

On the similarity and apparent cycles of isotopic variations in East Antarctic snow and ice cores

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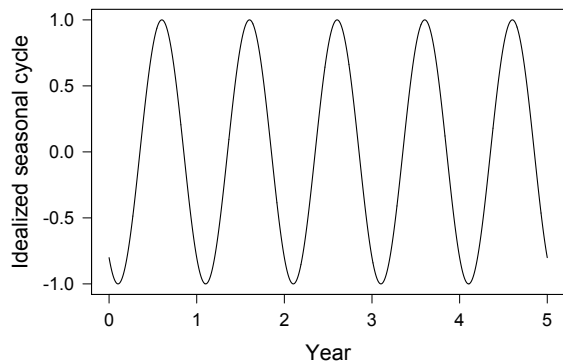
³ Laboratoire des Science du Climat et de l'Environnement – IPSL, France



Cycles in climatic parameters (?)

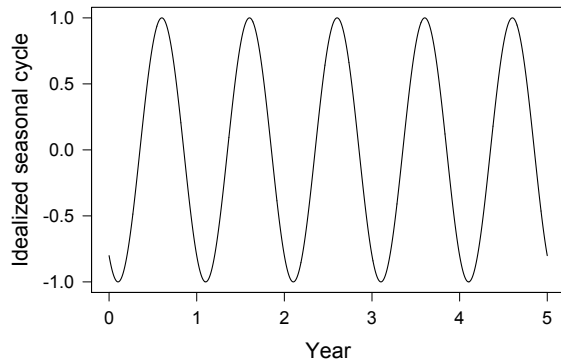
Cycles in climatic parameters (?)

Periodic seasonal cycle (temperature).

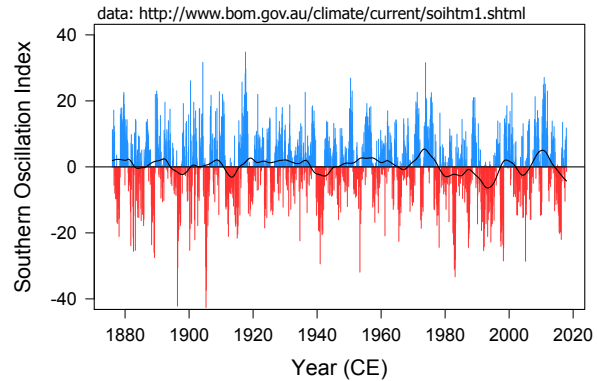


Cycles in climatic parameters (?)

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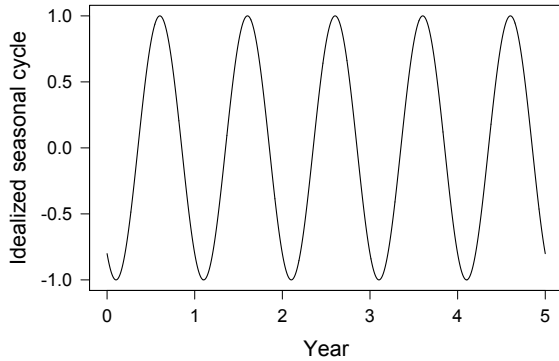


Quasi-periodic oscillations (e.g. ENSO).

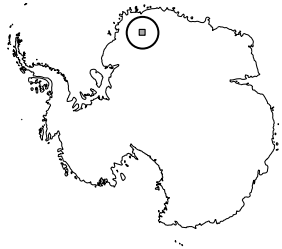
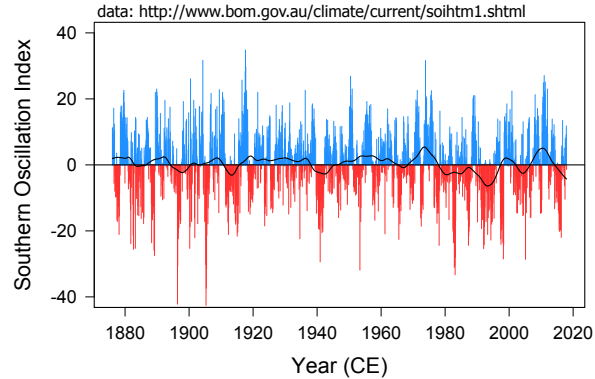


Cycles in climatic parameters (?)

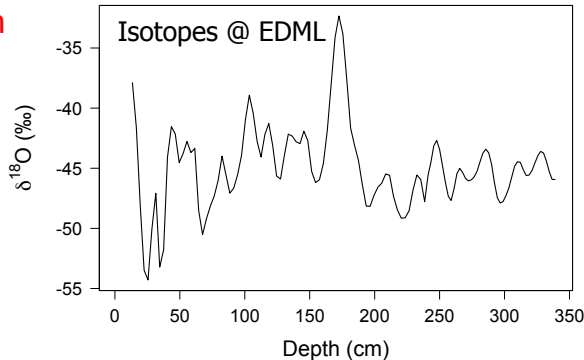
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Quasi-periodic oscillations (e.g. ENSO).



