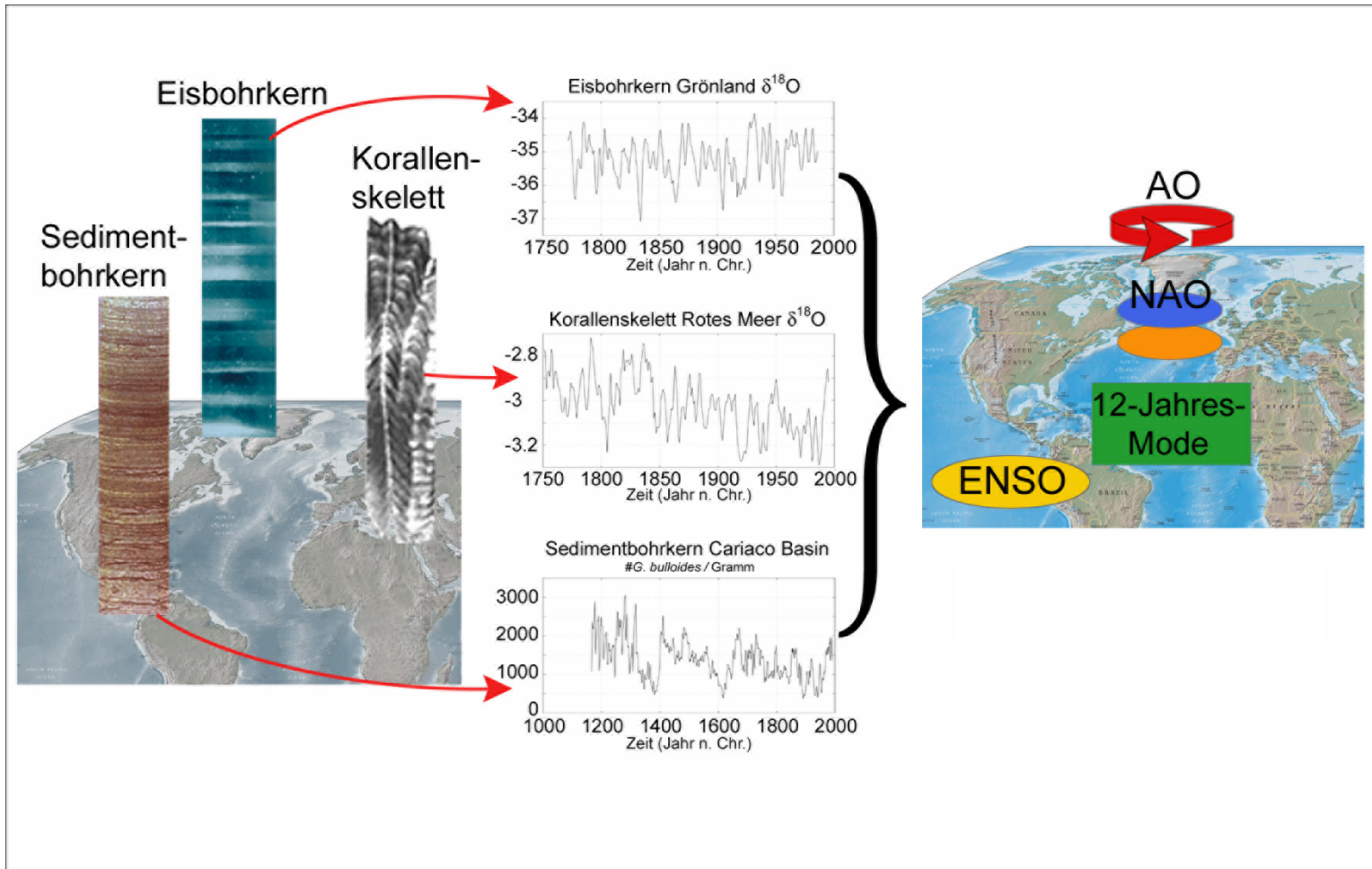


JAN 05, 1997



# Upscaling

## Interpretation of Proxy Data



# Proxy Data

- Annual, seasonal, etc.
- $^{18}\text{O}$ , etc.

# Instrumental Data

- Daily, Annual, seasonal, etc.
- Temperature, salinity, precipitation, etc.