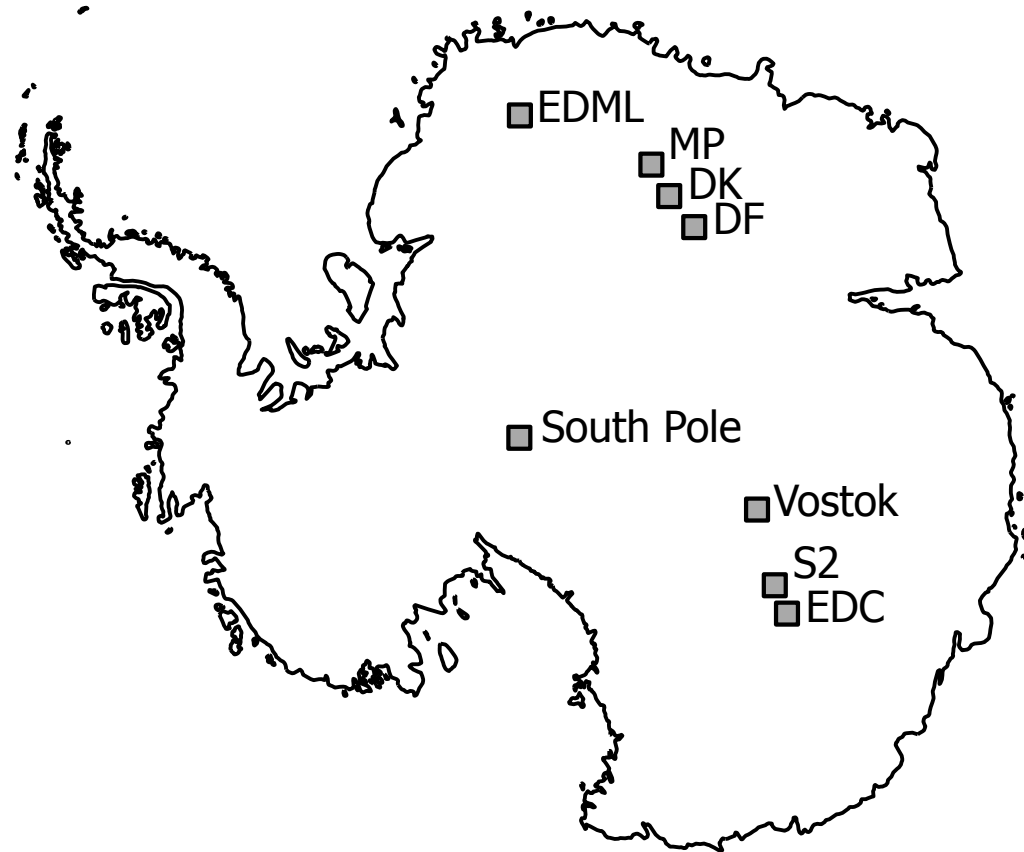
warm
↑
↓
cold



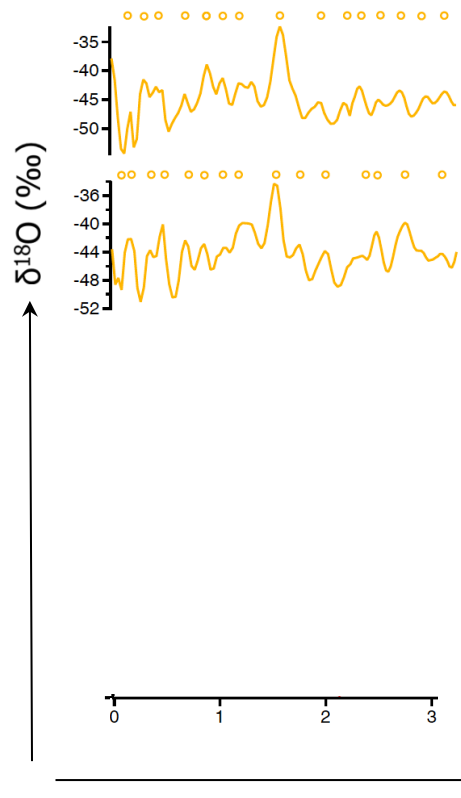
- Stable isotopes from Antarctic snow are interpreted as proxy for temperature.
- What is the **origin of the apparent cycles** in the isotopic time series?

Münch et al. (2017), Cryosphere

Similar “cycles” in East Antarctic isotope profiles



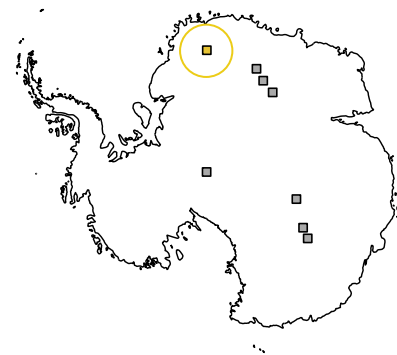
Similar "cycles" in East Antarctic isotope profiles



EDML

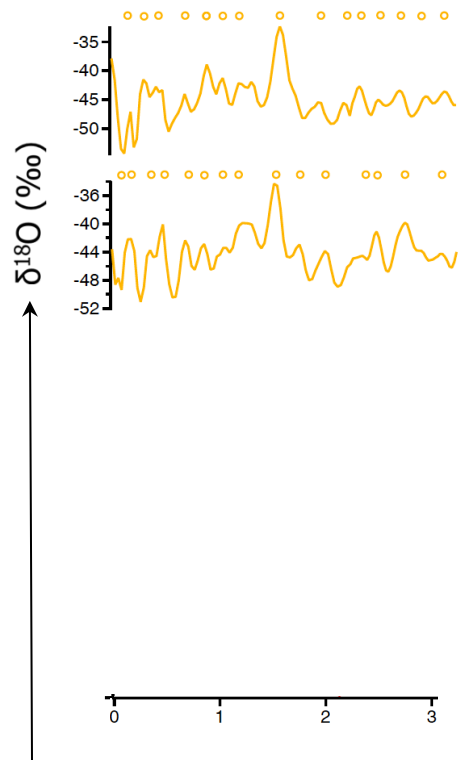
~ 18 cm annual accumulation of snow

$\Delta_{\text{max}} \sim 19$ cm average distance between maxima



Casado et al. (2017), Cryosphere Disc.

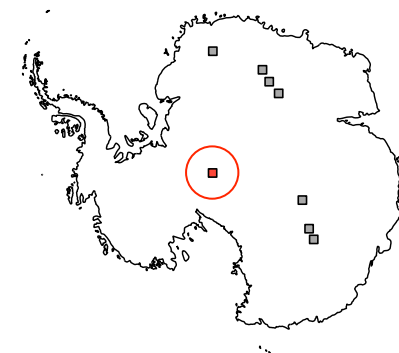
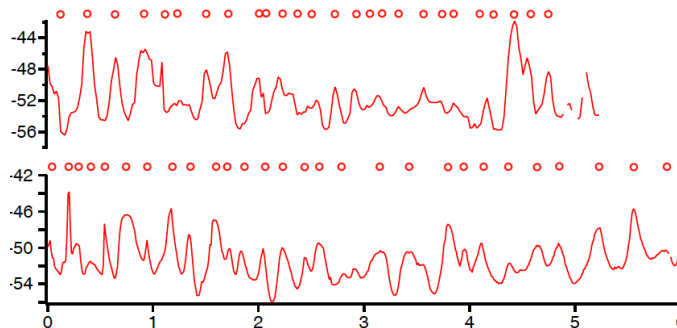
Similar "cycles" in East Antarctic isotope profiles