# Statistic

## Covariance (cross, auto)

$$\gamma(\Delta) = E \left( (x(t) - \bar{x}) (y(t + \Delta) - \bar{y}) \right)$$

e.g. coral e.g. meteorol. data

## Correlation (cross, auto)

$$\rho_{xy} = \frac{\gamma(\Delta)}{\text{normalized}}$$

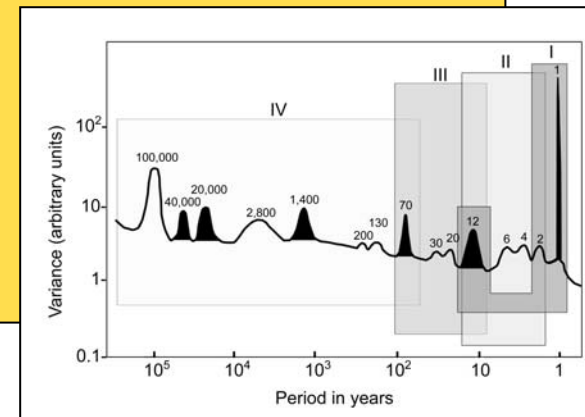
measures the tendency of x (t) and y (t) to covary

## Spectrum (cross, auto)

(spectral density)

$$\Gamma(\omega) = \sum_{\Delta=-\infty}^{\infty} \gamma(\Delta) e^{-2\pi i \Delta \omega}$$