EDML

~ 18 cm annual accumulation of snow

Δ_{\max} ~ 19 cm average distance between maxima



South Pole

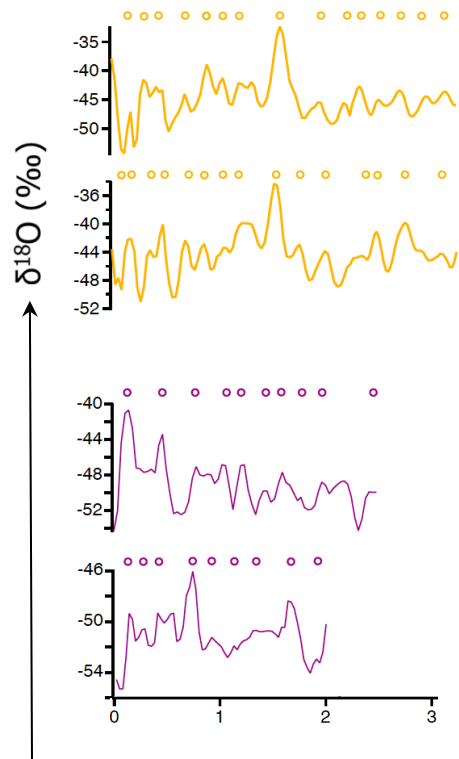
accum. ~ 20 cm

Δ_{\max} ~ 20 cm

Depth (m)

Casado et al. (2017), Cryosphere Disc.

Similar "cycles" in East Antarctic isotope profiles



EDML

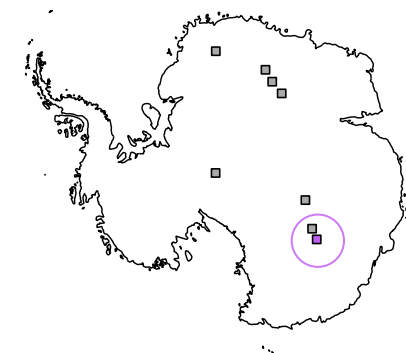
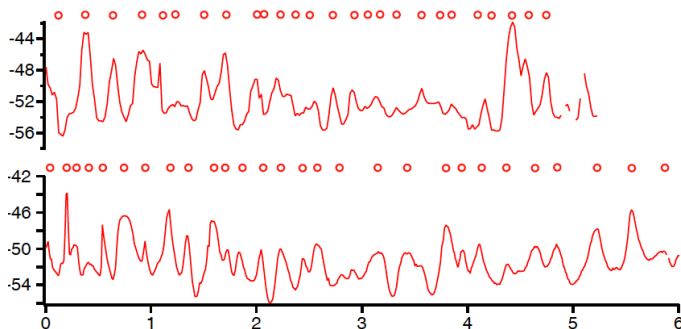
~ 18 cm annual accumulation of snow

Δ_{\max} ~ 19 cm average distance between maxima

Dome C

accum. ~ 8 cm

Δ_{\max} ~ 18 cm



South Pole

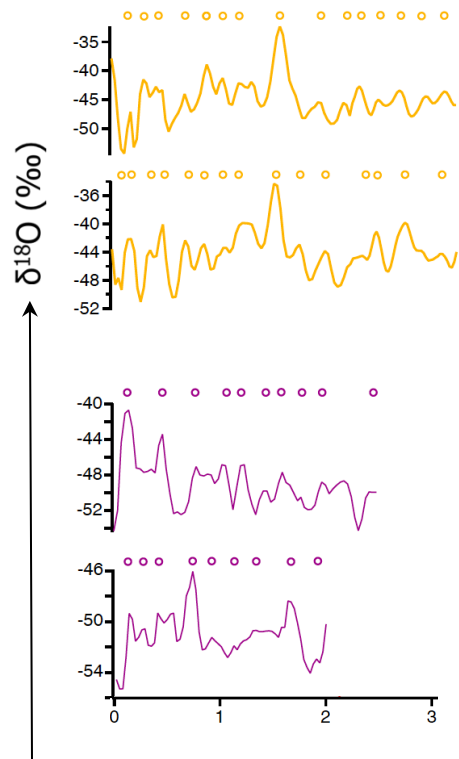
accum. ~ 20 cm

Δ_{\max} ~ 20 cm

Depth (m)

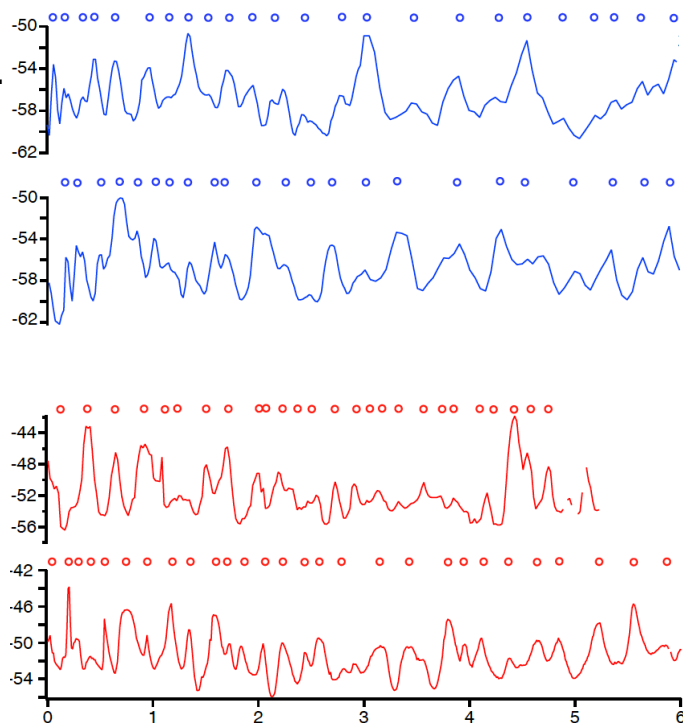
Casado et al. (2017), Cryosphere Disc.