measures variance

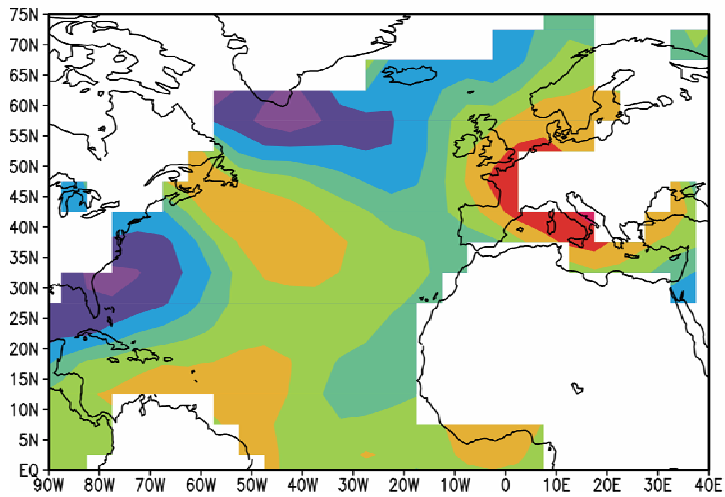


# Spatial pattern

- Regression
- Correlation
- Composite maps

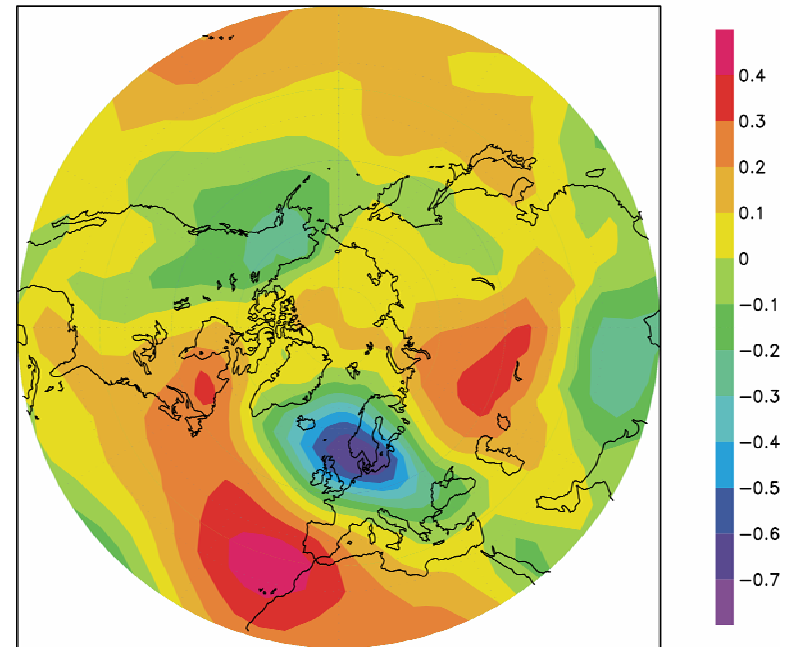
# Correlation: Precipitation Kiel

COR PP-KIEL SST WINTER INTERANNUAL



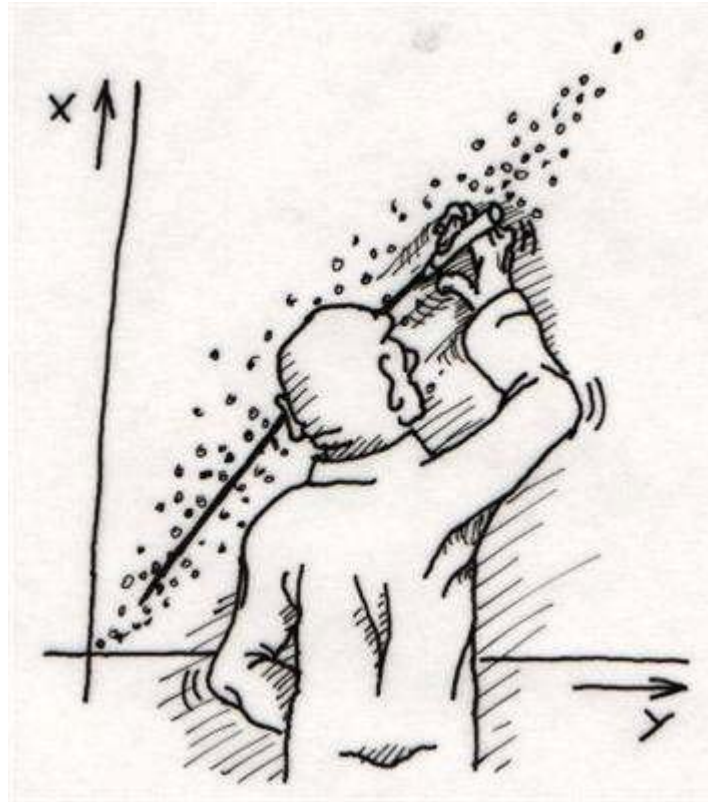
**SST**

COR PP-KIEL SLP WINTER INTERANNUAL



**SLP**

# Regression



# Regression

**Linear function  $f(x) = a x + b$**

**Task: find  $f(x)$  given data points  $g(x_i)$**

**Such that  $( f(x_i)-g(x_i) )^2$  is minimal**



# linear regression

models the relationship between a dependent variable  $Y$ , independent variables  $X_p$ , and a random term  $\varepsilon$ . The model can be written as

$$Y = \beta_1 + \beta_2 X_2 + \cdots + \beta_p X_p + \varepsilon$$

where  $\beta_1$  is the intercept ("constant" term), the  $\beta_i$ s are the respective parameters of independent variables, and  $p$  is the number of parameters to be estimated in the linear regression.