Similar "cycles" in East Antarctic isotope profiles



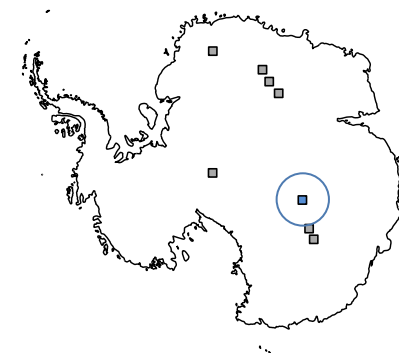
EDML
 ~ 18 cm accum.
 $\Delta_{\max} \sim 19$ cm

Dome C
 accum. ~ 8 cm
 $\Delta_{\max} \sim 18$ cm



Vostok
 accum. ~ 7 cm
 $\Delta_{\max} \sim 22$ cm

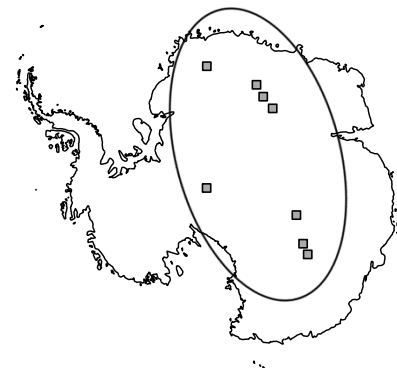
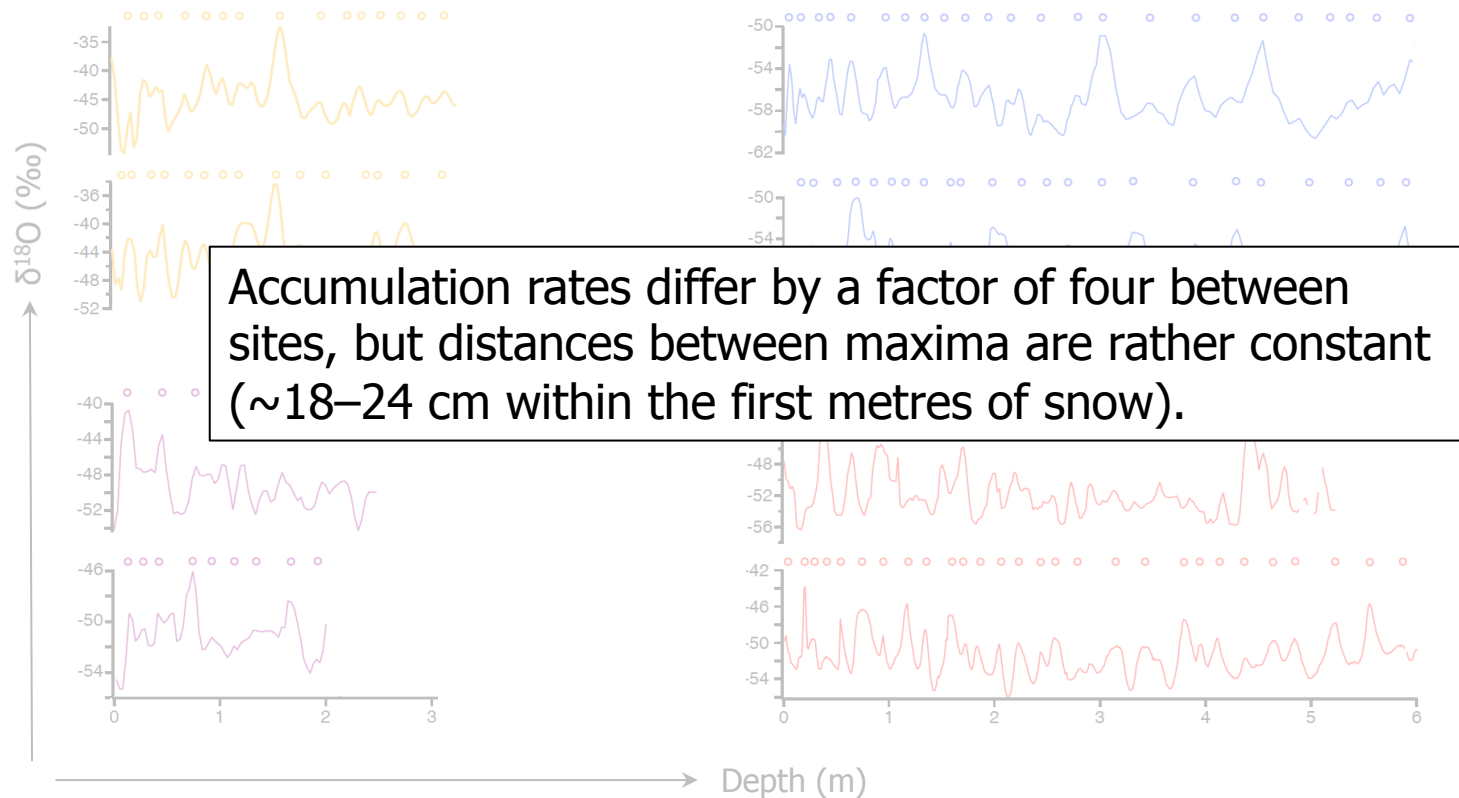
South Pole
 accum. ~ 20 cm
 $\Delta_{\max} \sim 20$ cm



Depth (m)

Casado et al. (2017), Cryosphere Disc.

Similar "cycles" in East Antarctic isotope profiles



Casado et al. (2017), Cryosphere Disc.

Understanding observed cycles

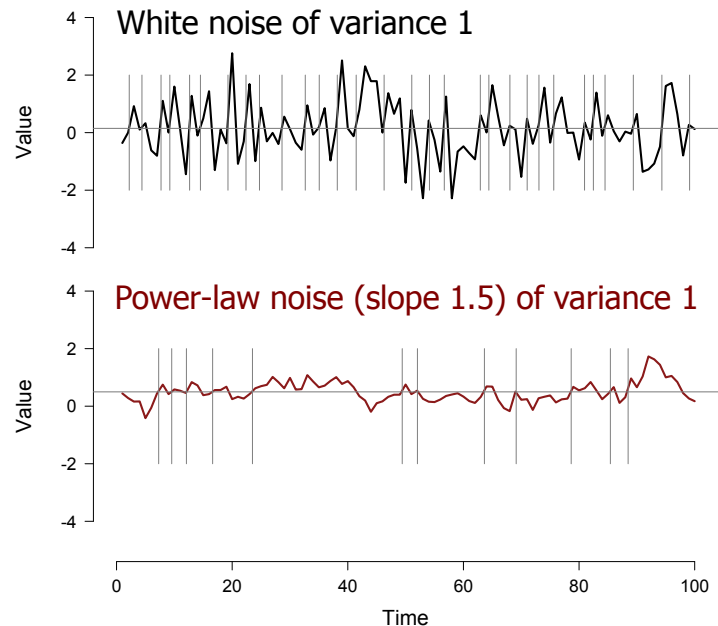
1. Mathematics for crossing statistics of random noise: Rice's formula
2. Model for signal formation of isotope profiles

Rice's formula

How often does a random time series cross the zero line / have maxima?