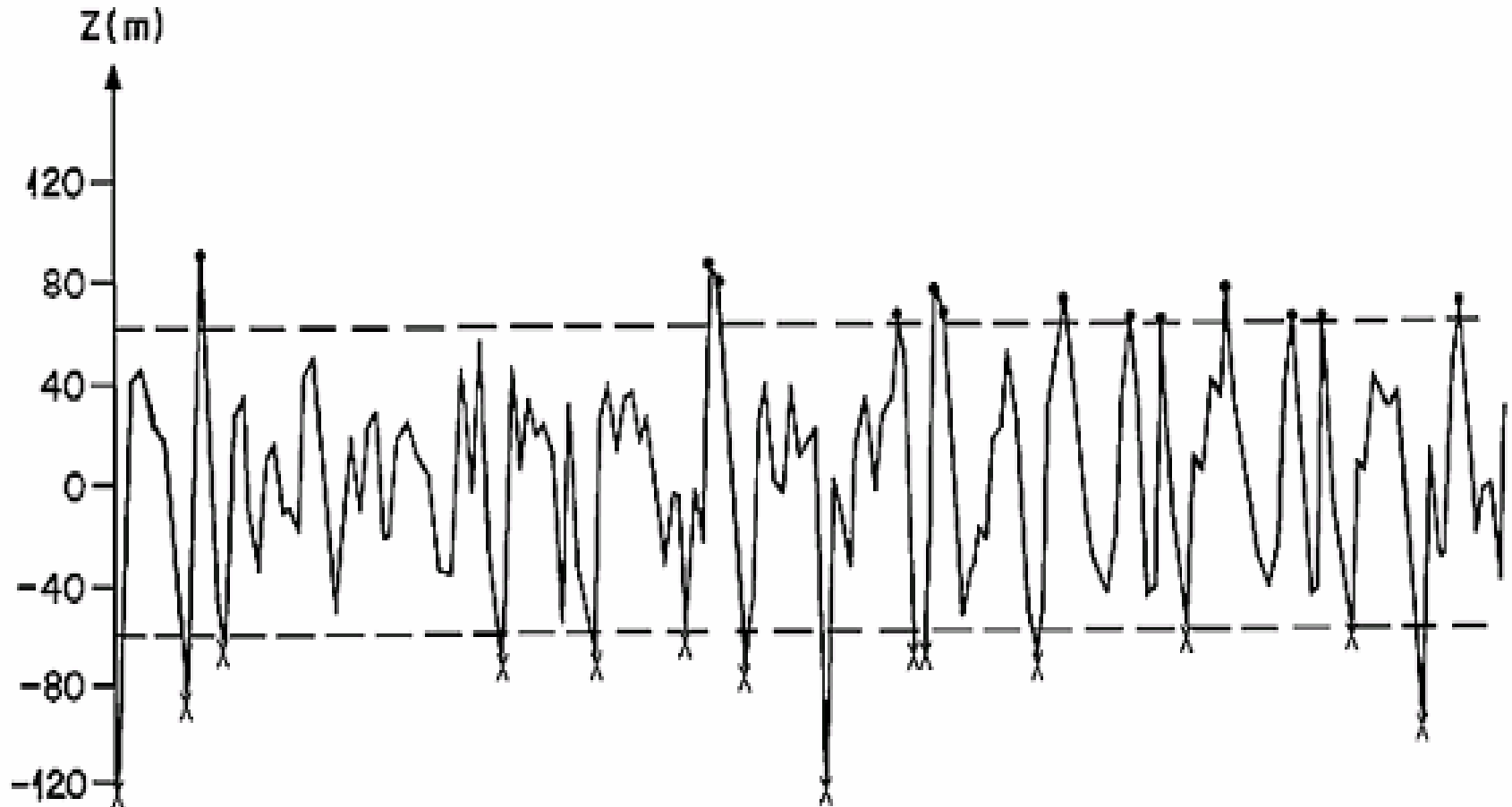
# Least-squares analysis

was developed by Carl Friedrich Gauss in the 1820s. This method uses the following assumptions:

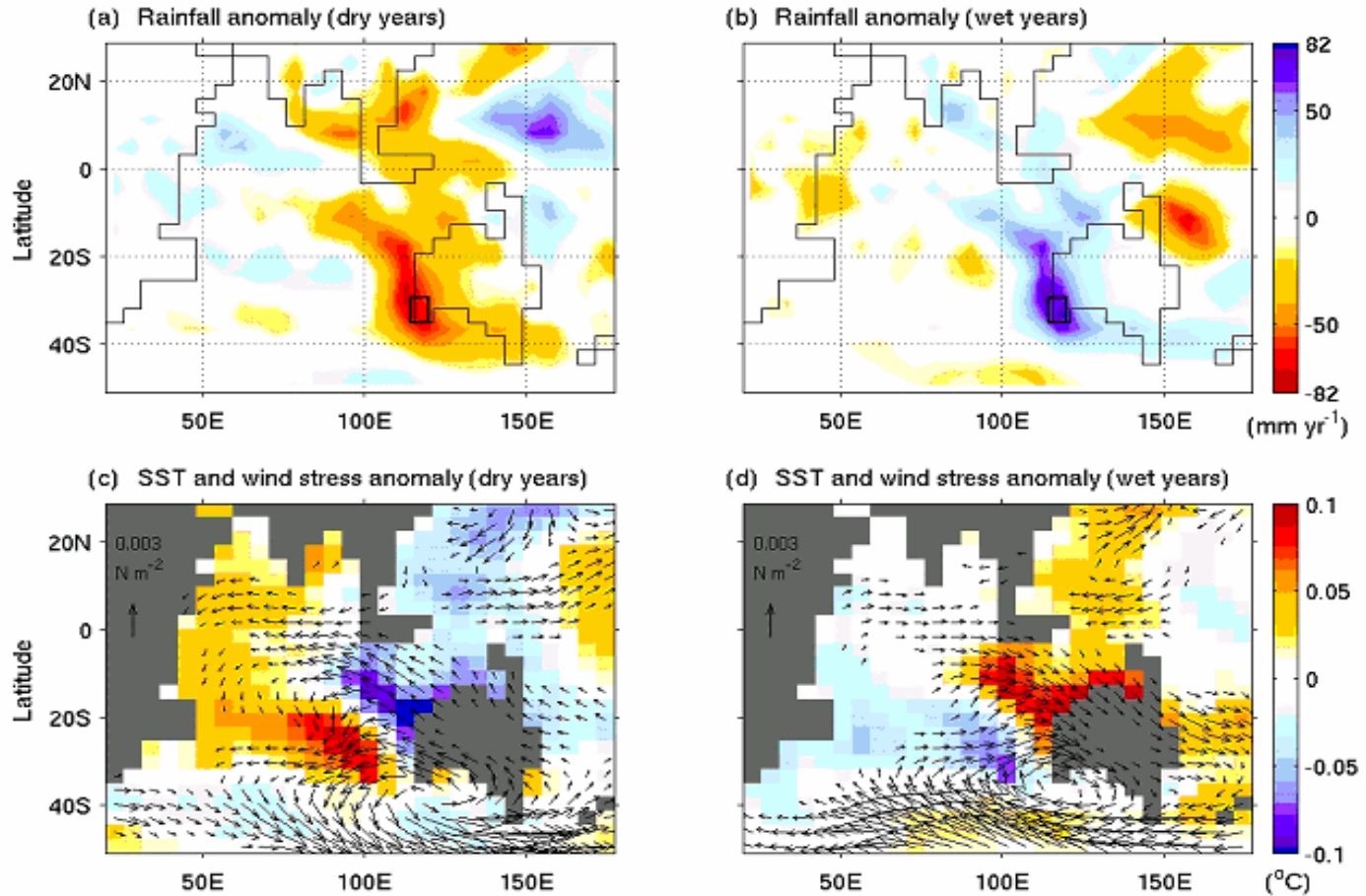
- The random errors  $\varepsilon_i$  have expected value 0
- The random errors  $\varepsilon_i$  are uncorrelated
- The random errors  $\varepsilon_i$  all have the same variance.