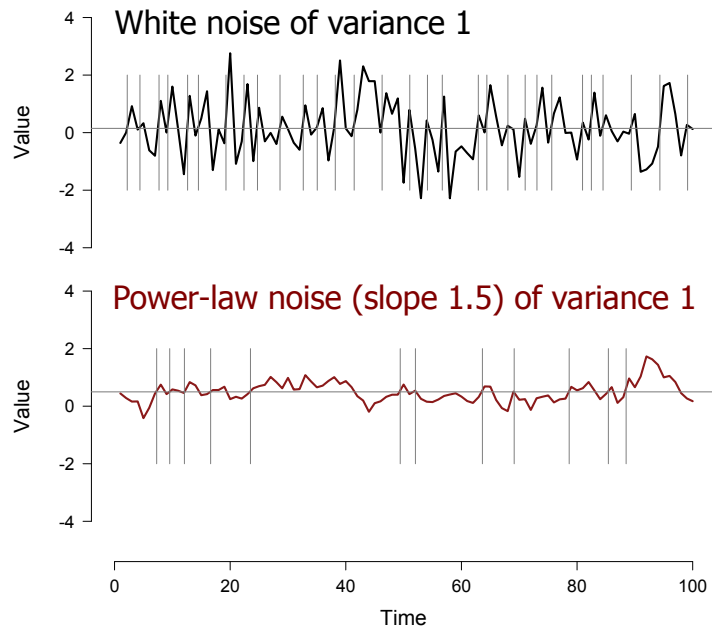
Rice's formula

How often does a random time series cross the zero line / have maxima?



Rice's formula

How often does a random time series cross the zero line / have maxima?



➤ Formula by S. O. Rice (Rice, 1944, 1945):

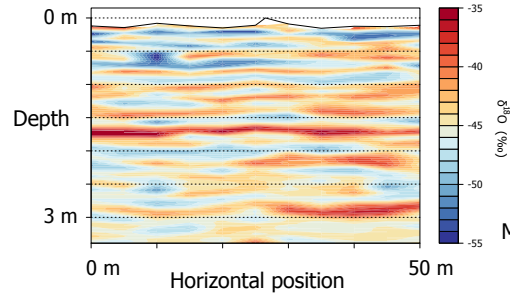
Expected distance between upward crossings:

$$\Delta^+ = 2\pi \sqrt{\frac{\Omega_0}{\Omega_2}} \propto \sqrt{\frac{\text{var}(X)}{\text{var}(X')}}$$

Expected distance between maxima:

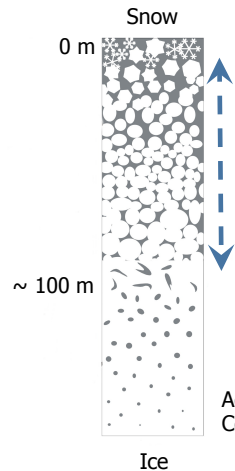
$$\Delta_{\max} = 2\pi \sqrt{\frac{\Omega_2}{\Omega_4}} \propto \sqrt{\frac{\text{var}(X')}{\text{var}(X'')}}$$

Isotope profiles qualitatively



On local scale: large spatial variability created in depositional process.

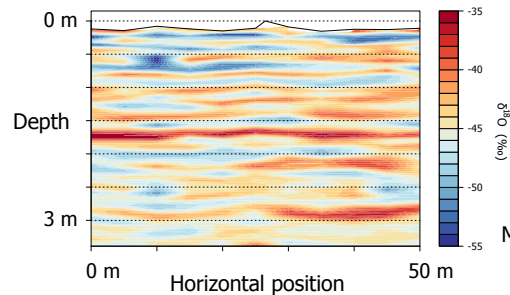
Modified from: Münch et al. (2018), Cryosphere



With depth: smoothing due to diffusional mixing of vapour within the snow and firn column.

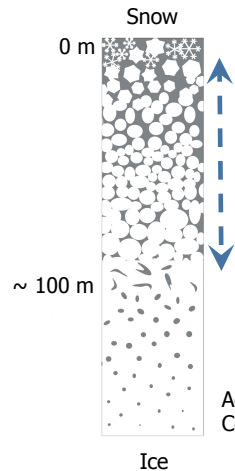
Adapted from:
Centre for Ice and Climate, University of Copenhagen

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Adapted from: Centre for Ice and Climate, University of Copenhagen

➤ Null hypothesis:
Rice's formula for
diffused white noise:

$$\Delta_{\max} = 2\pi \sqrt{\frac{2}{3}} \sigma$$

Diffusion length
~ similar across sites.

Laepple et al. (2018), Cryosphere

(More realistic) Forward model for isotope profiles

1. Isotopic seasonal cycle driven by local temperatures.

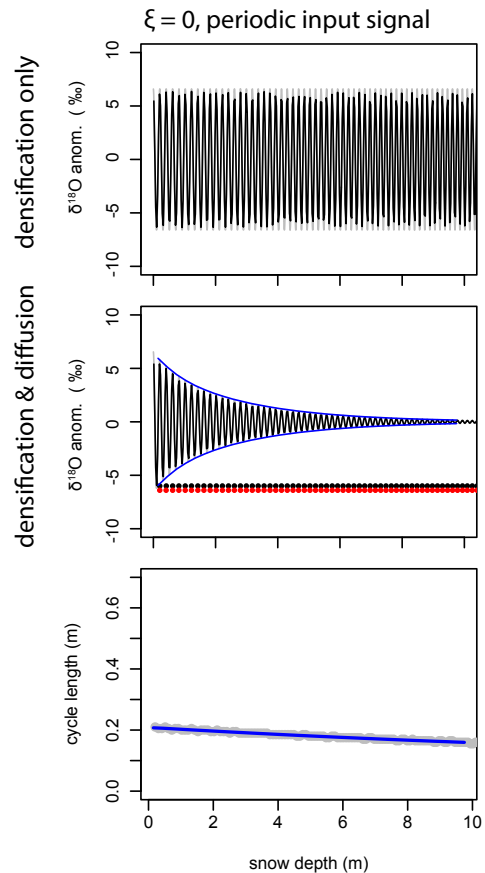


2. Part of variance (fraction ξ) transferred to noise in depositional process.



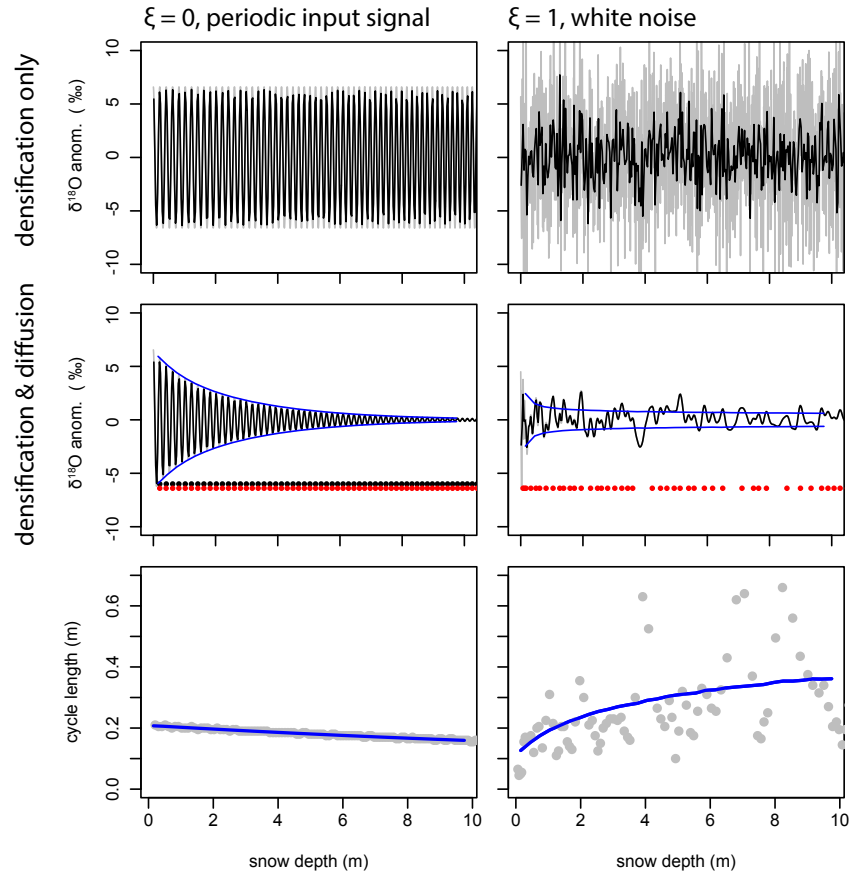
3. Diffusion and densification of signal.