# Composite Maps

dt.: Kartenzusammenstellung

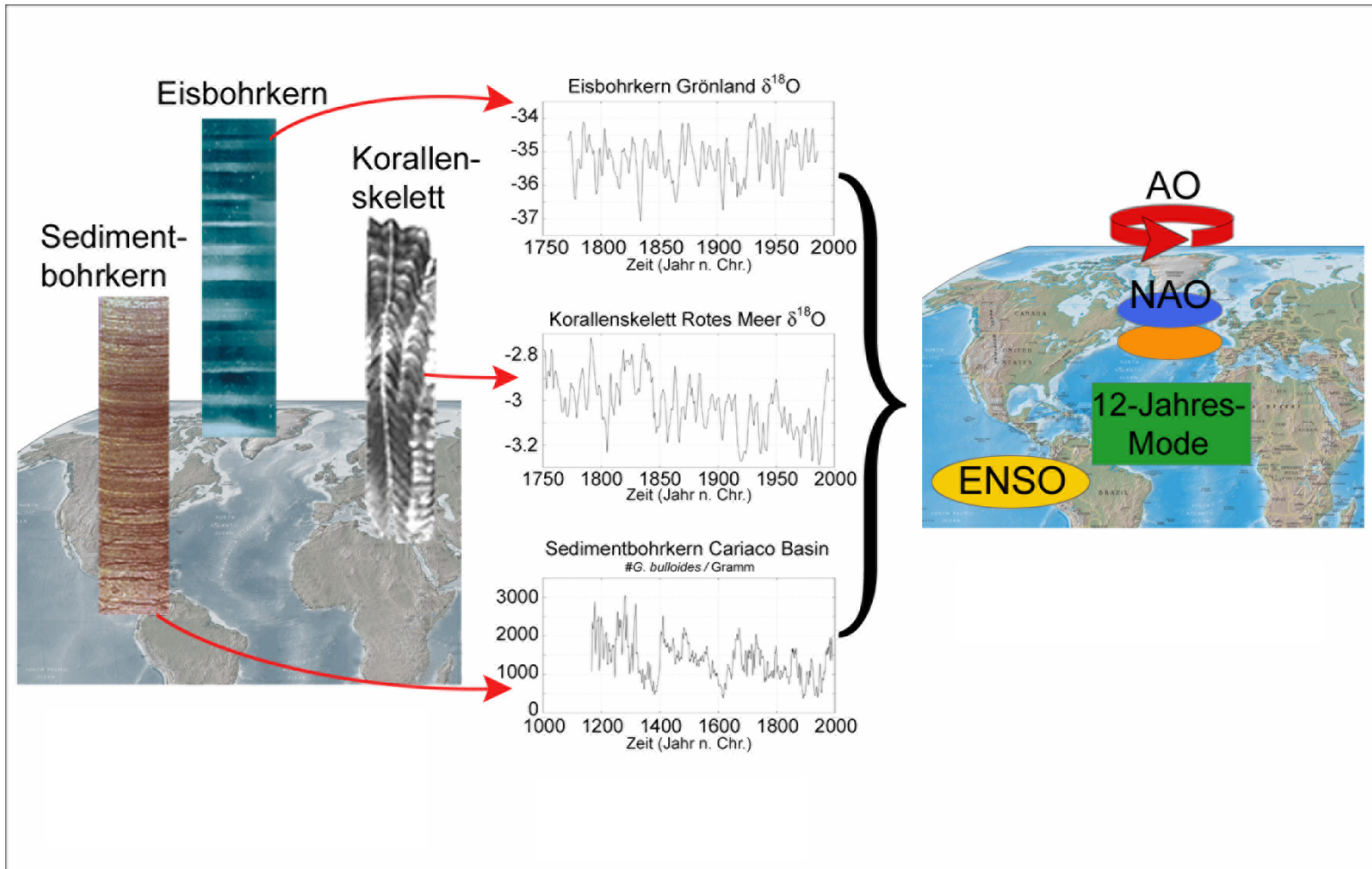


# Example



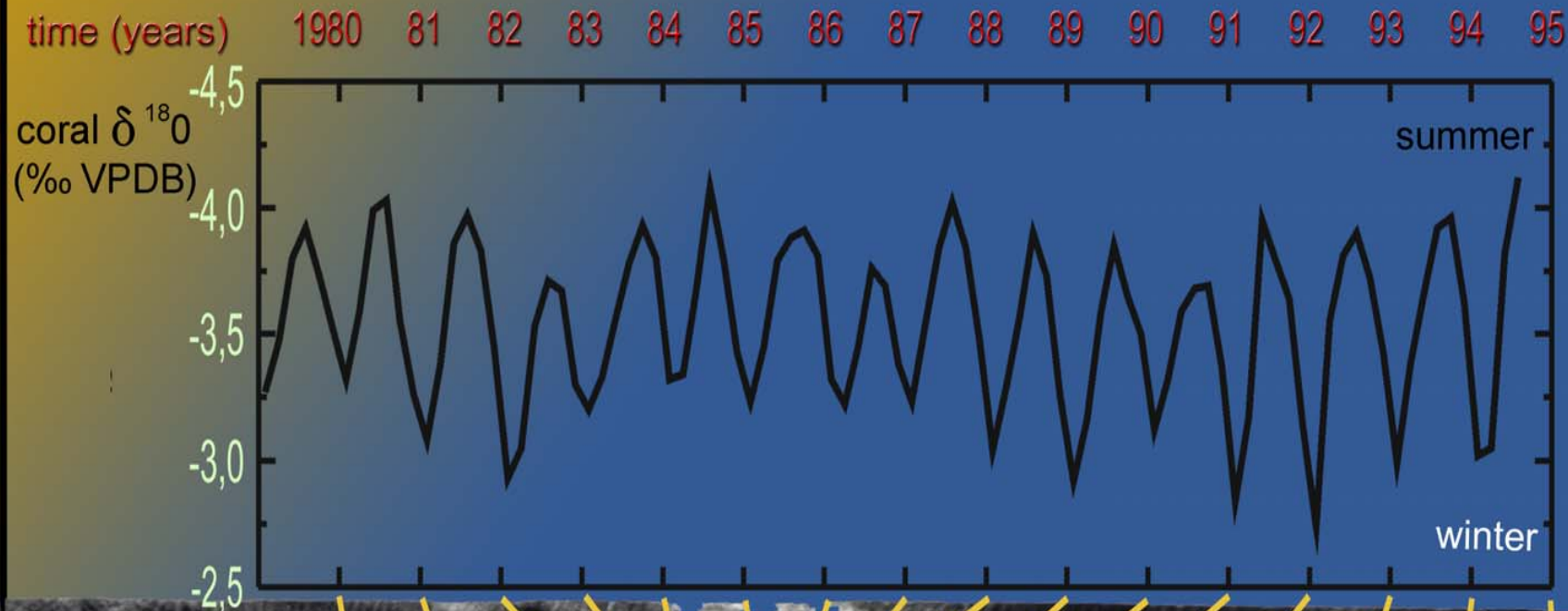
# Upscaling

## Interpretation of Proxy Data



# ARCTIC OSCILLATION SIGNATURE IN A RED SEA CORAL

## Seasonal oxygen isotope signature



Skeleton of Red Sea coral

# Statistic

## Covariance (cross, auto)

$$\gamma(\Delta) = E \left( (x(t) - \bar{x}) (y(t + \Delta) - \bar{y}) \right)$$

e.g. coral e.g. meteorol. data

## Correlation (cross, auto)

$$\rho_{xy} = \frac{\gamma(\Delta)}{\text{normalized}}$$

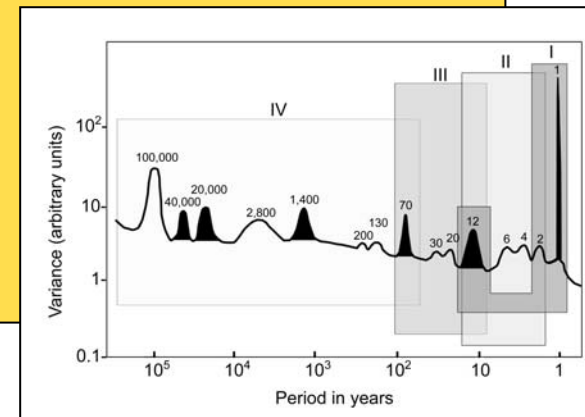
measures the tendency of x (t) and y (t) to covary