Structure of isotopic signal & cycle length



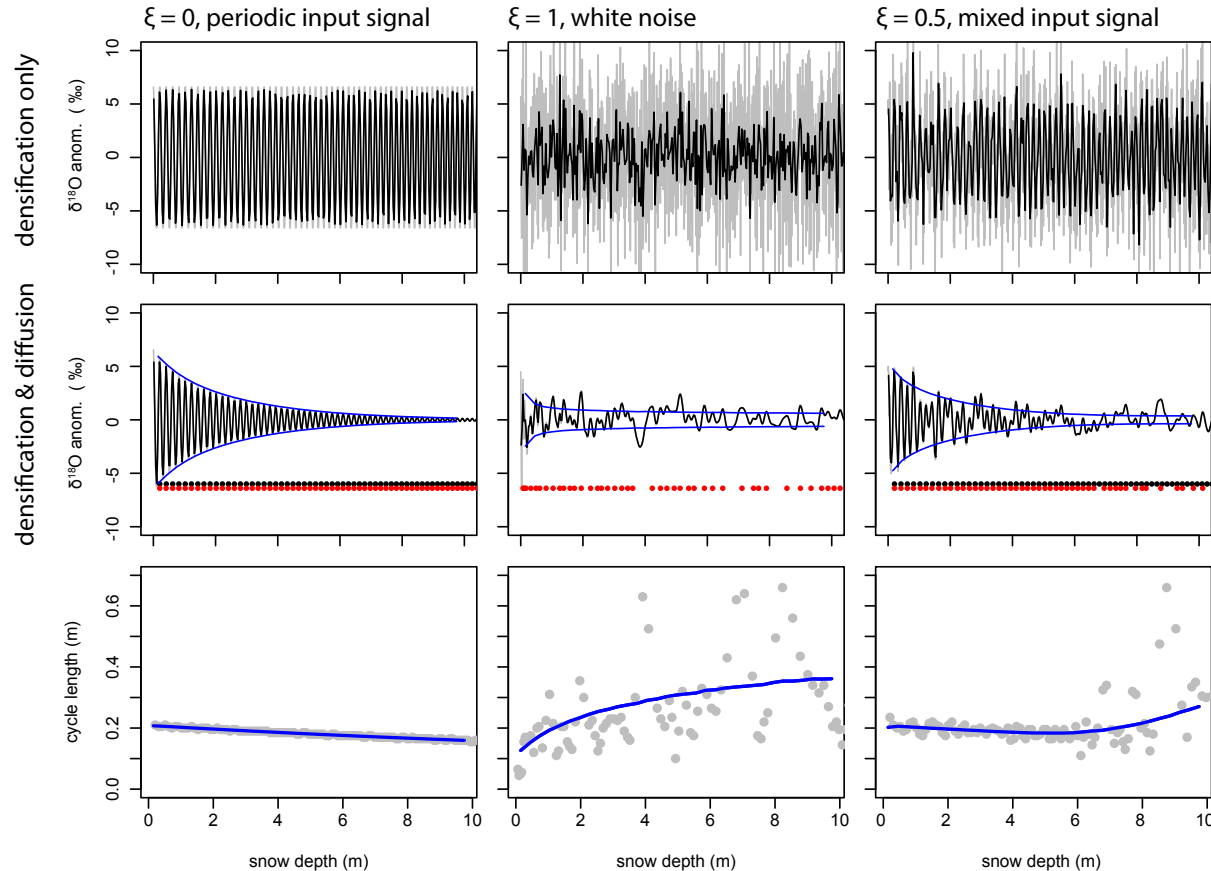
Laepple et al. (2018), Cryosphere

Structure of isotopic signal & cycle length



Laepple et al. (2018), Cryosphere

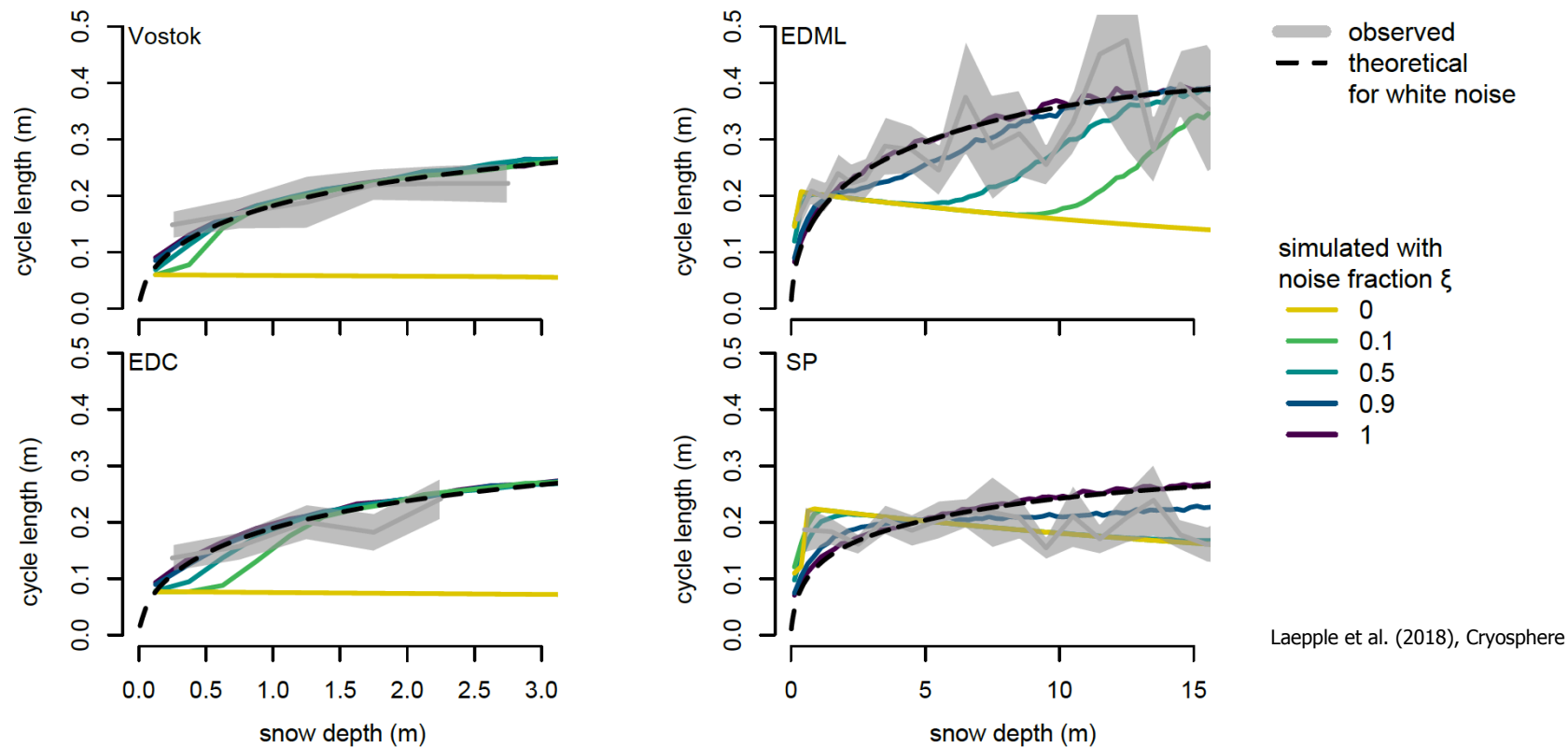
Structure of isotopic signal & cycle length



Depth dependency of "cycle length" informs about nature of signal.