## Spectrum (cross, auto)

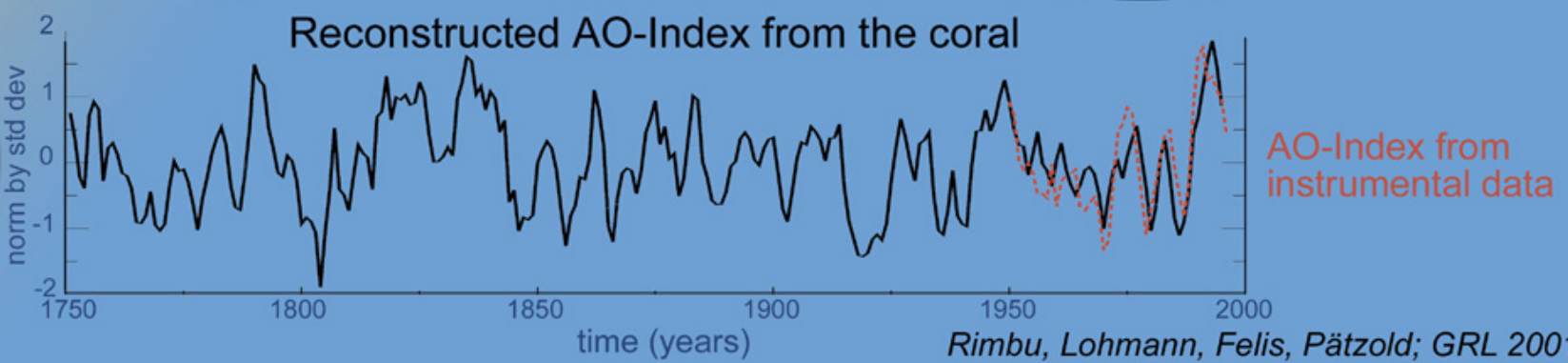
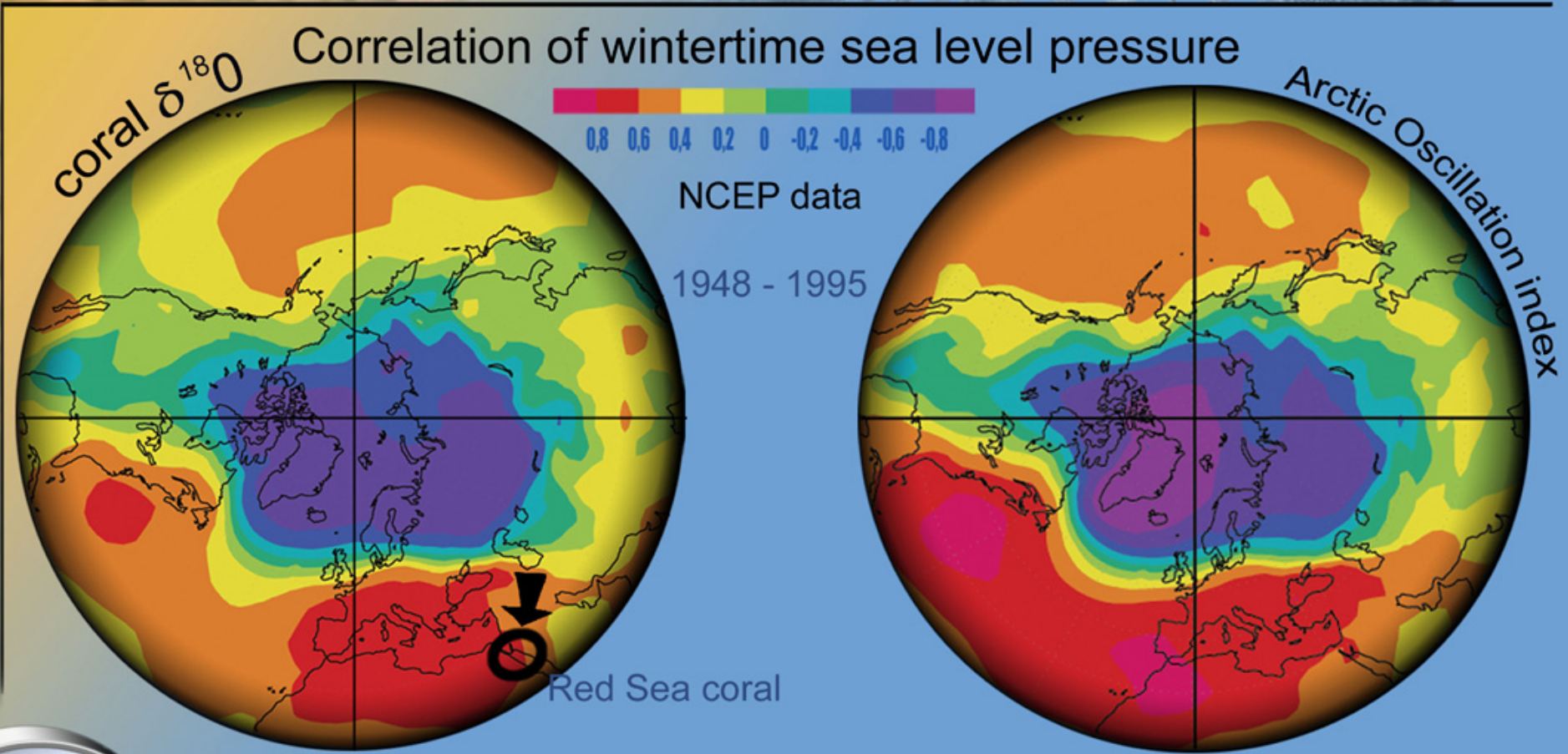
(spectral density)

$$\Gamma(\omega) = \sum_{\Delta=-\infty}^{\infty} \gamma(\Delta) e^{-2\pi i \Delta \omega}$$

measures variance

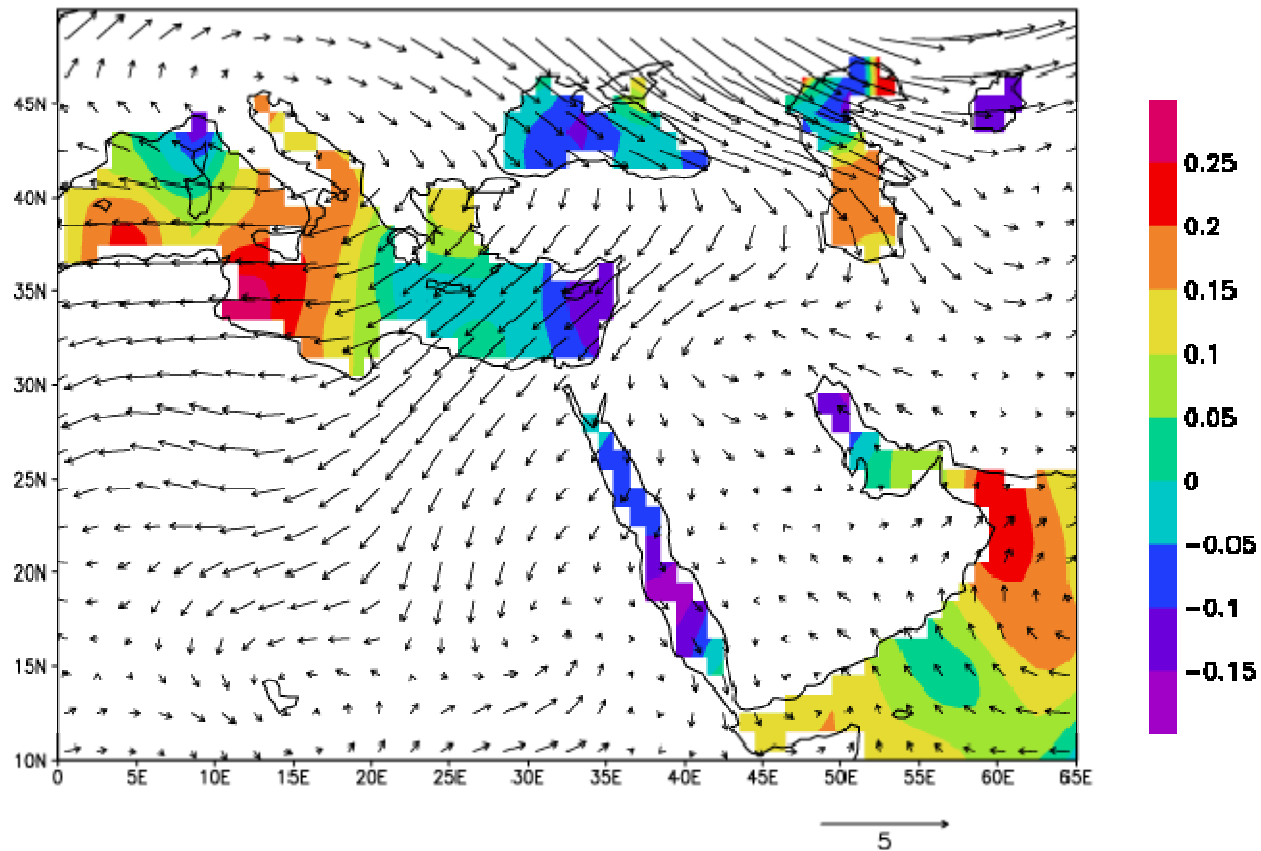


# ARCTIC OSCILLATION SIGNATURE IN A RED SEA CORAL





# ARCTIC OSCILLATION SIGNATURE IN A RED SEA CORAL



Composite Map of SST [ $^{\circ}\text{C}$ ] and 925 hPa wind [m/s]  
for 1948 -1995, January - February

**mechanistic understanding**

# Practical units for Dynamics II

21. May 2007

- Analysis of spatio-temporal pattern
- Open web browser (e.g. mozilla)
- <http://climexp.knmi.nl/>
- <http://kiste.palmod.uni-bremen.de:8080/upsc/>  
(student mensa)
- Time series (choose one, calculate one)
- Climate of your home town/region (4 seasons)
- Use correlation, regression, composite maps
- Write a report (2-4 pages)

# Examples