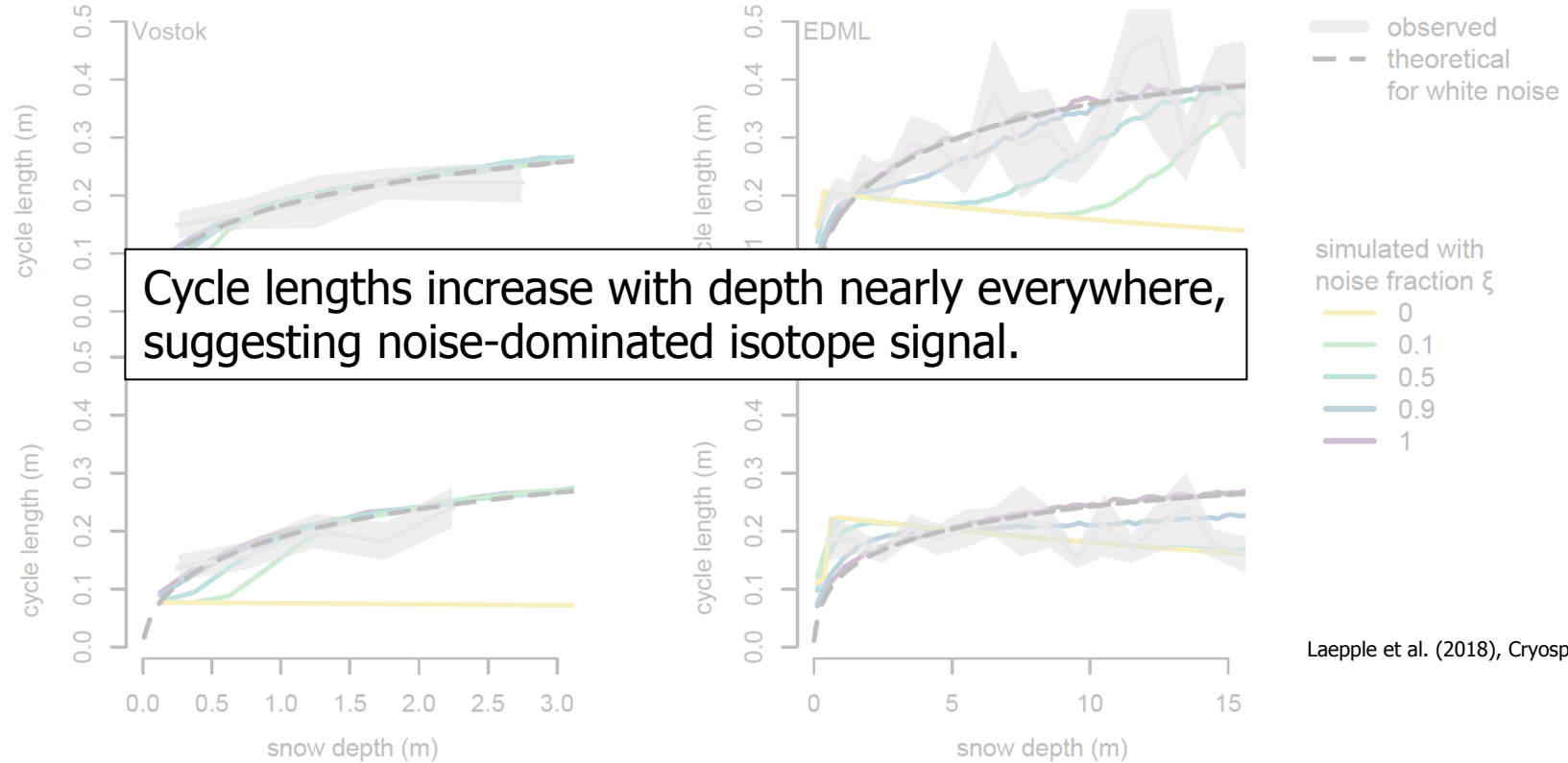
Laepple et al. (2018), Cryosphere

Observed vs. theoretical "cycle lengths"



Laepple et al. (2018), Cryosphere

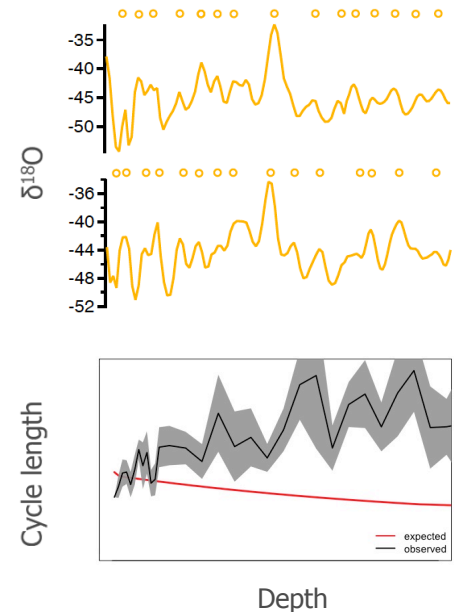
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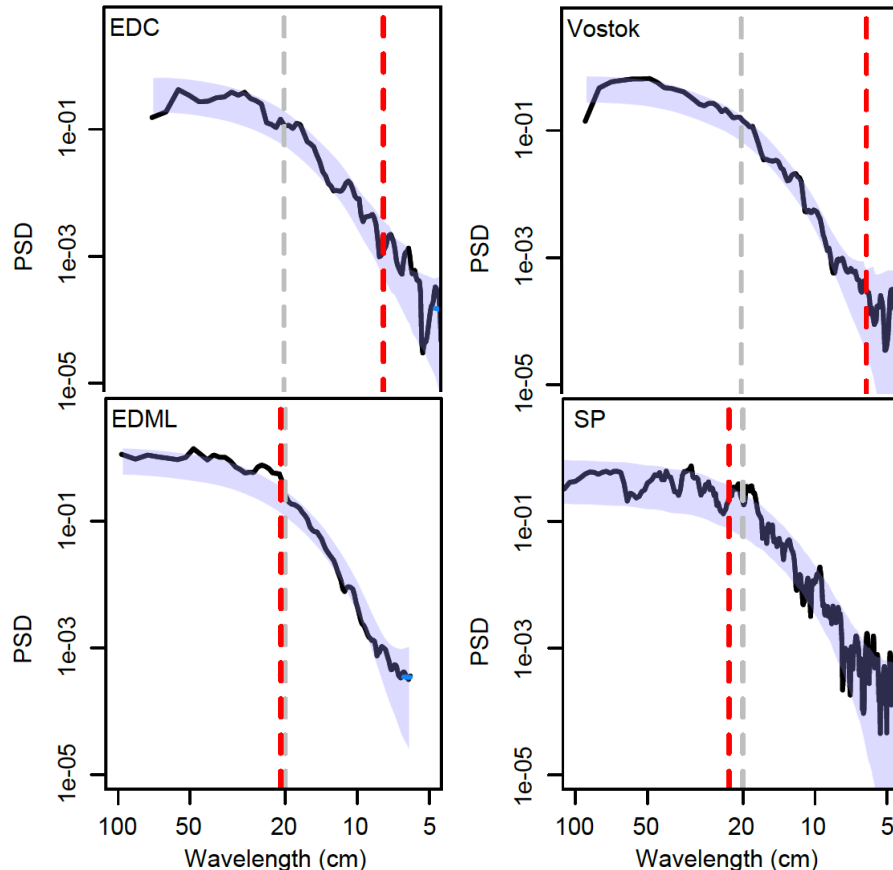
Laepple et al. (2018), Cryosphere

Summary

- Similar “cycle lengths” across East Antarctic are no direct climatic features but effect of diffusional smoothing.
- This suggests a mostly noise-dominated isotope signal.
- Similar smoothing effects could be important for other proxies, e.g. bioturbation in marine sediments.
- for more details:
Laepplé, Münch, et al. (2018), *The Cryosphere*, 12(1), 169–187.



Similar power spectra across Antarctic sites



No significant spectral power around the wavelengths corresponding to either the **annual accumulation rate** or the average “cycle” length.

Laepple et al. (2018), Cryosphere